

Name : _____

Teacher : _____

SYDNEY TECHNICAL HIGH SCHOOL

**MATHEMATICS
Year11**

PRELIMINARY ASSESSMENT

TASK 2

JULY 2003

Time allowed: 70 minutes

Q1	Q2	Q3	Q4	Q5	Q6	Q7	Q8	TOTAL
/8	/8	/8	/8	/8	/8	/9	/9	/66

Instructions:

- Show all necessary working in every question.
- Attempt all questions.
- All questions are not of equal value.
- Full marks may not be awarded for careless or badly arranged work.
- Approved calculators may be used.
- These questions are to be handed in with your answers.

QUESTION 1: (8 marks)

- (1) a. Write down the exact value of $\tan 30^\circ$
- (3) b. Factorise
- i. $x^3 - 27$
- ii. $x^2 - xy - 3x + 3y$
- (2) c. Solve $|2x+1| \leq 7$
- (2) d. Solve $3x^2 - 14x - 5 = 0$

QUESTION 2: (8 marks)

- (2) a. Rationalise the denominator of

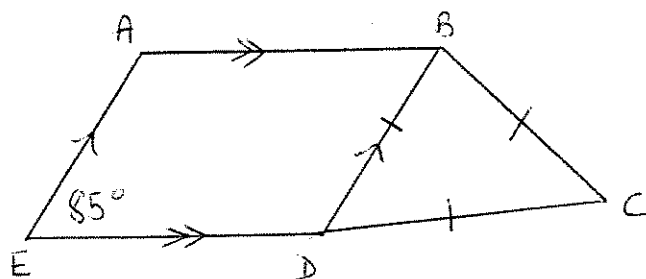
$$\frac{3}{\sqrt{7}+2}$$

- (3) b. Solve simultaneously

$$2x + 3y + 1 = 0$$

$$3x - y = 4$$

- (3) c. Find the value of $\angle ABC$, giving reasons.



Not to scale

QUESTION 3: (8 marks)

- (6) a) Write down the exact value of:

i. $\cos 225^\circ$

ii. $\sec(-30^\circ)$

iii. $\tan^2 390^\circ$

- (2) b) If $\cos \theta = p$ and $\sin \alpha = q$, find an expression for,

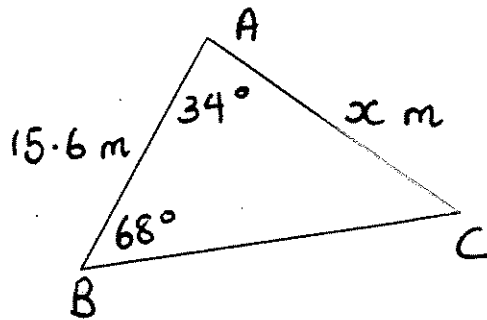
$$\cos(360^\circ - \theta), \sin(180^\circ + \alpha)$$

QUESTION 4:

(8 marks)

(1) a. Solve $\sin(2x)^\circ = \cos(40 + x)^\circ$, where $0^\circ \leq x \leq 90^\circ$

(5) b.



i. Find x , correct to the nearest centimetre.

ii. Calculate the area of $\triangle ABC$, correct to the nearest square metre.

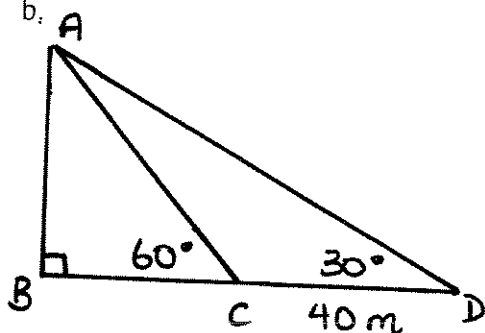
(2) c. The midpoint M of the interval AB is $(1, -3)$
Find the co-ordinates of B given A is $(7, 2)$

QUESTION 5:

(8 marks)

(3) a. If $\sin \alpha = m$ and α is obtuse, find an expression for $\cos \alpha$

(5) b.



i. Write down the size of $\angle ACD$

ii. Find the length of AC

iii. Find the exact length of AB

QUESTION 6: (8 marks)

(2) a. Solve $\cos x = -\frac{1}{2}$ for $-180^\circ \leq x \leq 180^\circ$

(3) b. Solve $3\tan^2 x - 1 = 0$ for $0^\circ \leq x \leq 360^\circ$

(3) c. Solve $\sec 2x = 1$ for $0^\circ \leq x \leq 360^\circ$

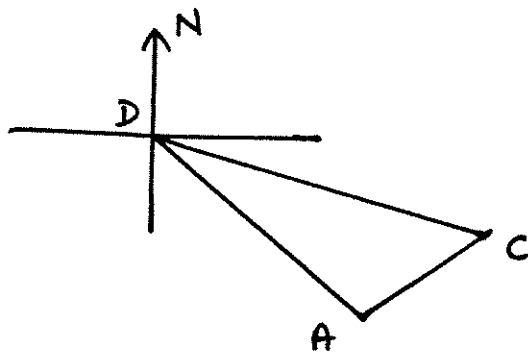
QUESTION 7: (9 marks)

(4) a. Prove that

$$\frac{\sin \theta}{1 + \cos \theta} + \frac{1 + \cos \theta}{\sin \theta} = 2 \operatorname{cosec} \theta$$

(5) b. Daffy walks on a bearing of 150° T, from D, for 12km before changing his course at

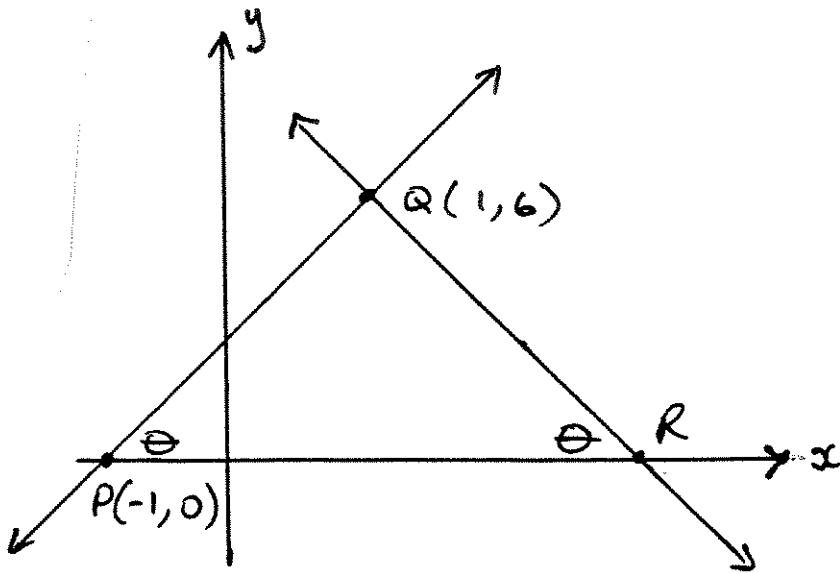
A to 040° T and continuing for 8km to C.



- i Copy the diagram and explain why $\angle DAC = 70^\circ$
- ii How far is Daffy from his starting point?
- iii What is the bearing of C from Daffy's starting point D?

QUESTION 8: (9 marks)

Triangle PQR is isosceles with
P (-1,0), Q (1,6)



- (1) a. Find the distance of PQ
- (2) b. Find the equation of the line through P and Q
- (1) c. Find the size of θ , correct to the nearest degree
- (3) d. Find the equation of the QR, and hence find the co-ordinates of R
- (2) e. Find the perpendicular distance from P to QR

Question 3

YEAR 11 TERM 3
COMMON TEST
2 UNIT

Question 1

a) $\tan 30^\circ = \frac{1}{\sqrt{3}}$ ①

b) $x^3 - 27 = (x-3)(x^2 + 3x + 9)$ ①

ii. $x^2 - xy - 3x + 3y$
 $= x(x-y) - 3(x-y)$ ①
 $= (x-y)(x-3)$ ①

c) $|2x + 1| \leq 7$
 $2x + 1 \leq 7$ $-2x - 1 \leq 7$
 $2x \leq 6$ $-2x \leq 8$
 $x \leq 3$ ① $x \geq -4$ ①

d) $3x^2 - 14x - 5 = 0$
 $\begin{matrix} 3x & + & 1 \\ x & - & 5 \end{matrix}$
 $(3x + 1)(x - 5) = 0$
 $x = -\frac{1}{3}$ ①, $x = 5$ ①

Question 2

a) $\frac{3}{\sqrt{7}+2} \times \frac{\sqrt{7}-2}{\sqrt{7}-2} = \frac{3(\sqrt{7}-2)}{7-4}$
 $= \sqrt{7}-2$ ①

b) $2x + 3y = -1$
 $9x - 3y = 12$ ①

$11x = 11$
 $x = 1$ ①
 $y = -1$ ①

c) $\angle DBC = 60^\circ$ ($\triangle BDC$ is equilateral)
①

① $\angle ABD = 85^\circ$ (opp L's in //ogram equal)

∴ $\angle ABC = 60 + 85 = 145^\circ$ (sum of adj L's)

a) i. $\cos 225^\circ = -\cos 45^\circ$
 $= -\frac{1}{\sqrt{2}}$ //
ii. $\sec(-30^\circ) = \frac{1}{\cos 30^\circ} = \frac{2}{\sqrt{3}}$ //
iii. $\tan^2 390^\circ = (\tan 30^\circ)^2$
 $= (\frac{1}{\sqrt{3}})^2$ //
 $= \frac{1}{3}$

b) $\cos(360 - \theta)$ $\sin(180 + \alpha)$
(4th quad) (3rd quad)
 $= \cos \theta - \sin \alpha$ ✓
 $= p - q$
 $= -pq$ ✓

Question 4

a) $\sin 2x = \cos(40 + x)$
 $2x + 40 + x = 90$
 $3x = 50$
 $x = 50/3$ ✓ ①

b) i. $\frac{x}{\sin 68^\circ} = \frac{15.6}{\sin 78^\circ}$ ① = 78°
 $x = \frac{15.6 \sin 68^\circ}{\sin 78^\circ}$ ① = Sine rule
 $= 14.79$ m ① Ans correct to 2 dec pl.

ii. $A = \frac{1}{2} ab \sin C$ ①
use ans to part (i) $= \frac{1}{2} \times 15.6 \times 14.79 \times \sin 34^\circ$
 $= 64.509...$
 $= 65$ m² > ① either

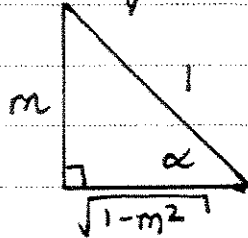
c) (x, y) $(7, 2)$ Midpt $(1, -3)$
 $\frac{x+7}{2} = 1$ $\frac{y+2}{2} = -3$
 $x+7 = 2$ $y+2 = -6$
 $x = -5$ $y = -8$ ①
∴ $B(-5, -8)$

marks
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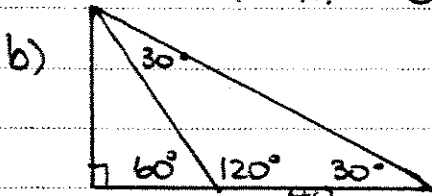
Question 5

2nd quad

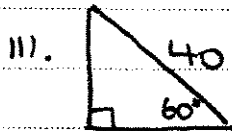
a) $\sin \alpha = m$



$\therefore \cos \alpha = -\frac{\sqrt{1-m^2}}{1}$
 $= -\sqrt{1-m^2}$ ①



- i. $\angle ACD = 120^\circ$ ①
- ii. $AC = 40$ m $\triangle ACD$ is isosceles. ①



$\sin 60^\circ = \frac{AB}{40}$ ①
 $AB = 40 \sin 60^\circ$
 $= 40 \frac{\sqrt{3}}{2}$ ①
 $= 20\sqrt{3}$ ①

Question 6

a) $\cos x = -\frac{1}{2}$ $-180^\circ \leq x \leq 180^\circ$
 $x = 120^\circ, -120^\circ$ ① ①
 $\cos 60^\circ = \frac{1}{2}$

b) $3 \tan^2 x - 1 = 0$
 $\tan x = \pm \frac{1}{\sqrt{3}}$ ①
 $x = 30^\circ, 150^\circ, 210^\circ, 330^\circ$ ②

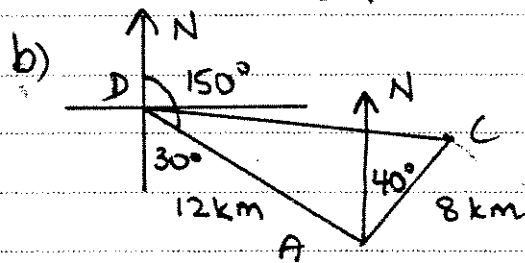
c) $\sec 2x = 1$
 $\therefore \cos 2x = 1$ ①
 $2x = 0^\circ, 360^\circ, 720^\circ$ ①
 $x = 0^\circ, 180^\circ, 360^\circ$ ①

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Question 7

a) LHS = $\frac{\sin \theta}{1 + \cos \theta} + \frac{1 + \cos \theta}{\sin \theta}$

① $= \frac{\sin^2 \theta + (1 + \cos \theta)^2}{\sin \theta (1 + \cos \theta)}$
 ① $= \frac{\sin^2 \theta + 1 + 2 \cos \theta + \cos^2 \theta}{\sin \theta (1 + \cos \theta)}$
 $= \frac{1 + 1 + 2 \cos \theta}{\sin \theta (1 + \cos \theta)}$
 ① $= \frac{2(1 + \cos \theta)}{\sin \theta (1 + \cos \theta)}$
 $= \frac{2}{\sin \theta}$
 $= 2 \operatorname{cosec} \theta$
 $= \text{RHS}$



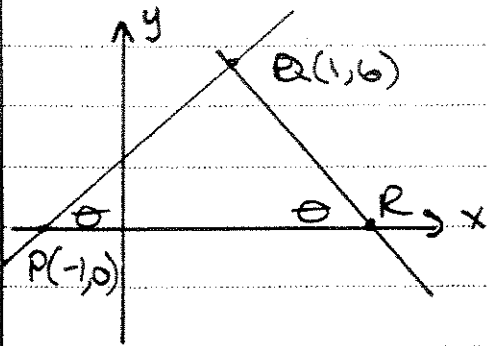
- i. $\angle DAC = 30^\circ + 40^\circ = 70^\circ$
- ii. $x^2 = 12^2 + 8^2 - 2 \times 12 \times 8 \times \cos 70^\circ$
 $x = 11.93$ km (2dp)

iii. $\frac{\sin \alpha}{8} = \frac{\sin 70^\circ}{11.93}$
 $\sin \alpha = \frac{\sin 70^\circ \times 8}{11.93}$
 $\alpha = 39^\circ$

$\therefore \text{bearing} = 150 - 39 = 111^\circ \text{T}$

① include diagram

Question 8



$$\begin{aligned} \text{a) } d &= \sqrt{(1 - (-1))^2 + (6 - 0)^2} \\ &= \sqrt{2^2 + 6^2} \\ &= \sqrt{40} \quad \text{--- ①} \\ &= 2\sqrt{10} \end{aligned}$$

$$\begin{aligned} \text{b) } m_{PQ} &= \frac{6 - 0}{1 - (-1)} \\ &= \frac{6}{2} \\ &= 3 \quad \text{①} \end{aligned}$$

$$\begin{aligned} \therefore y - 6 &= 3(x - 1) \\ y &= 3x + 3 \quad \text{①} \end{aligned}$$

$$\begin{aligned} \text{c) } \tan \theta &= m \\ \tan \theta &= 3 \\ \theta &= 72^\circ \quad \text{①} \end{aligned}$$

$$\begin{aligned} \text{d) } m_{QR} &= -3 \quad \text{① as } \angle QRP = \theta \\ \therefore y - 6 &= -3(x - 1) \\ y - 6 &= -3x + 3 \\ 3x + y - 9 &= 0 \quad \text{①} \end{aligned}$$

$$\begin{aligned} \therefore R \text{ when } y &= 0 \\ x &= 3 \\ R(3, 0) \quad \text{①} \end{aligned}$$

$$\begin{aligned} \text{e) } d_{\perp} &= \frac{|ax_1 + by_1 + c|}{\sqrt{a^2 + b^2}} > \text{either } \text{①} \\ &= \frac{|3x + y - 9|}{\sqrt{9 + 1^2}} \text{ pt } (-1, 0) \\ &= \frac{|-3 + 0 - 9|}{\sqrt{10}} \\ &= \frac{12}{\sqrt{10}} \quad \text{①} \\ &= \frac{6\sqrt{10}}{5} \end{aligned}$$