



**Question 1****(8 marks)**

- a) Simplify  $\sqrt{75} + \sqrt{32} - \sqrt{27}$  2
- b) Express  $0.\dot{1}2\dot{5}$  as a fraction in simplest form. 1
- c) Evaluate  $\frac{\sqrt{16.98+9.074}}{4.99}$  correct to 3 significant figures 2
- d) Simplify  $\frac{x^2 + 12x + 36}{x^2 + 6x}$  2
- e) Fully factorise  $8 - 27d^3$  1

**Question 2 (start a new page)****(8 marks)**

- a) Solve for  $x$  :
- (i)  $\frac{2x}{3} - 4 = x + 2$  2
- (ii)  $(x + 3)^2 = 7$  2
- b) Express  $\frac{x+1}{x^2-1} - \frac{x-1}{x+1}$  as a fraction in its lowest terms 3
- c) Express  $a^{-3} \times (8a^6)^{\frac{1}{3}}$  in simplest form, without the use of negative indices 1

**Question 3 (start a new page)****(8 marks)**

- a) Solve simultaneously  $x - 4y + 12 = 0$  and  $y = 3 - 2x$ . 3
- b) Solve  $2x^2 - 5x - 12 = 0$  2
- c) Solve and sketch the solution set of  $|4 - 3x| < 7$  3

**Question 4 (start a new page)****(8 marks)**

- a) Sketch the function and state the domain and range of the function

3

$$y = \frac{1}{2x - 3}$$

- b) When a number is subtracted from its square the result is 56. Write an equation to represent this information and hence find the answer.

3

- c) Solve for x:
- $3^x = 9^{x-2}$

2

**Question 5 (start a new page)****(8 marks)**

- a) Explain whether
- $f(x) = x^3 - x$
- is an odd function, even function or neither.

2

- b) State the domain and range of the function
- $y = 2^{-x}$

2

- c) Draw a neat sketch of
- $y = x^2 - 7x + 12$
- showing x and y intercepts and vertex
- 
- Hence state the domain and range.

4

**Question 6 (start a new page)****(8 marks)**

- a) Simplify
- $\frac{m^3 + m^2}{x^2 - x} \div \frac{m+1}{x-x^3}$
- as a single fraction in simplest form.

3

- b) Fully factorise
- $w^4 - 16$

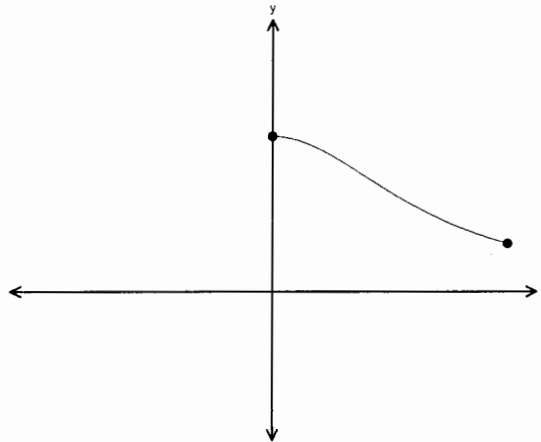
2

- c) Show that
- $\frac{3\sqrt{2} - 2\sqrt{3}}{3\sqrt{2} + 2\sqrt{3}}$
- can be expressed in the form
- $a + b\sqrt{6}$
- and find
- $a$
- and
- $b$
- .

3

**Question 7 (start a new page)****(7 marks)**

- a) Solve  $x^2 - 3x - 1 = 0$  correct to 2 decimal places. 2
- b) Solve  $|2x - 2| = 6x + 10$  Check your solution 3
- c) i) What is the condition for an even function 1  
ii) Complete the graph of the function on your answer sheet, so it represents an even function 1

**Question 8 (start a new page)****(8 marks)**

- a) If  $f(x) = 3x^2 - 5x + 4$  and  $g(x) = 2x + 10$  find:
- i)  $f(2) + f(-2)$  1
- ii) the values of  $x$  for which  $f(x) = 6$  2
- iii) the values of  $x$  for which  $f(x) = g(x)$  2
- b) Show the region of the number plane where the following hold simultaneously: 3
- $$(x-2)^2 + y^2 \leq 4$$
- $$y \leq 0$$

END OF EXAMINATION



**QUESTION 1**

a)  $\sqrt{75} + \sqrt{32} - \sqrt{27} = 5\sqrt{3} + 4\sqrt{2} - 3\sqrt{3}$   
 $= \underline{\underline{2\sqrt{3} + 4\sqrt{2}}}$

b) Let  $x = 0.\dot{1}\dot{2}\dot{5}$   
 $10x = 1.\dot{2}\dot{5}$   
 $1000x = 125.\dot{2}\dot{5}$   
 $990x = 124$   
 $x = \frac{124}{990}$   
 $\therefore 0.\dot{1}\dot{2}\dot{5} = \underline{\underline{\frac{62}{495}}}$

c)  $\underline{\underline{1.02}}$  (3 sig fig)

d)  $\frac{(x+6)(x+6)}{x(x+6)} = \underline{\underline{\frac{x+6}{x}}}$

e)  $2^3 - (3d)^3 = \underline{\underline{(2-3d)(4+6d+9d^2)}}$

**Question 2**

a) i)  $\frac{2x}{3} - 4 = x + 2$   
 $2x - 12 = 3x + 6$   
 $-18 = x$

$\therefore x = \underline{\underline{-18}}$

ii)  $\underline{\underline{(x-11)(x+8)}}$

b)  $\frac{(x+1)}{(x-1)(x+1)} - \frac{(x-1)}{x(x+1)}$   
 $\frac{x(x+1) - (x-1)^2}{x(x-1)(x+1)}$   
 $\frac{x^2 + x - [x^2 - 2x + 1]}{x(x-1)(x+1)}$   
 $\frac{\cancel{x^2} + x - \cancel{x^2} + 2x - 1}{x(x-1)(x+1)}$   
 $\underline{\underline{\frac{3x-1}{x(x-1)(x+1)}}}$

c)  $\frac{x+1}{(x+1)(x-1)} - \frac{x-1}{x+1} = \frac{(x+1)^2 - (x-1)^2}{(x+1)(x-1)}$   
 $= \underline{\underline{\frac{4x}{(x+1)(x-1)}}}$

d)  $a^{-3} \times 2a^2 = 2a^{-1}$   
 $= \underline{\underline{\frac{2}{a}}}$

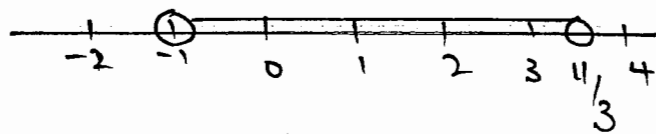
**Question 3**

a)  $x - 4(3 - 2x) + 12 = 0$   
 $x - 12 + 8x + 12 = 0$   
 $9x = 0$   
 $\therefore x = 0$

$\underline{\underline{y = 3}}$

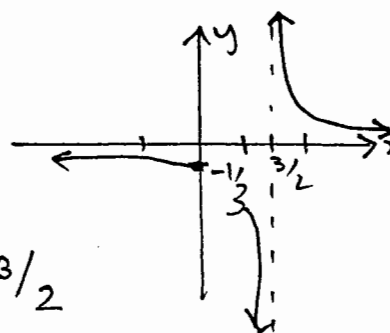
b)  $x = \frac{5 \pm \sqrt{25 - 4 \cdot 2 \cdot -12}}{4}$   
 $x = \frac{5 \pm \sqrt{121}}{4}$   
 $x = \underline{\underline{4, -3/2}}$

c)  $4 - 3x < 7$        $4 - 3x > -7$   
 $-3x < 3$                $-3x > -11$   
 $x > -1$                    $x < 11/3$   
 $-1 < x < 11/3$



**Question 4**

a)  $2x - 3 = 0$   
 $2x = 3$   
 $\therefore x = 3/2$   
 $\therefore D: x \neq 3/2$



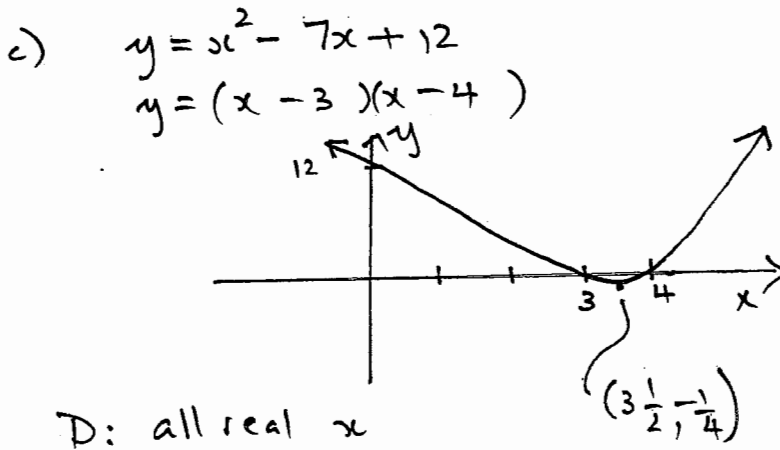
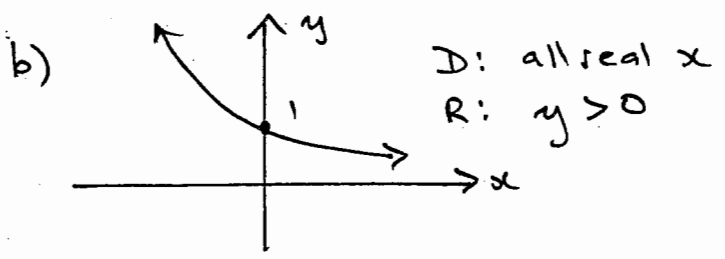
R: all  $y, y \neq 0$

a) let  $x$  be number  
 $x^2 - x = 56$   
 $x^2 - x - 56 = 0$   
 $(x+7)(x-8) = 0$   
 $x = -7, x = 8$

b)  $3^x = 3^{2(x-2)}$   
 $x = 2x - 4$   
 $\therefore 4 = x$   
 ii  $x = 4$

Question 5

a)  $f(x) = x^3 - x$   
 $f(-x) = (-x)^3 + x$   
 $= -x^3 + x$   
 $-f(-x) = x^3 - x$   
 $\therefore f(x) = -f(-x)$  odd



D: all real  $x$   
 R:  $y \geq -4$

Question 6

a)  $\frac{m^2(m+1)}{x(x-1)} \times \frac{x(1-x^2)}{(m+1)}$   
 $\frac{m^2(1-x)(1+x)}{-(1-x)}$   
 $-m^2(1+x)$

b)

$w^4 - 16$   
 $(w^2 - 4)(w^2 + 4)$   
 $(w-2)(w+2)(w^2 + 4)$

c)  $\frac{3\sqrt{2} - 2\sqrt{3}}{3\sqrt{2} + 2\sqrt{3}} \times \frac{3\sqrt{2} - 2\sqrt{3}}{3\sqrt{2} - 2\sqrt{3}}$   
 $\frac{18 - 6\sqrt{6} - 6\sqrt{6} + 12}{6}$   
 $\frac{30 - 12\sqrt{6}}{6}$   
 $5 - 2\sqrt{6}$   
 $\therefore a = 5 \quad b = -2$

Question 7

a)  $x = \frac{3 \pm \sqrt{9 - 4 \cdot 1 \cdot -1}}{2}$   
 $x = \frac{3 \pm \sqrt{13}}{2}$   
 $x = 3.30, -0.30$

$$\begin{aligned} b) \quad 2x - 2 &= 6x + 10 \\ -12 &= 4x \\ x &= -3 \end{aligned}$$

check:

$$\begin{aligned} |-6 - 2| &= -18 + 10 \\ 8 &\neq -8 \\ \therefore x = -3 &\text{ not solution} \end{aligned}$$

$$2x - 2 = -6x - 10$$

$$\begin{aligned} 8x &= -8 \\ x &= -1 \end{aligned}$$

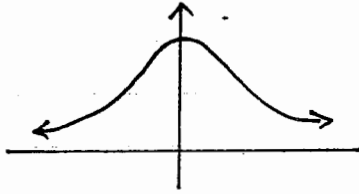
check:

$$\begin{aligned} |-2 - 2| &= -6 + 10 \\ 4 &= 4 \\ &\text{true} \end{aligned}$$

$\therefore x = -1$  only solution

c) i)  $f(x) = f(-x)$

ii)



### Question 8

a) i)  $f(2) + f(-2)$   
 $= (12 - 10 + 4) + (12 + 10 + 4)$   
 $= \underline{\underline{28}}$

ii)  $3x^2 - 5x + 4 = 6$   
 $3x^2 - 5x - 2 = 0$   
 $(3x + 1)(x - 2) = 0$   
 $x = -1/3, x = 2$

iii)  $3x^2 - 5x + 4 = 2x + 10$   
 $3x^2 - 7x - 6 = 0$   
 $(3x + 2)(x - 3) = 0$   
 $x = -2/3, x = 3$

b)

