

Question 1 (10 Marks)	Marks
a) Simplify $\frac{a^2 - 9}{(a+3)^2}$	1
b) Expand and simplify $(a+b)^2 - (a-b)^2 + (a-b)(a+b)$	2
c) Factorize completely $x^4 - 16$	2
d) Simplify $\frac{x^2 + 5x + 6}{x^2 - 4} \div \frac{x^2 - 1}{x^2 - x - 2}$	3
e) Factorize completely $8x^3 - 27y^3$	2

Question 2 (10 Marks) *Start a new page*

- a) Solve $x^2 + 6x - 1 = 0$ by completing the square, leaving your answer in simplest surd form. 2
- b) Express $x = 0.\dot{3}\dot{6}$ as a rational number. 2
- c) The weekly wages of five carpenters and three apprentices amount to \$1880 and the wages of three carpenters and five apprentices amounts to \$1640. By constructing a pair of simultaneous equations, find the weekly wages of both a carpenter and an apprentice. 3
- d) Find the values of a and b if $a + b\sqrt{7} = \frac{1}{7 + \sqrt{7}}$ 3

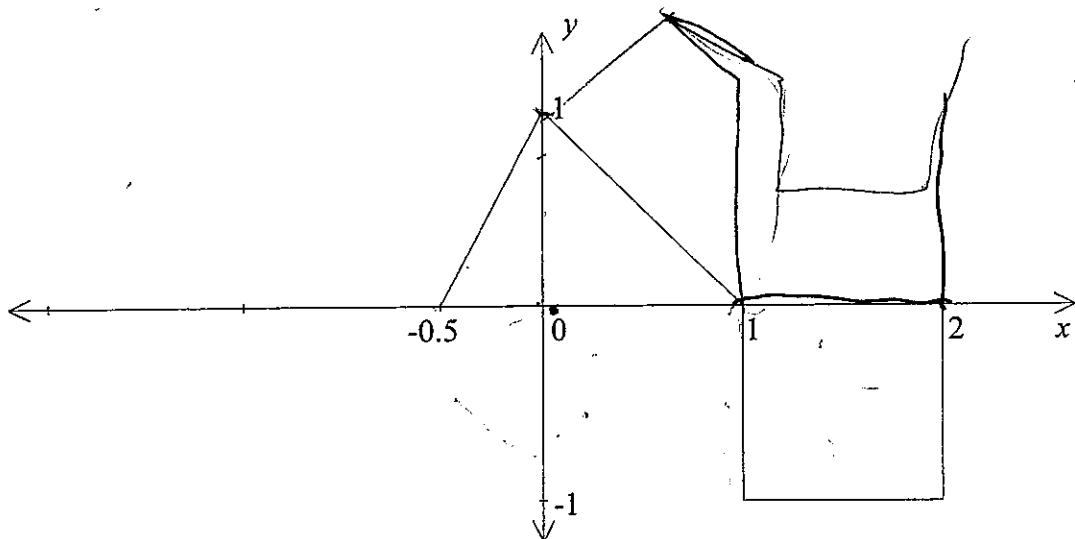
Question 3 (10 Marks) *Start a new page*

- a) Let $f(x) = 2x + 5$
- i) Find $g(x)$, the inverse of $f(x)$. 1
 - ii) Show that $f(g(x)) = g(f(x))$ 2
- b) Let $y = 9x - x^3$
- i) Sketch the graph of this function clearly showing all intercepts. 3
 - ii) From your graph, write down the region for which $9x - x^3 < 0$ 1
- c) Sketch $x + |y + 1| = 1$ indicating all important points. 3

Question 4 (10 Marks) *Start a new page*

Marks

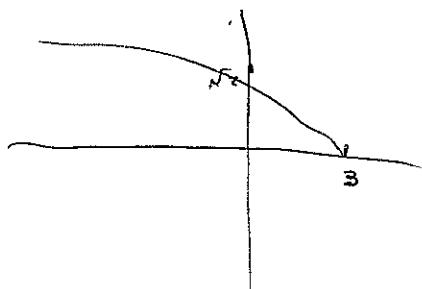
- a) Graph $f\left(x - \frac{1}{2}\right) + 1$, if $f(x)$ has the following graph. 2



- b) Sketch $y = \sqrt{3-x}$ 2

- c) Solve the inequation: $\frac{5}{x-4} \geq 1$. 3

- d) Prove whether the function $f(x) = e^x + \frac{1}{e^x}$ is odd, even or neither. 3



END OF PAPER

Q1 a) $\frac{a^2 - 9}{(a+3)^2} = \frac{(a-3)(a+3)}{(a+3)^2} = \frac{a-3}{a+3}$

(1M)

OK

b) $(a+b)^2 - (a-b)^2 + (a-b)(a+b)$
 $= a^2 + 2ab + b^2 - (a^2 - 2ab + b^2) + a^2 - b^2$
 ~~$= a^2 + 2ab + b^2 - a^2 + 2ab - b^2 + a^2 - b^2$~~
 $= a^2 + 4ab - b^2$ (1M)

(1M)

c) $x^4 - 16 = (x^2 - 4)(x^2 + 4)$ (1M) $= (x-2)(x+2)(x^2 + 4)$ (1M)

d) $\frac{x^2 + 5x + 6}{x^2 - 4} \div \frac{x^2 - 1}{x^2 - x - 2} = \frac{(x+2)(x+3)}{(x+2)(x-2)} \times \frac{(x+2)(x-3)}{(x-1)(x+1)}$
 $= \frac{x+3}{x-1}$

IM Factorising
IM inverting

1M answer
correct

e) $8x^3 - 27y^3 = (2x - 3y)(4x^2 + 6xy + 9y^2)$
 IM correct terms IM correct signs

Q2 a) $x^2 + 6x - 1 = 0$

b) let $x = 0.3\bar{6}3636\ldots$
 $\therefore 100x = 36.\overline{363636}\ldots$ (1M)

$x^2 + 6x + 9 = 1 + 9$

$\therefore 99x = 36$

$(x+3)^2 = 10$ (1M)

$x = \frac{36}{99} = \frac{4}{11}$ (1M)

$x = \pm \sqrt{10}$

$x = -3 + \sqrt{10}, -3 - \sqrt{10}$ (1M)

c) wages of carpenters = c wages of apprentices = a

(1M) $\begin{cases} 5c + 3a = 1880 \\ 3c + 5a = 1640 \end{cases} \times 5$

(1M) $\begin{cases} 25c + 15a = 9400 \\ \frac{9c + 15a}{16c} = 4920 \\ \therefore 16c = 4480 \end{cases}$

$c = 280 \therefore a = 160$ (1M)

d) $a + b\sqrt{7} = \frac{1}{7+\sqrt{7}} \times \frac{7-\sqrt{7}}{7-\sqrt{7}}$ (1M) $= \frac{7-\sqrt{7}}{42}$ (1M)
 $\therefore a = \frac{1}{6} \quad b = -\frac{1}{42}$. (1M)

y = ...

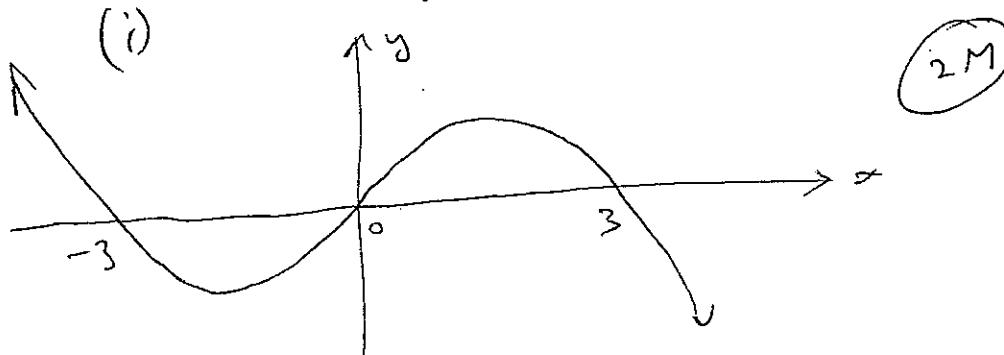
a) $f(x) = 2x + 5$
 $y = 2x + 5$ $\therefore x = 2y + 5 \quad \therefore y = \frac{x-5}{2}$

(i) $\therefore g(x) = \frac{x-5}{2}$ (1M)

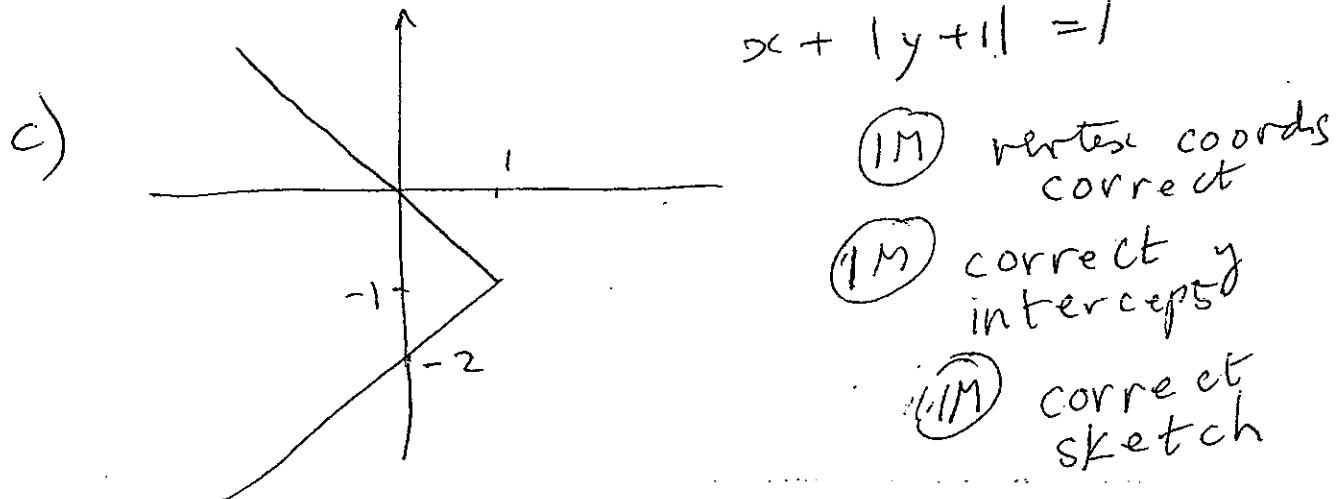
(ii) $f(g(x)) = f\left(\frac{x-5}{2}\right) = \cancel{x}\left(\frac{x-5}{\cancel{x}}\right) + 8 = x$ (1M)

$g(f(x)) = g(2x+5) = \cancel{2x+8-8} = x$ (1M)

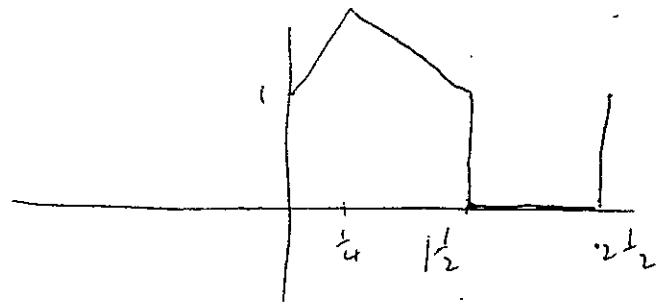
b) $y = 9x - x^3$ $-x^3 \searrow$
 $= x(9-x^2) = x(3-x)(3+x)$
 $x \text{ intercepts or } 0, 3, -3$
 $y \text{ intercept is } y=0$



(ii) $9x - x^3 < 0$
 $\therefore x > 3 \text{ or } -3 < x < 0$ (1M)

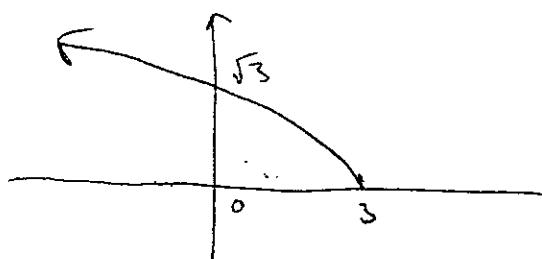


Q4 a)



1 each
for vert/horiz
shifts

b)



$$g = \sqrt{3-x}$$

$$3-x \geq 0$$

$$x \leq 3$$

c)

$$\frac{5}{x-4} (x-4)^2 \geq (x-4)^2 \leftarrow \text{(IM)} x \neq 4$$

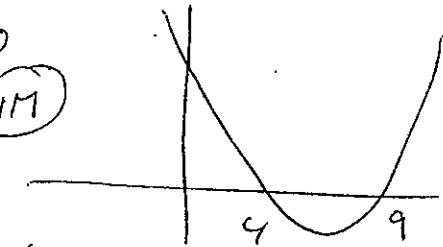
$$(x-4)(x-4-5) \leq 0$$

$$(x-4)(x-9) \leq 0$$

$$D: 4 < x \leq 9$$

(Is suggest we don't be too harsh about $x \leq 4$ at this stage.)

(IM)



d)

$$f(x) = e^x + \frac{1}{e^x}$$

$$f(-x) = e^{-x} + \frac{1}{e^{-x}}$$

(IM)

$$= \frac{1}{e^x} + e^x$$

(IM)

$$= f(x)$$

$\therefore f(x)$ is even

(IM)