

Name:	
Геаcher:	

Set By: IM

Wednesday 17 March 2004

- Attempt ALL questions. Begin each question on a new sheet of paper.
- Only Board approved calculators (excluding graphic calculators) may be used.
- Total possible mark is 34. Marks may be deducted for insufficient or illegible work.
- TIME ALLOWED: 45 minutes

Question 1:

(5 marks)

Given $f(x) = x^2 + 3x$ find, in simplest form:

(a)
$$f(1-a)$$

2

(b)
$$\frac{f(x+h)-f(x)}{h}$$

3

Question 2: Begin a new sheet of paper

(6 marks)

Sketch the graphs of the following functions indicating any intercepts and asymptotes.

(a)
$$y = 3^x + 1$$

3

(b)
$$y = \log_{10}(x-1)$$

3

Question 3: Begin a new sheet of paper

(7 marks)

(a) (i) State the domain and range of $y = \sqrt{1-x}$.

2

(ii) Sketch, on a number plane, the graph of $y = \sqrt{1-x}$, showing the coordinates of the x intercept.

2

(b) Sketch the region in the number plane satisfying the following pair of inequalities:

3

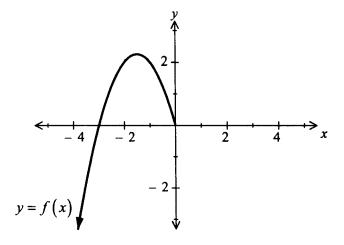
$$x^2 + (y-4)^2 \le 16$$
 and $y \ge 4 - x^2$

Question 4: Begin a new sheet of paper

(6 marks)

(a) Copy and then complete the graph of y = f(x) below so that it is an even function.





(b) Prove that
$$f(x) = x^3 - x$$
 is an odd function.

2

3

(c) Solve for
$$x$$
 if:

$$|4-x^2|=2$$

(5 marks)

Question 5: Begin a new sheet of paper

Consider the function $y = \frac{x+1}{x-2}$.

(a) For what value of x is
$$y = \frac{x+1}{x-2}$$
 undefined?

1

1

(c) Sketch the graph of
$$y = \frac{x+1}{x-2}$$
 labelling clearly any important features.

3

Question 6 commences on the next page ...

2

Question 6: Begin a new sheet of paper

(5 marks)

(a) On the same set of axes, sketch the graphs of: (i)

2

- y = |x-2| and (β) y = 4-x (α)
- (ii) Hence or otherwise solve:

$$(\alpha) \quad |x-2| = 4-x$$

1

$$(\beta) \qquad |x-2| \geq 4-x$$

1

Find the value(s) of a such that |x-2| = a-x has no solutions. (b)

1

END OF TASK