## YEAR 10 YEARLY PART A

## SECTION A - 30 Marks (1 mark each)

1. Solve $3-2 x<7$
A $\quad x<-2$
B $\quad x>-2$
C $\quad x<2$
D $\quad x>2$
2. $x^{\frac{3}{4}}$ is equivalent to:
A $\sqrt[3]{x^{4}}$
B $\sqrt[4]{x^{3}}$
C $\frac{3}{x^{4}}$
D $\frac{x^{3}}{4}$
3. If $\cos x^{\circ}>0$ and $\tan x^{\circ}<0$, then
A $0<x<90$
B $\quad 90<x<180$
C $180<x<270$
D $\quad 270<x<360$
4. Sarah borrowed $\$ 2500$ from a bank for 3 years. She was charged simple interest on the loan. Altogether she repaid $\$ 3287.50$. What was the rate of interest charged per annum?
A $7.98 \%$
B $10.5 \%$
C $23.95 \%$
D $31.5 \%$
5. 



The equation of the line $l$ through the origin and perpendicular to the line PQ is

A $y=4 x$
B $y=-4 x$
C $y=\frac{1}{4} x$
D $y=-\frac{1}{4 x}$
6. What is the reciprocal of $\left(\frac{1}{a}+2 a\right)$ ?
A $\frac{a}{1+2 a^{2}}$
B $\frac{1+2 a^{2}}{a}$
C $\quad a+\frac{1}{2 a}$
D $\frac{1}{1+2 a}$
7. Solve $x^{2}+5 x-3=0$
A $\quad x=\frac{-5 \pm \sqrt{37}}{2}$
B $\quad x=\frac{5 \pm \sqrt{37}}{2}$
C $\quad x=\frac{-5 \pm \sqrt{13}}{2}$
D $\quad x=\frac{5 \pm \sqrt{13}}{2}$
8. Which equation represents the line through $(-3,2)$ parallel to $y=3-4 x$ ?
A $\quad y+2=-4(x+3)$
B $\quad y-2=-3(x+3)$
C $\quad y-2=-4(x+3)$
D $\quad y-2=3(x+3)$
9. Events $A$ and $B$ are subsets of the sample space $S$ in which all outcomes are equally likely. If $n(A)=10, n(B)=15, n(S)=30$ and $P(A \cup B)=\frac{3}{5}$, then $n(A \cap B)$ is equal to:
A 7
B 9
C 18
D 25
10. The base of a triangle is twice as long as a side of a square and their areas are the same.

Then the ratio of the altitude of the triangle to the side of the square is:
A 1:4
B 1:2
C 1:1
D $2: 1$
11. At $2: 15 \mathrm{pm}$, the hour and minute hands of a clock form an angle of:
A $30^{\circ}$
B $5^{\circ}$
C $\quad 22 \frac{1^{\circ}}{2}$
D $7 \frac{1}{2}^{\circ}$
12. If $8.2^{x}=5^{y+8}$, then when $y=-8, x=$
A -4
B $\quad-3$
C 0
D 4
13. The graph $y=2 x^{2}+4 x+3$ has its

A lowest point at $(-1,1)$
B highest point at $(-1,1)$
C lowest point at $(-1,9)$
D highest point at $(-1,9)$
14. A straight line joins the points $(-1,1)$ and $(3,9)$. Its $x$-intercept is:
A $-\frac{3}{2}$
B $-\frac{2}{3}$
C $\frac{2}{5}$
D 2
15. The diameters of two circles are 8 cm and 12 cm respectively. The ratio of the area of the smaller to the area of the larger circle is:
A $2: 3$
B $1: 2$
C $\quad 9: 4$
D $4: 9$
16. When simplified, $\left(x^{-1}+y^{-1}\right)^{-1}$ is equal to:
A $x+y$
B $\frac{x y}{x+y}$
C $x y$
D $\frac{1}{x y}$
17.


PT is a tangent to the circle, centre O .
T is the point of contact.
What is the size of $\theta$ ?
A $32^{\circ}$
B $26^{\circ}$
C $64^{\circ}$
D $58^{\circ}$
18. If a worker receives a 20 percent cut in wages, he may regain his original pay exactly by obtaining a raise of:
A 20 percent
B $\quad 25$ percent
C $\quad \$ 20$
D $\quad \$ 25$
19.

| Subject | Mean Mark | SD |
| :--- | :---: | :---: |
| English | 50 | 6 |
| Maths | 60 | 8 |

What mark in Maths is equivalent to a mark of 62 in English?
A 68
B 66
C 76
D $\quad 74$
20. Water is poured into a container at a constant rate. The graph shows the depth of water in the container as it was being filled.

Which of the following containers could have been used?

A

B


21. $x^{-2} y^{\frac{1}{3}}=$
A $\quad \frac{x}{2 \sqrt[3]{y}}$
B $\quad \frac{2 \sqrt[3]{y}}{x}$
C $\frac{\sqrt[3]{y}}{x^{2}}$
D $\frac{x^{2}}{\sqrt[3]{y}}$
22. A square and an equilateral triangle have equal perimeters. The area of the triangle is $9 \sqrt{3} \mathrm{~cm}^{2}$. Expressed in centimetres, the diagonal of the square is:
A $\frac{9}{2}$
B $2 \sqrt{5}$
C $\quad 4 \sqrt{2}$
D $\frac{9 \sqrt{2}}{2}$
23. If the parabola $y=a x^{2}+b x+c$ passes through the points $(-1,12),(0,5)$ and $(2,-3)$, the value of $a+b+c$ is:
A $\quad-4$
B $\quad-2$
C 0
D 1
24.


From this diagram, which statement is correct?
A $\quad \frac{x}{\sin 70^{\circ}}=\frac{25}{\sin 30^{\circ}}$
B $\frac{x}{\sin 100^{\circ}}=\frac{25}{\sin 80^{\circ}}$
C $\frac{x}{\sin 70^{\circ}}=\frac{25}{\sin 50^{\circ}}$
D $\quad \frac{x}{\sin 70^{\circ}}=\frac{25}{\sin 80^{\circ}}$
25.


In $\triangle A B C, A B=8, B C=7, C A=6$ and side $B C$ is extended, as shown in the figure, to a point $P$ so that $\triangle P A B$ is similar to $\triangle P C A$. The length of $P C$ is:
A 6
B $\quad 7$
C 8
D $\quad 9$
26. In $\triangle A B C, \angle B A C=60^{\circ}$ and $B C=9$. Find the length of the diameter of the circle.


Diagram not to scale
A $11 \frac{1}{2}$
B $\frac{9 \sqrt{3}}{2}$
C $\quad 12 \frac{1}{2}$
D $6 \sqrt{3}$
27. There are two natural ways to inscribe a square in a given isosceles right triangle. If it is done as in Figure 1 below, then one finds that the area of the square is $441 \mathrm{~cm}^{2}$. What is the area (in $\mathrm{cm}^{2}$ ) of the square inscribed in the same $\triangle A B C$ as shown in Figure 2 below?


Figure 1


Figure 2
A 378
B 392
C 400
D 441
28. It takes 30 seconds to fill a 5 litre bucket with water. What is the rate of flow in litres per hour?
A 10
B 150
C 600
D 1200
29. A regular hexagon and a regular pentagon have a common edge as shown. Find the size of $<B A C$.

A $24^{\circ}$
B $\quad 30^{\circ}$
C $\quad 36^{\circ}$
D $45^{\circ}$
30. If $x$ varies directly as the cube of $y$, and $y$ varies directly as the fifth root of $z$, then $x$ varies directly as the $n^{\text {th }}$ power of $z$, where $n$ is:
A $\frac{1}{15}$
B $\frac{5}{3}$
C $\frac{3}{5}$
D 15
a) What is the exact value of $\cos \left(180^{\circ}-60^{\circ}\right)$ ? $\quad \mathbf{1}$
b) Solve $\cos x=1$ for $0^{0} \leq x \leq 360^{\circ} \quad 1$
c) Solve $2 x-7 \sqrt{x}=15$.
d) What is the domain and range of $y=-\sqrt{25-(x-2)^{2}}+3$ ?
e) Find the remainder when $\mathrm{P}(\mathrm{x})=x^{3}-2 x^{2}+x-1$ is divided by $(x+2)$.
f) A certain integer is between 10 and 100. Its value is 8 times the sum of its digits and if the integer is reduced by 45 , its digits are reversed. By forming a pair of simultaneous equations or otherwise find the integer.
g) i) Write down the centre and the radius of the circle with equation $(x+2)^{2}+(y+3)^{2}=4$.
ii) Find the shortest distance from the line $x-2 y-8=0$ to the centre of the circle in (i).
iii) Hence or otherwise determine the length of the chord cut off from the line by the circle.
(Giving reasons for your answer).

## Question 32. ( 20 marks) Start a new page

a) $A B C D$ is a cyclic quadrilateral in which $A B / / D C$. Given that $O$ is the centre of the circle, $\angle A O D=130^{\circ}, \angle C B D=20^{\circ}$ and $D C$ is produced to $E$ :

i) Copy the diagram neatly and include all of the given information.
ii) Find the value of $<B C E$ giving full reasons.
b) i) Neatly draw the graph of $y=3 \sin 2 x$ for $0^{\circ} \leq x \leq 360^{0}$.
ii) State the amplitude and period for $y=3 \sin 2 x$.
iii) Solve $3 \sin 2 x=-3$ for $0^{0} \leq x \leq 360^{\circ}$.
c) i) On your answer sheet about 6 cm below your final answer for b) draw an 8 cm interval on your page. Label the interval $A B$.
ii) Construct using compass and ruler only a $60^{\circ}$ angle with its vertex at $A$. Show all construction lines.
iii) Construct a perpendicular at $B$. Show all construction lines.
d) Solve $2^{2 n+2}-2^{2 n-1}=1792$.
e) Find the solution set to $6 k^{2}+13 k<8$.

## Question 33. (20 marks) Start a new page

a) In the diagram below $A$ is the point $(4,0)$ and $B$ is $(9,0)$ find the coordinates of $P$; giving reasons.

b) A hill with a uniform slope is inclined at $14^{0}$ to the horizontal. From the bottom of the hill $A$, the angle of elevation of $T$, the top of a tower $T B$ standing on a hill is $25^{\circ}$. On moving 50 m up the hill to a point $C$, the angle of elevation of $T$ is $55^{\circ}$.
i) Draw a neat diagram to represent this data. (Use a ruler).
ii) Find the size of $<A T C$.
iii) Find the length of $T A$ correct to one decimal place.
iv) Find the height of the tower $T B$ correct to two decimal places.

## QUESTION 33 continued over the page!

c) $A B C D$ is a square with $M$ the midpoint of $B C$ and $N$ is the midpoint of $C D . A M$ and $B N$ intersect at $P$.
A
D

N
i) Draw the diagram neatly to represent this data. (mark on all given data).
ii) Prove $\triangle A B M \equiv \triangle B C N$.
iii) Prove $\triangle B P M / / / \triangle B C N$.
iv) Find the area of the quadrilateral $A P N D$ if $A B=10 \mathrm{~cm}$.

## Question 34. (20 marks) Start a new page

a) Two dice are thrown. What is the probability of getting a sum under seven if it is known that at least one of the two dice shows a two?
b) It takes 45 hours for one cleaner to clean the school. How many hours are saved if six cleaners are cleaning the school at the same rate?
c) $A C$ is a tangent to the circle at $B . A E$ is a tangent to the circle at $F$. Given that $\angle \mathrm{CBD}$ is $63^{\circ}$ and $<\mathrm{DFE}$ is $49^{\circ}$, find the values of $x$ and $y$ giving reasons.
A

d) Prove that $\cot A(\operatorname{cosec} A-\cot A)=\frac{\cos A}{1+\cos A}$
e) Solve $\sin ^{2} \theta-2 \sin \theta \cos \theta=8 \cos ^{2} \theta$ to the nearest minute for $-180^{\circ} \leq \theta \leq 180^{\circ}$
f) i) Write down the equation of the line through $L(-1,2)$ with gradient $m$.
ii) Hence, determine the equation of the line through $L$, if $L$ divides the intercepts with the coordinate axis in the ratio $-2: 5$.

## YEAR 10 YEARLY 2009 EXAMINATION

## ANSWER SHEET

## SECTION A: 30 QUESTIONS [1 MARK EACH]

NAME: $\qquad$
CLASS: $\qquad$
Mark the appropriate answer with an cross $\mathbf{X}$

| 1 | A | \% | C | D |
| :---: | :---: | :---: | :---: | :---: |
| 2 | A | 2 | C | D |
| 3 | A | B | C | 8 |
| 4 | A | B | C | D |
| 5 | A | B | ) | D |
| 6 | A |  | C | D |
| 7 | < | B | C | D |
| 8 | A | B | 8 | D |
| 9 | - | B | C | D |
| 10 | A | B | 8 | D |
| 11 | A | B | 8 | D |
| 12 | A | 18 | C | D |
| 13 | A | B | C | D |
| 14 | * | B | C | D |
| 15 | A | B | C | - |
| 16 | A | 决 | C | D |
| 17 | A | 2 | C | D |
| 18 | A | D | C | D |
| 19 | A | B | 8 | D |
| 20 | A | 面 | C | D |
| 21 | A | B | d | D |
| 22 | A | B | C | W |
| 23 | A | B | ) | D |
| 24 | A | B | C |  |
| 25 | A | B | C |  |
| 26 | A | B | C | D |
| 27 | A | ¢ | C | D |
| 28 | A | B | ¢ | D |
| 29 | $\lambda$ | B | C | D |
| 30 | A | B | 20 | D |


| Question | Mark |
| :---: | :---: |
| Section A |  |
| $1-30$ | $/ \mathbf{3 0}$ |
| Section B |  |
| 31 | $/ 20$ |
| 32 | $/ 20$ |
| 33 | $/ 20$ |
| 34 | $/ \mathbf{1 1 0}$ |

Year 10 marly 2009

Question 31
a) $\begin{aligned} \cos \left(180^{\circ}-60^{\circ}\right) & =-\cos 60^{\circ}\left(\begin{array}{c}\text { mk } \\ \text { ingtor } \\ \text { inorg }\end{array}\right) \\ & =-1 / 2\end{aligned}$ $=-1 / 2$
for $0^{\circ} \leqslant x \leqslant 360^{\circ}$
b) $\cos x=1$ for $0^{\circ} \leqslant x \leqslant 360^{\circ}$ $x=0^{\circ}$ or $360^{\circ} \quad$ (1/2 each)

$$
\Rightarrow \quad 2 x-7 \sqrt{x}-15=0
$$

let $\sqrt{x}=m$

$$
\begin{align*}
\therefore & 2 m^{2}-7 m-15=0  \tag{lm}\\
& (2 m+3)(m-5)=0 \\
& m=-1 / 2 \quad \text { or } m=5 \\
& \sqrt{x}=-1 / 2 \text { or } \quad \sqrt{x}=5(1)
\end{align*}
$$ no realselution

( $12 \times x$ ) as $\sqrt{x} \geqslant 0$

$$
\therefore x=25
$$

$$
\left(y_{2} m k\right)^{\circ n} y
$$

gui) centre is $(-2,-3)$
(Ink)
radius is 2
ii) $d=\left|\frac{1 x-2+-2 x-3-8}{\sqrt{1+4}}\right|$

$$
\begin{equation*}
=\frac{|-2+6-8|}{\sqrt{5}} \tag{imk}
\end{equation*}
$$

$$
=\frac{4}{\sqrt{5}}
$$

$=\frac{4 \sqrt{5}}{5}$ units
( ink)

$\Rightarrow$

$$
\begin{align*}
& y=-\sqrt{25-(x-2)^{2}}+3 \\
& (y-3)^{2}=25-(x-2)^{2}
\end{align*}
$$



Domain is $-3 \leqslant x \leqslant 7$ ( 1 mk )
Range is $-2 \leqslant y \leqslant 3$ ( $1 \mathrm{~m} k$ )

$$
\begin{align*}
\Rightarrow & P(x)=x^{3}-2 x^{2}+x-1 \\
& P(-2)=-8-8-2-1 \\
\therefore & P(-2)=-19 \tag{2mks}
\end{align*}
$$

f) no. is 72
(by pythagoras.
(1) $4-16=2$

$$
x=\frac{2}{\sqrt{5}}
$$

$$
\text { in } x>0
$$ (perpendicular

line from centre bisect the chord.)
total 20 mks

Question 32 (20 marks)
(a) (1)

(ii) (et $\hat{B C E}=x$
(1) $\hat{A B A}=65^{\circ}$ (the angle ot the circunteop is half the angle at the cettre on thessame arc).

1) $\widehat{A B C}=65^{\circ}+20$ (som of atjacent $=85^{\circ} \quad$ anglea).
$1) \therefore \hat{B C E}=85^{\circ}$ (alterate ongles are equal; $A B|\mid(\mid C)$.

ii) amplitude is 3
period is $180^{\circ}$ Tink
i) $\quad 3 \sin 2 x=-3$ for $0^{\circ} \leqslant x \leqslant 360^{\circ}$. $x=135^{\circ}$ or $315^{\circ}$ ( 1 mk )

(i) Ink (8cm and At B labelled)
(ii) 2 mks (deduct maks, if there's no constrution).
(iii) 2 mks
(d)

$$
\begin{align*}
2^{2 n+2}-2^{2 n-1} & =1792 \\
2^{2 n-1}\left(2^{3}-1\right) & =1792 \\
\therefore 2^{2 n-1} & =256 \\
2^{2 n-1} & =2^{8}  \tag{1}\\
2 n-1 & =8 \\
2 n & =9 \\
\therefore n & =4^{1 / 2} \tag{1}
\end{align*}
$$

(1792:7)

$$
\text { e) } \begin{align*}
6 k^{2} & +13 k<8 \\
6 k^{2}+13 k-8 & <0  \tag{12}\\
(3 k+8)(2 k-1) & <0 \tag{1}
\end{align*}
$$



$$
\therefore-2^{2 / 3}<k<1 / 2
$$

$\frac{\text { Question } 33}{(20 \text { marks) }) ~}$
) $O P^{2}=O A, O B \quad$ (tangent squared equals the product of the intersects on the secant.).

$$
O P^{2}=4 \times 9
$$

$$
o p^{2}=36(\sqrt{11})
$$

$o p=6 \quad(a s$ op>o its a length)
(120) (1)


د) (1)


(i) $\overline{T A C}=11^{\circ}\left(25^{\circ}-14^{\circ}\right)$
ii) $A \hat{T C}=41^{\circ}-11^{\circ}$ (exterior angle ot $\triangle T A C$
(1)

$$
=30^{\circ}
$$ equals sum of 2 interior opposite angles.).

ii) $\hat{A C T}=139^{\circ}$ (angle sum of a triangle is $180^{\circ}$.)

$$
\begin{align*}
& \frac{50}{\sin 30^{\circ}}=\frac{T A}{\sin 139^{\circ}}  \tag{1/2}\\
& 100 \times \sin 139^{\circ}=T A \\
& T A=65.6059029 \\
& T A=65.6 \mathrm{~m} \quad \text { (1 d.p.). } \tag{2}
\end{align*}
$$

v) $\hat{A B D}=76^{\circ}$ (angle sum of $\triangle A B O$ is $180^{\circ}$ ).
$\hat{C B T}=104^{\circ}$ (sum of adjacent angles
In $\triangle A T C$, on a st. angle is $180^{\circ}$ ).

$$
\begin{aligned}
\frac{T_{C}}{\sin 11^{\circ}} & =\frac{50}{\sin 30^{\circ}} \\
T C & =100 \cdot \sin 11^{\circ}
\end{aligned}
$$

I $\triangle C B T$,

$$
\begin{aligned}
\frac{T B}{\sin 41^{\circ}} & =\frac{T C}{\sin 104^{\circ}} \\
T B & =\frac{100 \sin 11^{\circ} \sin 41^{\circ}}{\sin 104^{\circ}} \\
& =\frac{12.51819642}{0.9702957263} \\
& =12.90142385
\end{aligned}
$$

$\therefore$ Rowe is 12.9 m high.


1 mk (all data must be preset.).
(ii) In As $A B M, B C N$
$A B=B C$ (sides of a square are all equal.).
$B M=C N$ (midpoints of equal sides)
$A B_{M}=\hat{B C N}$ (all angles in a square are $90^{\circ}$ ).
$\therefore \triangle A B M \equiv \triangle B C N$ (SAB.)
(iii) In $\Delta$ 's $B P M, B C N$

$\hat{A M B}=\hat{B N C}$ (corresponding angles in congruent tingles are equal l
$\hat{B}$ is common
$\therefore \triangle B P M \| \triangle B C N$ (equiangular)
(iv) $A B$ is 10 cm data
area of $\triangle A B M=\frac{1}{2} \times 10 \times 5$

$$
\begin{equation*}
=25 \mathrm{~cm}^{2} \tag{3}
\end{equation*}
$$

area of $\triangle B N C=25 \mathrm{~cm}^{2}$
ratio of $\triangle B P M: \triangle B C N=1: \sqrt{5}$
ratio of areas $=1: 5$

$$
=x: 25 \quad \therefore x=5 \mathrm{~cm}^{2}
$$

area of APND $=100-25-25+5=55$ er

Question 34 (20mks)
a) $P(\operatorname{sum}<7)$.


$$
\therefore P(\operatorname{sum}<7)=\frac{7}{11}
$$

b) 45 hours for 1 deaner
$\frac{45}{6}$ for 6 cleaners $=7^{1 / 2}$

$$
\begin{align*}
\text { hours saved } & =45-7^{1 / 2}  \tag{2}\\
& =37^{1 / 2} \text { hours. }
\end{align*}
$$

(f)(i) $y-2=m(x+1)$

(ii)

$$
\begin{align*}
& A(0, m+2) \\
& B\left(-\frac{m-2}{m}, 0\right) \tag{112}
\end{align*}
$$

$x$ intercept: $y$ intercept $-2: 5$

$$
\begin{gathered}
\left(-\frac{m-2}{m}, 0\right) \\
-2: 5
\end{gathered}
$$

$$
(-1,2)=\left(\frac{-2 \times 0+5\left(-\frac{m-2}{m}\right)}{3}, \frac{5 \times 0+-2(m+2)}{3}\right)
$$

$$
\begin{gather*}
-3=\frac{-5 m-10}{m} \\
-3 m=-5 m-10 \\
2 m=-10 \\
m=-5 \tag{1}
\end{gather*}
$$

$$
\text { or } 5 x+y+3=0
$$



Join $B$ to $F$
$\hat{B F D}=63^{\circ}$ (angle in the alternate seaneert equals angle between chords $\tan 8=-t y$.
Similarly $\hat{F B} D=49^{\circ}$

$$
\therefore x=180^{\circ}-49-63^{\circ}\binom{\text { angle sun } \delta}{\triangle B P F \text { is } 180^{\circ}}
$$

$\hat{A B F}=68^{\circ}$ (angl sum of $\hat{A B C}$ is $180^{\circ}$ ).
similarly $A \hat{F B}=65^{\circ}$

$$
\begin{align*}
& \therefore y=180^{\circ}-2\left(68^{\circ}\right) \quad(\text { angle } \operatorname{sim} \text { of }  \tag{1}\\
&\left.\triangle A B F \text { is } 180^{\circ}\right) . \\
& y=44^{\circ}
\end{align*}
$$

(d)

$$
\begin{align*}
\text { LHS } & =\cot A(\operatorname{cosec} A-\cot A) \\
& =\frac{\cos A}{\sin A}\left(\frac{1}{\sin A}-\frac{\cos A}{\sin A}\right)  \tag{1}\\
& =\frac{\cos A(1-\cos A)}{\sin ^{2} A} \\
& =\frac{\cos A(1-\cos A)}{(1-\cos A)(1+\cos A)}  \tag{1}\\
& =\frac{\cos A}{1+\cos A}  \tag{1}\\
& =\text { RHS. }
\end{align*}
$$

(e) $\sin ^{2} \theta-2 \sin \theta \cdot \cos \theta-8 \cos ^{2} \theta=0$

$$
\begin{aligned}
\tan ^{2} \theta-2 \tan \theta-8 & =0 \\
(\tan \theta-4)(\tan \theta+2) & =0 \\
\tan \theta & =4 \quad \text { or } \tan \theta
\end{aligned}=-2(1 / 2)
$$

$$
\begin{equation*}
\therefore \theta=7 \underbrace{\circ}_{c} 58^{\circ},-104^{\circ} 2^{\prime},-\underbrace{63^{\circ} 26^{\prime}, 116^{\circ} 34^{\prime}}_{1} \tag{1}
\end{equation*}
$$



Join $B$ to $F$

$$
\therefore x=68^{\circ}
$$

