

NAME _____

TEACHER _____

Sydney Technical High School**2 Unit Mathematics****Year 11****Assessment task 2****August 2009****General Instructions**

- Each question attempted is to be started on a NEW PAGE, clearly marked with the number of the question, your name and class on the top right hand side of the page
- Working time allowed - 70 minutes
- Questions are of UNEQUAL value
- Write using black or blue pen
- APPROVED CALCULATORS may be used
- All necessary working should be shown. Marks may be deducted if working is poorly set out or difficult to read

Question 1	Question 2	Question 3	Question 4	Question 5	Question 6	Question 7	Question 8	TOTAL
/8	/8	/7	/7	/7	/8	/7	/7	/59

Question 1 (8 marks)

- a) Factorise fully : $2x^3 - x^2 + 8x - 4$ (2)
- b) Solve $-1 < 2x + 3 \leq 5$ (2)
- c) Find the domain and range of $y = \frac{1}{(2x + 3)}$ (2)
- d) Show that the points A(3,2) , B(-2,1) and C(8,3) are collinear (2)

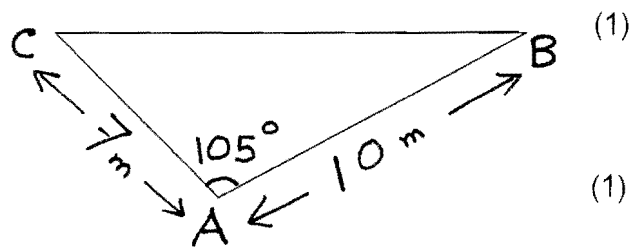
Question 2 (8 marks) (Start a new page)

- a) Use the quadratic formula to solve the equation : $4x^2 + 5x - 2 = 0$
leaving your answers in the exact form (2)
- b) Simplify $5\sqrt{3} + \sqrt{20} - 2\sqrt{12} + \sqrt{45}$ (2)
- c) Simplify $\frac{\sin^2 \theta + \cos^2 \theta}{\tan^2 \theta}$ (1)
- d) Solve $\cos \theta = -\frac{1}{\sqrt{2}}$ for $0^\circ \leq \theta \leq 360^\circ$ (2)
- e) Is $f(x) = x^3 - x$ an odd function? Explain your answer. (1)

Question 3 (7 marks) (Start a new page)

- a) The sum of the interior angles of a regular polygon is 2340° . Find the measure of each interior angle of the polygon. (1)
- b) Prove that $(1 - \tan x)^2 + (1 + \tan x)^2 = 2 \sec^2 x$ (2)

- c) (i) Find the length of BC to the nearest cm.



- (ii) Find the Area of $\triangle ABC$
(in m^2 to 2 decimal places)
- (1)

- d) Find the perpendicular distance from $(-2, 2)$ to the line $6x + 3y - 1 = 0$ in the exact form
- (2)

Question 4 (7 Marks) (Start a new page)

- a) Find 'x' if $\sin 80^\circ = \cos (90 - x)^\circ$
- (1)

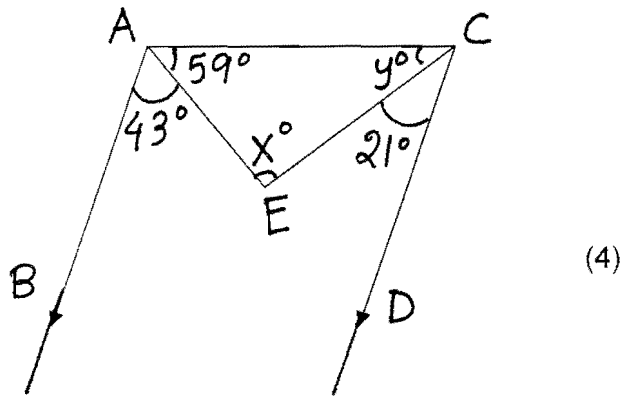
- b Draw a neat sketch of the following curve showing all relevant points

$$y = (x + 2)^2 + 2$$

(2)

- c) Evaluate 'x' and 'y' giving reasons

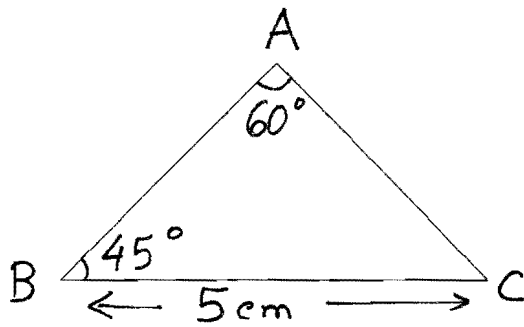
(drawing not to scale)



Question 5 (7 Marks) (Start a new page)

- a) Solve $|2x + 1| = 3x - 2$ and check solutions
- (3)

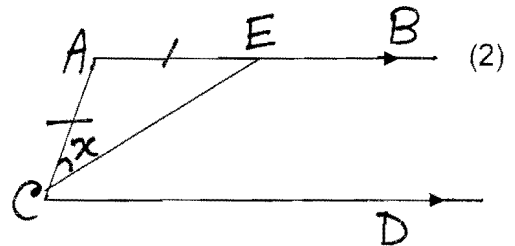
- b) Find the exact length of AC (2)



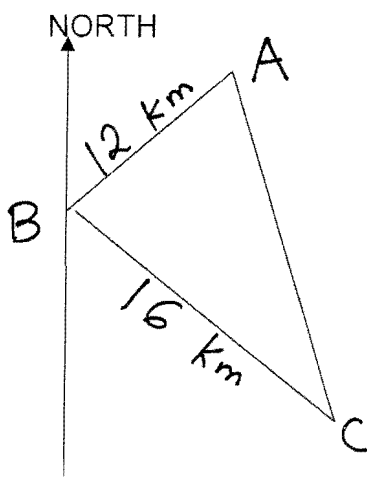
- c) Find the equation of the straight line that makes an angle of 135° with the positive x-axis and passes through the point (2,6) (2)

Question 6 (8 marks) (Start a new page)

- a) AB is parallel to CD and $AE = AC$
 Let $\angle ACE = x$
 Prove that $\angle ACE = \angle ECD$



- b) Two yachts sail in a straight line from a buoy B. Yacht A sails 12 km in the direction 038° T and yacht C sails 16 km in the direction 128° T. Copy the diagram into your books and show all the angles given.



(drawing not to scale)

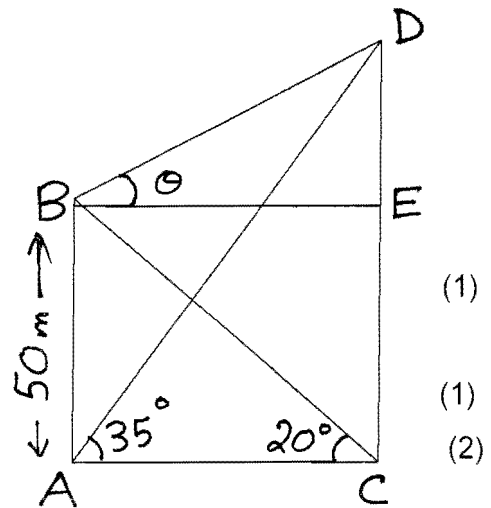
- (i) How far apart are A and C? (2)
- (ii) What is the bearing of yacht A as seen from yacht C, to the nearest minute? (2)

- c) Find the equation of the straight line passing through $(3,7)$ and parallel to the line $5x - y - 2 = 0$ (2)

Question 7 (7 Marks) (Start a new page)

- a) AB and CD are two vertical buildings with their bases A and C on level ground. The height of AB is 50m. The angle of elevation of B from C is 20° and angle of elevation of D from A is 35° . Calculate

- (i) Horizontal distance AC between the two buildings, to 1 decimal place
 (ii) The height of CD, to 1 decimal place
 (i) The angle of elevation θ of D as seen from B, to the nearest minute.



- b) Find the equation of the straight line with gradient of -2 that passes through the midpoint of the line joining $(5, -2)$ and $(-3, 4)$ (2)
- c) Find the exact value of $\cos 225^\circ$ (1)

Question 8 (7 marks) (Start a new page)

- a) If $\sin x = -\frac{3}{5}$ and $\cos x > 0$, find the values of
 (i) $\tan x$ (ii) $\sec x$ (2)
- b) Solve : $\sqrt{3} \tan \theta = 1$ for $0^\circ \leq \theta \leq 360^\circ$ (2)
- c) Prove that A $(1,5)$, B $(4, -6)$ and C $(-3, -2)$ are the vertices of a right angled triangle (3)

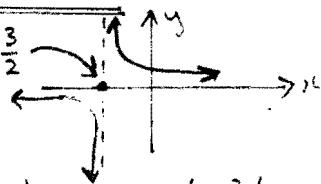
Question 1

a) $2x^3 - x^2 + 8x - 4$
 $x^2(2x-1) + 4(2x-1)$
 $= (2x-1)(x^2+4)$

b) $-1 < 2x+3$ and $2x+3 \leq 5$
 $-4 < 2x$ $2x \leq 2$
 $-2 < x$ $x \leq 1$

$\therefore -2 < x \leq 1$

c) If $2x+3=0$ $-\frac{3}{2}$
 $2x = -3$
 $x = -3/2$



\therefore Domain: all real x , $x \neq -3/2$
 Range: all real y , $y \neq 0$

d) $m_{AB} = \frac{2-1}{3-2} = \frac{1}{5}$

$m_{BC} = \frac{1-3}{-2-8} = \frac{-2}{-10} = \frac{1}{5}$

since gradient equal A, B, C collinear

e) $f(x) = x^3 - x$

$f(-x) = -x^3 + x$

$-f(-x) = x^3 - x$

$\therefore f(x) = -f(-x) \therefore$ odd fn

Question 3

a) int angle sum 2340°

$(n-2) \times 180 = 2340$

$180n - 360 = 2340$

$180n = 2700$

no angles $n = 15$

\therefore each interior angle 156°

b) LHS = $(1 - \tan^2 x)^2 + (1 + \tan^2 x)^2$
 $= 1 - 2\tan^2 x + \tan^4 x + 1 + 2\tan^2 x + \tan^4 x$
 $= 2 + 2\tan^2 x$
 $= 2(1 + \tan^2 x)$
 $= 2\sec^2 x$
 $=$ RHS

c) i)

$BC^2 = 7^2 + 10^2 - 2 \times 7 \times 10 \times \cos 105^\circ$

$BC = 13.61 \text{ m}$

\therefore OR $BC = 1361 \text{ cm}$

ii)

Area = $\frac{1}{2} \times 7 \times 10 \times \sin 105^\circ$

$= 33.81 \text{ m}^2$ (2 dec pl)

d) Given point: $(-2, 2)$

Given line: $6x + 3y - 1 = 0$

Perp. dist.

$d = \frac{|(6 \times -2) + (3 \times 2) - 1|}{\sqrt{6^2 + 3^2}}$

$= \frac{7\sqrt{5}}{15}$ units

Question 2

a) $x = \frac{-5 \pm \sqrt{25 - 4 \times 4 \times -2}}{8}$
 $= \frac{-5 \pm \sqrt{57}}{8}$

b) $5\sqrt{3} + \sqrt{20} - 2\sqrt{12} + \sqrt{45}$
 $= 5\sqrt{3} + 2\sqrt{5} - 4\sqrt{3} + 3\sqrt{5}$
 $= \sqrt{3} + 5\sqrt{5}$

c) $\frac{\sin^2 \theta + \cos^2 \theta}{\tan^2 \theta} = \frac{1}{\tan^2 \theta}$
 $= \cot^2 \theta$

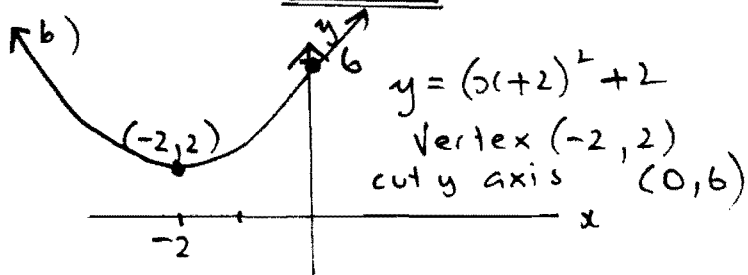
d) $\cos \theta = -\frac{1}{\sqrt{2}}$ $\frac{\sqrt{5}|A|}{\sqrt{T|C}}$

acute $\theta = 45^\circ$

$\therefore \theta = 135^\circ, 225^\circ$

Question 4

a) $\sin 80^\circ = \cos (90-x)$
 $80 + (90-x) = 90$
 $\therefore x = 80^\circ$



c)

$$43 + 59 + 21 + y = 180^\circ$$

(cointerior angles $AB \parallel CD$)
 $\therefore y = 57^\circ$

$$59 + x + 57 = 180^\circ$$

(angle sum of $\triangle AEC$)
 $x = 64^\circ$

Question 5

a) $2x+1 = 3x-2$ & $2x+1 = -(3x-2)$
 $3 = x$ $2x+1 = -3x+2$
 $5x = 1$
 $x = 1/5$

check: $|6+1| = 9-2$, $|1\frac{2}{5}| \neq -1\frac{2}{5}$

7 = 7 false
 $\therefore x = 3$ only solution

b)

$$\frac{AC}{\sin 45^\circ} = \frac{5}{\sin 60^\circ}$$

$$AC = \frac{5 \sin 45^\circ}{\sin 60^\circ}$$

$$= \left(5 \cdot \frac{1}{\sqrt{2}}\right) \div \frac{\sqrt{3}}{2}$$

$$= \frac{10}{\sqrt{6}} \text{ cm}$$

c)

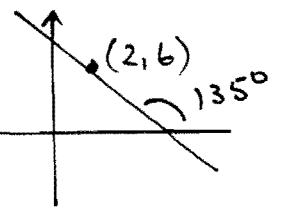
$$m = \tan 135^\circ$$

$$m = -1$$

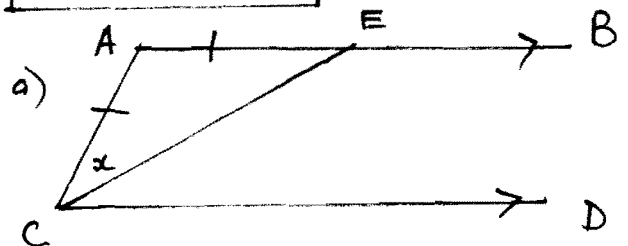
$$y - 6 = -1(x - 2)$$

$$y - 6 = -x + 2$$

$$x + y - 8 = 0$$

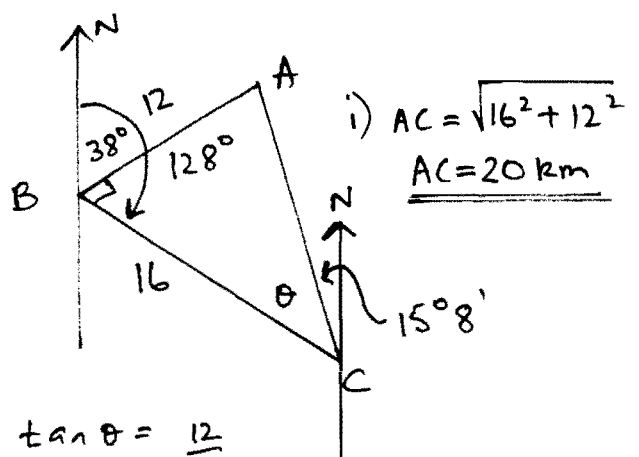


Question 6



Let $\hat{ACE} = x$
 $\therefore \hat{AEC} = x$ (base angles of isosceles triangle)
 $\hat{ECD} = x$ (alternate angles $AB \parallel CD$)
 $\therefore \hat{ACE} = \hat{ECD}$

b)



i) $AC = \sqrt{16^2 + 12^2}$
 $AC = 20 \text{ km}$

ii) $\tan \theta = \frac{12}{16}$
 $\therefore \theta = 36^\circ 52'$
 $\therefore \text{Bearing } 344^\circ 52'$

$$\begin{aligned}
 \text{c) } 5x - y - 2 &= 0 \\
 y &= 5x - 2 \quad m = 5 \quad (3, 7) \\
 y - 7 &= 5(x - 3) \\
 y - 7 &= 5x - 15 \\
 \underline{\underline{0 &= 5x - y - 8}}
 \end{aligned}$$

Question 7

$$\text{a) } \tan 20^\circ = \frac{SO}{AC}$$

$$\text{i) } AC = \frac{SO}{\tan 20}$$

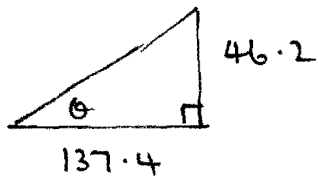
$$AC = 137.4 \text{ m}$$

$$\text{ii) } \tan 35^\circ = \frac{CD}{137.4}$$

$$CD = 137.4 \cdot \tan 35$$

$$\underline{\underline{CD = 96.2 \text{ m}}}$$

iii)



$$\tan \theta = \frac{46.2}{137.4}$$

$$\underline{\underline{\theta = 18^\circ 35'}}$$

$$\text{b) } M(1, 1) \quad m = -2$$

$$y - 1 = -2(x - 1)$$

$$y - 1 = -2x + 2$$

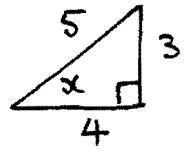
$$\underline{\underline{2x + y - 3 = 0}}$$

$$\begin{aligned}
 \text{c) } \cos 20^\circ &= \cos(180^\circ + 45^\circ) \\
 &= -\cos 45^\circ
 \end{aligned}$$

$$= -\frac{1}{\sqrt{2}}$$

Question 8

$$\begin{array}{c|c}
 S & A \checkmark \\
 \hline
 \checkmark T & C \checkmark \checkmark
 \end{array}$$



$$\text{i) } \tan x = \frac{-3}{4}$$

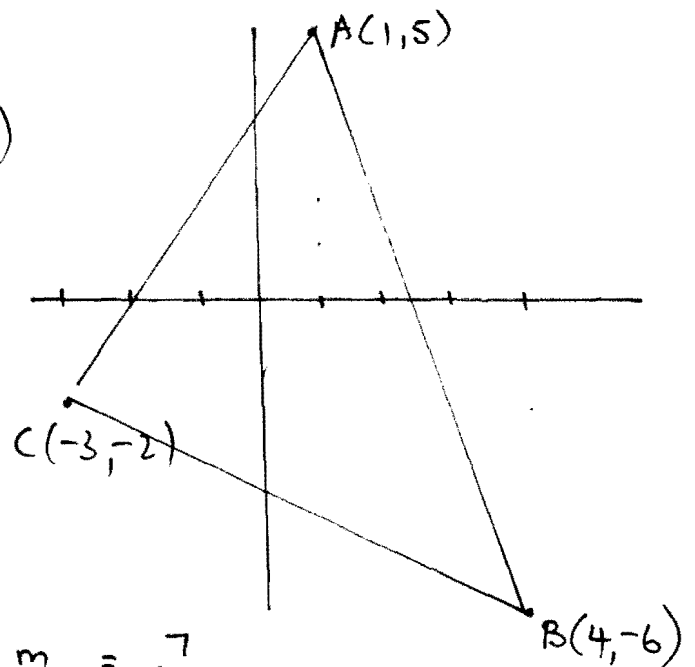
$$\underline{\underline{\text{ii) } \sec x = \frac{5}{4}}}$$

$$\begin{aligned}
 \text{b) } \sqrt{3} \tan \theta &= 1 \\
 \tan \theta &= \frac{1}{\sqrt{3}} \quad \checkmark \begin{array}{c|c} S & A \checkmark \\ \hline \checkmark T & C \end{array}
 \end{aligned}$$

$$\text{acute } \theta = 30^\circ$$

$$\therefore \underline{\underline{\theta = 30^\circ, 210^\circ}}$$

c)



$$m_{AC} = \frac{7}{4}$$

$$m_{CB} = -\frac{4}{7}$$

$$\text{Since } m_{AC} \cdot m_{CB} = -1$$

$$\therefore AC \perp CB$$

$$\hat{ACB} = 90^\circ \quad \Delta ABC \text{ is } 90^\circ \Delta$$