



# Mathematics

Total Marks – 120

### General Instructions

- Reading time – 5 minutes
- Working time – 3 hours
- Write using blue or black pen
- Attempt ALL questions.
- Begin each question on a new booklet
- Write your student number on each page
- All necessary working must be shown.
- Diagrams are not to scale.
- Board-approved calculators may be used.
- The mark allocated for each question is listed at the side of the question.

Students are advised that this is a Trial Examination only and does not necessarily reflect the content or format of the Higher School Certificate Examination.

### Question 1 – (12 marks)

Marks

- |  |   |
|--|---|
| a) If $a = 0.52$ find the value of $\frac{2+a^2}{2-a^2}$ to 3 significant figures. | 2 |
| b) Factorise $36m^2 - 9n^2$ completely.  | 2 |
| c) Convert $54^\circ$ to radians giving your answer in terms of $\pi$              | 2 |
| d) Solve $ 3x - 2  \leq 10$  | 2 |
| e) Find the primitive of $3 - e^{-2x}$   | 2 |
| f) Simplify $x(2 - y) - y(3 - x)$  | 2 |

Question 2 - (12 marks)

Marks

a) The points  $A(3, -3)$ ,  $B(-3, -4)$  and  $C(0, 3)$  are the vertices of a triangle  $ABC$ .

(i) Plot these points on the number plane. 1

(ii) Find the gradient of  $AC$ . 1

(iii) Find the angle of inclination of  $AC$  to the positive  $x$ -axis to the nearest degree. 1

(iv) Show that the equation of  $AC$  is  $2x + y - 3 = 0$ . 1

(v) Calculate the perpendicular distance of  $B$  from the side  $AC$ . 1

(vi) Hence find the area of  $\triangle ABC$   

$$\frac{|-6 -4 -3|}{\sqrt{5}} =$$
  
 ar AC  $\sqrt{25}$  2

(vii) Find the coordinates of  $D$  such that  $ABCD$  is a parallelogram. 1

b) For what values of  $p$  will  $x^2 + 5x + p$  be positive definite? 2

c) Find all the values of  $x$  between 0 and  $2\pi$  for which  $\sin x = -\frac{\sqrt{3}}{2}$  2

Question 3 - (12 marks)

Marks

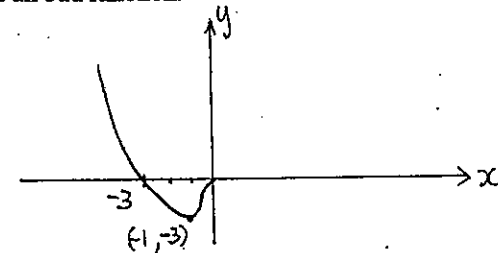
a) Differentiate

(i)  $\log_2(3x - 2)^2$  2

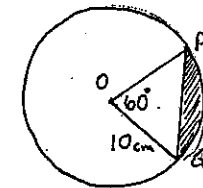
(ii)  $x^2 e^x$  2

(iii)  $\frac{1}{4x^4}$  2

b) The following diagram shows the graph of  $y = f(x)$  for  $x \leq 0$ . It is known that  $f(x)$  is an odd function.



Copy the diagram onto your answer booklet and complete the graph for  $x > 0$  2



From the diagram given of the circle centre  $O$  and radius 10cm. Find the exact value of:

(i) the length of the minor arc  $QP$ . 2

(ii) the area of the minor segment cut-off by the chord  $QP$ . 2

Question 4 - (12 marks)

Marks

a) Find:

(i)  $\int_4^9 x \sqrt{x} dx$

2

(ii)  $\int \frac{3x}{x^2+1} dx$

2

b) Differentiate

(i)  $\sin(5x + 3)$

2

(ii)  $\log_2(\cos x)$

2

(iii)  $e^x \tan 3x$

2

c) Find the value of

2

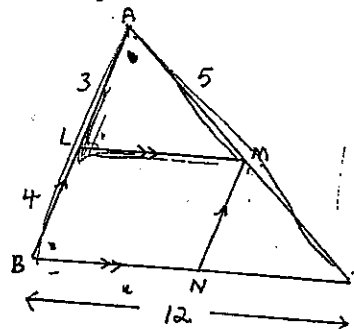
$$\sum_{n=1}^4 (3n^2 + 2)$$

Question 5 - (12 marks)

Marks

a) In the triangle  $ABC$ ,  $L$ ,  $M$  and  $N$  are on  $AB$ ,  $AC$  and  $BC$  respectively so that  $LM$  is parallel to  $BC$  and  $MN$  parallel to  $AB$

4



Find giving reasons:

(i) the length of  $MC$ .

(ii) the length of  $BN$ .

b) (i) Show that  $\frac{\sec^2 x}{\tan x} = \frac{1}{\sin x \cos x}$

2

and hence

(ii) Find the value of  $\int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \frac{1}{\sin x \cos x} dx$

3

c) (i) Copy and complete the table of values for  $y = \log_2(x + 2)$  in your booklet.

1

|     |      |      |     |     |     |
|-----|------|------|-----|-----|-----|
| $x$ | 0    | 0.5  | 1   | 1.5 | 2   |
| $y$ | 0.69 | 0.92 | 1.1 | 1.3 | 1.4 |

(ii) By using Simpson's rule with 5 function values, estimate the value of the integral  $\int_0^2 \log_2(x + 2) dx$

2

Question 6 - (12 marks)

Marks

a) The personal assistant to the CEO of Spendupbig Retail chain starts on an annual salary of \$30 000 with an annual increase of \$2 000.

(i) Show that his salary forms an arithmetic sequence and write down a formula for determining his salary after  $n$  years with the company.

2

(ii) Find his total earnings after he has worked for the company for 15 years.

2

(iii) In which year will his salary be \$42 000?

1

b) Find the value of the smallest term of the geometric series  $4 + 10 + 25 + \dots$  that is greater than  $10^{20}$ . Write your answer in scientific notation correct to 3 significant figures.

3

c) (i) Find  $\frac{d}{dx} \left( \frac{1}{2}x \sin 2x \right)$

2

(ii) Hence or otherwise find  $\int x \cos 2x \, dx$

2

Question 7 - (12 marks)

Marks

a) (i) For what values of  $x$  does this geometric series have a limiting sum?

2

$$2x + 6x^2 + 18x^3 + \dots$$

(ii) Write an expression for the limiting sum and hence find the limiting sum if  $x = \frac{1}{4}$

2

b) For the equation  $y = 2 \cos 3x$  find:

(i) the period.

1

(ii) the amplitude.

1

c) For the parabola  $y = -3 - 4x - x^2$  find:

(i) the vertex.

2

(ii) the focal length.

1

(iii) the focus.

1

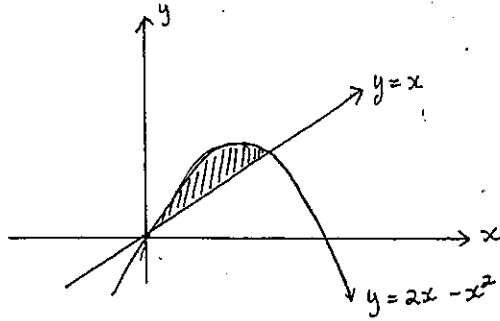
d) Sketch the region  $x^2 + y^2 > 25$

2

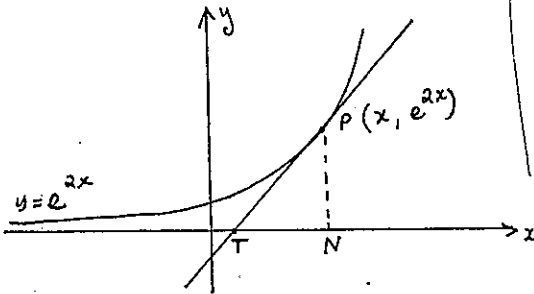
Question 9 - (12 marks)

Marks

- a) Find the volume of the solid formed when the region shaded in the diagram given is rotated around the  $x$ -axis. 4



b)



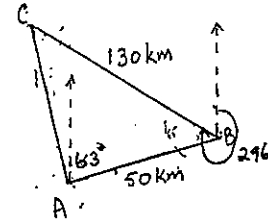
In the diagram above,  $P(x_1, e^{2x_1})$  is a variable point on the curve  $y = e^{2x}$ . The tangent at  $P$  crosses the  $x$ -axis at  $T$ . The perpendicular from  $P$  to the  $x$ -axis meets the  $x$ -axis at  $N$ .

- (i) Find the equation of the tangent to  $y = e^{2x}$  at  $P(x_1, e^{2x_1})$  2
- (ii) Find the coordinates of  $T$ . 1
- (iii) Show that for all positions of  $P$  the length of  $TN$  is constant. 2
- c) Find the solutions of  $2\sin^2\theta - \sin\theta = 0$   $0 \leq \theta \leq 2\pi$  3

Question 8 - (12 marks)

Marks

- a) A ship sails 50km from Port  $A$  to Port  $B$  on a bearing of  $063^\circ T$  then sails 130km from Port  $B$  to Port  $C$  on a bearing of  $296^\circ T$  as shown in the diagram.



- (i) Show that  $\angle ABC = 53^\circ$  2
- (ii) Find, correct to the nearest km, the distance of Port  $A$  to Port  $C$ . 2
- (iii) Find the bearing of Port  $A$  from Port  $C$ . 2

- b) The cost  $C$  (in dollars per hour) of running a boat depends on the speed  $v$  km/h of the boat according to the formula  $C = 500 + 40v + 5v^2$

- (i) Show that the total cost of the trip of 100km is 2

$$T = \frac{50000}{v} + 4000 + 500v$$

- (ii) What speed will minimise the total cost of the trip. 4

Question 10 -- (12 marks)

Marks

a) For the function  $y = x \log_e x$

(i) Write down the domain of the function.

1

$$x > 0$$

(ii) Write down the  $x$ -intercept of the function.

1

(iii) Find  $\frac{dy}{dx}$  and  $\frac{d^2y}{dx^2}$

2

(iv) Hence find any stationary points and determine their nature.

2

(v) Given that  $y \rightarrow 0^-$  as  $x \rightarrow 0^+$  sketch the curve showing all relevant features.

2

b) At the beginning of each month Jane deposits \$600 into a bank account which pays 9% p.a. calculated monthly.

(i) How much will be in her account after four years.

2

(ii) Jane needed \$50 000. How much should she have deposited each month into this account for her to have reached her goal in the four years.

2

Question 1

$$2 + (0.52)^2 = 1.31267$$

$$2 - (0.52)^2 = 1.31 \quad (3 \text{ sig. figs.})$$

$$36m^2 - 9n^2 = 9(2m-n)(2m+n)$$

$$54^\circ = 54 \times \frac{\pi}{180} \text{ radians}$$

$$= \frac{3\pi}{10}$$

$$|3x - 2| \leq 10$$

$$-10 \leq 3x - 2 \leq 10$$

$$-8 \leq 3x \leq 12$$

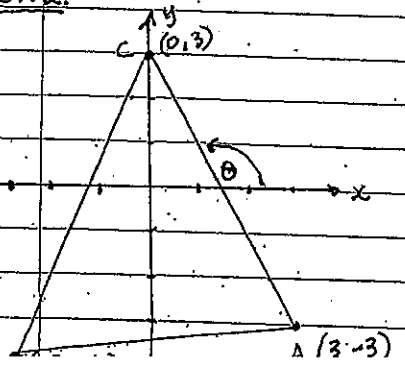
$$-\frac{8}{3} \leq x \leq 4$$

$$\int 3 - e^{-2x} dx = 3x + \frac{e^{-2x}}{2} + C$$

$$(2-y) - y(3-x) = 2x - 2xy - 3y + xy$$

$$= 2x - 3y$$

Question 2



(ii)  $m_{AC} = \frac{-3-3}{3-0} = -2$

(iii)  $\tan \theta = -2$   
 $\theta = 116^\circ 34'$   
 $\approx 117^\circ$

(iv)  $y - 3 = -2(x - 0)$   
 $y - 3 = -2x$   
 $2x + y - 3 = 0$

(v)  $d = \frac{|2x - 3 + 1x - 4 - 3|}{\sqrt{2^2 + 1^2}}$   
 $d = \frac{13}{\sqrt{5}}$

(vi)  $AC = \sqrt{(3-0)^2 + (-3-3)^2}$   
 $= \sqrt{9+36}$   
 $= \sqrt{45}$   
 $= 3\sqrt{5}$

Area =  $\frac{bh}{2}$   
 $= \frac{1 \times 3\sqrt{5} \times \frac{13}{\sqrt{5}}}{2}$   
 $= \frac{39}{2} \text{ square units}$

(vii)  $D = (6, 4)$

(i)  $b^2 - 4ac < 0, a > 0$

$x^2 + 5x + p \Rightarrow a = 1$   
 $\therefore a > 0$

$b^2 - 4ac < 0$   
 $25 - 4p < 0$   
 $4p < 25$   
 $p < \frac{25}{4}$

(2)  $\sin x = -\frac{\sqrt{3}}{2}$

related angle =  $\frac{\pi}{3}$

$x = \pi + \frac{\pi}{3}, 2\pi - \frac{\pi}{3}$   
 $= \frac{4\pi}{3}, \frac{5\pi}{3}$

Question 3

(i)  $y = \log_e(3x-2)$

$y = 2 \log_e(3x-2)$

$y' = 2 \cdot \frac{1}{3x-2} \cdot 3$   
 $= \frac{6}{3x-2}$

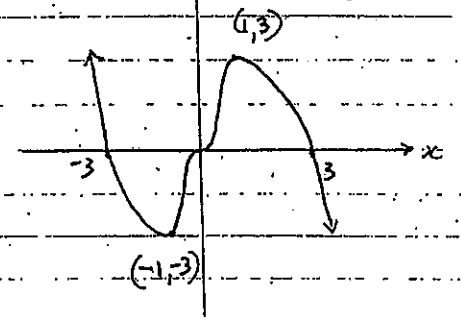
(ii)  $y = x^2 e^x$   
 $y' = 2x e^x + e^x \cdot x^2$   
 $= e^x(x^2 + 2x)$

(iii)  $y = \frac{1}{4x^4}$

$y = \frac{1}{4} x^{-4}$

$y' = -\frac{4}{4} x^{-5}$   
 $= -\frac{1}{x^5}$

(b)  $f(x)$  is odd  $\therefore$  rotational symmetry



(c) (i)  $l = r\theta$   $60^\circ = \frac{\pi}{3} \text{ radians}$

$= 10 \times \frac{\pi}{3}$   
 $= \frac{10\pi}{3}$

(ii)  $A = \frac{1}{2} r^2 (\theta - \sin \theta)$   
 $= \frac{1}{2} \times 10^2 \left( \frac{\pi}{3} - \sin \frac{\pi}{3} \right)$   
 $= 50 \left( \frac{\pi}{3} - \frac{\sqrt{3}}{2} \right)$

Question 4.

$$\begin{aligned} (1) \int_4^9 x \sqrt{x} dx &= \int_4^9 x^{\frac{3}{2}} dx \\ &= \left[ \frac{2}{5} x^{\frac{5}{2}} \right]_4^9 \\ &= \frac{2}{5} (3^5 - 2^5) \\ &= \frac{2}{5} (243 - 32) \\ &= \frac{422}{5} \\ &= 84 \frac{2}{5} \end{aligned}$$

$$\begin{aligned} \int \frac{3x}{x^2+1} dx &= \frac{3}{2} \int \frac{2x}{x^2+1} dx \\ &= \frac{3}{2} \log_e(x^2+1) + C \end{aligned}$$

$$(1) y = \sin(5x+3)$$

$$y = 5 \cos(5x+3)$$

$$(i) y = \log_e(\cos x)$$

$$\begin{aligned} y &= \frac{1}{\cos x} \cdot -\sin x \\ &= -\frac{\sin x}{\cos x} \\ &= -\tan x \end{aligned}$$

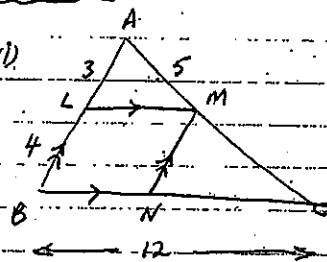
$$(iii) y = e^x \tan 3x$$

$$\begin{aligned} y' &= e^x \tan 3x + 3 \sec^2 3x \cdot e^x \\ &= e^x (\tan 3x + 3 \sec^2 3x) \end{aligned}$$

$$(c) \sum_{n=1}^4 (3n^2+2) = 5 + 14 + 29 + 50 = 98$$

Question 5.

(a) (i)



$$\begin{aligned} \frac{5}{MC} &= \frac{3}{4} \quad (\text{intercepts on } \parallel \text{ lines}) \\ MC &= \frac{20}{3} \end{aligned}$$

(ii)  $BN : NC = AM : MC$  (intercepts on  $\parallel$  lines)

$$\begin{aligned} \text{Divide 12 in the ratio } 5 : \frac{20}{3} &= 3:4 \\ \therefore \frac{3}{7} \text{ of } 12 &= 5 \frac{1}{7} \\ \therefore BN &= 5 \frac{1}{7} \end{aligned}$$

$$(b) (i) \frac{\sec^2 x}{\tan x} = \frac{1}{\sin x \cos x}$$

$$\begin{aligned} \text{LHS} &= \frac{\sec^2 x}{\tan x} \\ &= \frac{1}{\cos^2 x} \cdot \cot x \\ &= \frac{1}{\cos^2 x} \cdot \frac{\cos x}{\sin x} \\ &= \frac{1}{\sin x \cos x} \\ &= \text{RHS.} \end{aligned}$$

(ii)

$$\begin{aligned} \text{LHS} &= \frac{\sec^2 x}{\tan x} \\ &= \frac{1 + \tan^2 x}{\tan x} \\ &= \frac{1}{\tan x} + \tan x \\ &= \frac{\cos x}{\sin x} + \frac{\sin x}{\cos x} \\ &= \frac{\cos^2 x + \sin^2 x}{\sin x \cos x} \\ &= \frac{1}{\sin x \cos x} \\ &= \text{RHS.} \end{aligned}$$

$$\begin{aligned} (ii) \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \frac{1}{\sin x \cos x} dx &= \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \frac{\sec^2 x}{\tan x} dx \\ &= \log_e(\tan x) \Big|_{\frac{\pi}{6}}^{\frac{\pi}{3}} \\ &= \log_e(\tan \frac{\pi}{3}) - \log_e(\tan \frac{\pi}{6}) \\ &= \log_e \sqrt{3} - \log_e \frac{1}{\sqrt{3}} \\ &= \log_e \frac{\sqrt{3}}{\frac{1}{\sqrt{3}}} \\ &= \log_e 3 \end{aligned}$$

(c)

|   |      |        |      |        |      |
|---|------|--------|------|--------|------|
| x | 0    | 0.5    | 1    | 1.5    | 2    |
| y | ln 2 | ln 2.5 | ln 3 | ln 3.5 | ln 4 |
|   |      |        |      |        | 1.39 |

$$\begin{aligned} A \times \frac{1}{3} [ \ln 2 + \ln 4 + 4(\ln 2.5 + \ln 3.5) ] + 2 \\ &= \frac{0.5}{3} [ 12.9 ] \\ &= 2.16 \end{aligned}$$



Q6

$$A_1 = 30000 \quad A_2 = 32000 \quad A_3 = 34000$$

$$A_n = 30000 + (n-1)2000$$

$$= 28000 + 2000n$$

$$S_n = \frac{n}{2} (2a + (n-1)d)$$

$$= \frac{15}{2} (2 \times 30000 + 14 \times 2000)$$

$$= \$660000$$

$$T_n = 42000$$

$$28000 + 2000n = 42000$$

$$2000n = 14000$$

$$n = 7$$

∴ after 7 years.

$$4 + 10 + 25$$

$$= 4 \quad r = 2.5$$

$$ar^{n-1} > 10$$

$$4 \times (2.5)^{n-1} > 10$$

$$(2.5)^{n-1} > \frac{10}{4}$$

$$(n-1) \log(2.5) > \log\left(\frac{10}{4}\right)$$

$$n-1 > \frac{\log\left(\frac{10}{4}\right)}{\log(2.5)}$$

$$n > \frac{\log\left(\frac{10}{4}\right)}{\log(2.5)} + 1$$

$$n > 49.7$$

∴ the 50th term.

$$T_n = ar^{n-1}$$

$$T_{50} = 4 \times (2.5)^{49}$$

$$= 1.26 \times 10^{20}$$

(c) (i) let  $y = \frac{1}{2} x \sin 2x$

$$y' = \frac{x}{2} \cdot \cos 2x \cdot 2 + \frac{1}{2} \sin 2x$$

$$= \frac{1}{2} \sin 2x + x \cos 2x$$

(ii)  $\int \frac{1}{2} \sin 2x + x \cos 2x \, dx = \frac{1}{2} x \sin 2x$

$$\int \frac{1}{2} \sin 2x \, dx + \int x \cos 2x \, dx = \frac{1}{2} x \sin 2x$$

$$\int x \cos 2x \, dx = \frac{1}{2} x \sin 2x - \int \frac{1}{2} \sin 2x \, dx$$

$$\int x \cos 2x \, dx = \frac{1}{2} x \sin 2x - \frac{1}{2} \cdot \frac{-\cos 2x}{2} + c$$

$$= \frac{1}{2} x \sin 2x + \frac{1}{4} \cos 2x + c$$

Question 7

(a) (i)  $2x + 6x^2 + 18x^3 + \dots$

$$r = 3x \quad |r| < 1$$

$$-1 < 3x < 1$$

$$-\frac{1}{3} < x < \frac{1}{3}$$

(ii)  $x = \frac{1}{4}$

$$S_{\infty} = \frac{\frac{1}{4}}{1 - \frac{3}{4}}$$

$$= 2$$

b) (i) period =  $\frac{2\pi}{3}$

(ii) amplitude = 2

2)  $y = -3 - 4x - x^2$

$$x^2 + 4x = -y - 3$$

$$x^2 + 4x + 4 = -y - 3 + 4$$

$$(x+2)^2 = -y + 1$$

$$(x+2)^2 = -(y-1)$$

i) vertex  $(-2, 1)$

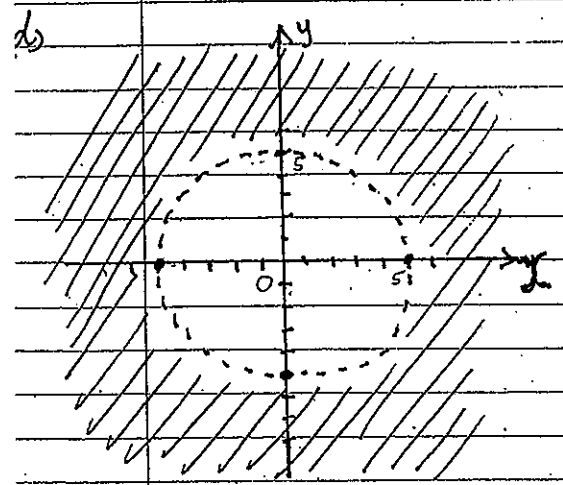
ii)  $x^2 = 4ay$

$$4a = -1$$

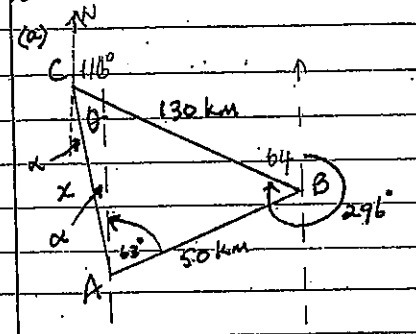
$$a = -\frac{1}{4}$$

∴ focal length =  $\frac{1}{4}$

iii) focus =  $(-2, \frac{3}{4})$



Question 8



(i) Using alternate angles on || lines

$$\angle ABC = 116 - 63$$

$$= 53^\circ$$

(ii)  $x^2 = 50^2 + 130^2 - 2 \times 50 \times 130 \times \cos 53^\circ$

$$x^2 = 11576.4$$

$$x = 107.59$$

$$= 108 \text{ km (nearest km)}$$

(iii)  $\frac{\sin \theta}{50} = \frac{\sin 53}{108}$  ( $\theta < 53^\circ$ )

$$\sin \theta = \frac{\sin 53}{108} \times 50$$

$$\theta = \sin^{-1}\left(\frac{\sin 53}{108} \times 50\right)$$

$$= 21.6^\circ$$

$$\approx 22^\circ$$

$\angle NCB = 116^\circ$

∴ bearing =  $116^\circ + 22^\circ$

$$= 138^\circ$$

∴ bearing of A from C =  $138^\circ$

$$\text{time taken} = \frac{100}{v}$$

$$\text{total cost} = \text{cost/h} \times \text{time}$$

$$T = C \times \frac{100}{v}$$

$$= (500 + 40v + 5v^2) \times \frac{100}{v}$$

$$T = \frac{50000}{v} + 4000 + 500v$$

$$\frac{dT}{dv} = ?$$

$$= 50000v^{-2} + 4000 + 500v$$

$$= -\frac{50000}{v^2} + 500$$

$$= -\frac{50000}{v^2} + 500$$

$\approx 0$  for max or min

$$0 = -\frac{50000}{v^2} + 500$$

$$\frac{50000}{v^2} = 500$$

$$50000 = 500v^2$$

$$100 = v^2$$

$$\pm 10 = v$$

$$= \frac{100000}{v^3}$$

$\approx 10$   $T'' > 0 \therefore$  min.

minimum cost when speed = 10 km/h.

### Question 9.

(a)  $y = x$   
 $y = 2x - x^2$

$$x = 2x - x^2$$

$$x^2 - x = 0$$

$$x(x-1) = 0$$

$$x = 0, 1$$

$$\text{Vol} = \pi \int_0^1 (2x - x^2)^2 - x^2 dx$$

$$= \pi \int_0^1 (4x^2 - 4x^3 + x^4 - x^2) dx$$

$$= \pi \int_0^1 (3x^2 - 4x^3 + x^4) dx$$

$$= \pi \left[ \frac{3x^3}{3} - \frac{4x^4}{4} + \frac{x^5}{5} \right]_0^1$$

$$= \pi \left[ x^3 - x^4 + \frac{x^5}{5} \right]_0^1$$

$$= \pi \left[ (1 - 1 + \frac{1}{5}) - 0 \right]$$

$$= \frac{\pi}{5} \text{ cubic units.}$$

(b) (i)  $y' = 2e^{2x_1}$   $P(x_1, e^{2x_1})$

$$\therefore m = 2e^{2x_1}$$

$$y - y_1 = m(x - x_1)$$

$$y - e^{2x_1} = 2e^{2x_1}(x - x_1)$$

(ii) let  $y = 0$

$$\therefore -e^{2x_1} = 2e^{2x_1}(x - x_1)$$

$$-\frac{1}{2} = (x - x_1)$$

$$x = x_1 - \frac{1}{2}$$

$$T = (x_1 - \frac{1}{2}, 0)$$

$$T = (x_1 - \frac{1}{2}, 0)$$

$$TN = x_1 - (x_1 - \frac{1}{2}) = \frac{1}{2}$$

TN is independent of  $x_1$   
 $\therefore$  TN is a constant.

i.e.  $TN = \frac{1}{2}$  for all  $x_1$

(c)  $2\sin^2\theta - \sin\theta = 0$

$$\sin\theta(2\sin\theta - 1) = 0$$

$$\sin\theta = 0 \quad 2\sin\theta - 1 = 0$$

$$\theta = 0, \pi, 2\pi \quad \sin\theta = \frac{1}{2}$$

$$\theta = \frac{\pi}{6}, \frac{5\pi}{6}$$

$$\therefore \theta = 0, \pi, 2\pi, \frac{\pi}{6}, \frac{5\pi}{6}$$

### Question 10.

(a)  $y = x \log_e x$

(i) domain  $x > 0$

(ii) x-int.  $y = 0$

$$x \log_e x = 0$$

$$\log_e x = 0$$

$$x = e^0 = 1$$

$$\therefore (1, 0)$$

(iii)  $y = x \log x$

$$\frac{dy}{dx} = 1 \cdot \log x + x \cdot \frac{1}{x}$$

$$= \log x + 1$$

$$\frac{d^2y}{dx^2} = \frac{1}{x}$$

(iv)  $y' = 0$  for stationary pts.

$$\log x + 1 = 0$$

$$\log x = -1$$

$$x = e^{-1}$$

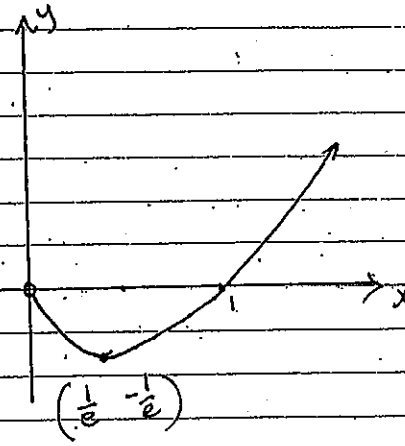
$$x = \frac{1}{e}$$

$$y'' = \frac{1}{x}$$

$$= \frac{1}{\frac{1}{e}}$$

$$= e > 0 \therefore \text{min.}$$

$$\left(\frac{1}{e}, \frac{1}{e}\right)$$



$$\$600 \quad 9\% = \frac{9}{12}\% \text{ per month}$$
$$= 0.75\%$$

$$1 = 600(1.0075)^{48}$$

$$2 = 600(1.0075)^{47}$$

$$3 = 600(1.0075)^{46}$$

$$\dots$$
$$8 = 600(1.0075)$$

$$= 600(1.0075) \quad r = 1.0075 \quad n = 48$$

$$S = \frac{600(1.0075) \left( \frac{1.0075^{48} - 1}{1.0075 - 1} \right)}{1.0075 - 1}$$

$$= \$34771.27$$

$$50000 = \frac{x \cdot (1.0075) \left( \frac{1.0075^{48} - 1}{1.0075 - 1} \right)}{1.0075 - 1}$$

$$x = \frac{50000 \times 0.0075}{(1.0075) \left( \frac{1.0075^{48} - 1}{1.0075 - 1} \right)}$$

$$= \$862.78$$