## HORNSBY GIRLS HIGH SCHOOL



# 2011 TRIAL HIGHER SCHOOL CERTIFICATE EXAMINATION

## Mathematics Extension 1

#### **General Instructions**

- Reading Time 5 minutes
- Working Time 2 hours
- o Write using a black or blue pen
- Approved calculators may be used
- A table of standard integrals is provided at the back of this paper
- All necessary working should be shown for every question
- Begin each question in a new booklet

#### Total marks (84)

- $\circ$  Attempt Questions 1 7
- o All questions are of equal value

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#### **Total Marks**

#### **Attempt Questions 1–7**

#### All Questions are of equal value

Begin each question in a new booklet, writing your student number and question number in the boxes indicated. Extra writing booklets are available.

## Question 1 (12 marks) Use a SEPARATE writing booklet.

Marks

(a) Evaluate 
$$\lim_{x \to 0} \frac{8x}{\sin 5x}$$

1

(b) The point 
$$C(11,-5)$$
 divides the interval joining  $A(-3,2)$  and  $B$  in the ratio 7:2 internally. Find the coordinates of  $B$ .

2

(c) Solve 
$$\frac{2x+1}{x-3} < 3, x \ne 3$$

3

(d) Evaluate 
$$\int_{1}^{9} \frac{dx}{x + \sqrt{x}}$$
 using the substitution  $x = u^{2}$ .

3

(e) Find 
$$\int (\tan x - 1)^2 dx$$

3

Question 2 (12 marks) Use a SEPARATE writing booklet.

Marks

(a) Evaluate  $\int_0^{\frac{\pi}{4}} \cos^2 x \, dx.$ 

2

- (b) Consider the function  $f(x) = 2\cos^{-1}\left(\frac{x}{3}\right)$ .
  - (i) Evaluate f(0).

1

(ii) State the domain and range of y = f(x).

2

(iii) Sketch y = f(x).

1

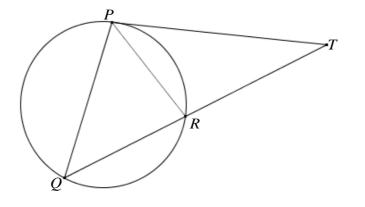
- (c) A class consists of 12 girls and 10 boys.
  - (i) A committee of 4 is to be chosen from the class. How many ways can this be done?

1

(ii) How many ways could the committee be chosen if it is to be made up of 3 girls and 2 boys?

2

(d) PT is a tangent to the circle PRQ and QR is a chord produced to intersect PT at T.



NOT TO SCALE

(i) Prove that  $\triangle PRT$  and  $\triangle QPT$  are similar.

2

(ii) Hence, prove that  $PT^2 = QT \times RT$ .

1

## **Question 3** (12 marks) Use a SEPARATE writing booklet.

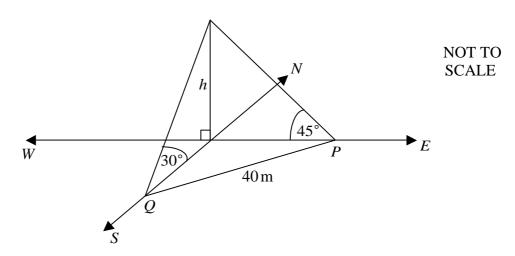
Marks

3

3

1

(a)



A vertical tower of height h metres stands on horizontal ground. From a point P, on the ground due east of the tower, the angle of elevation of the top of the tower is  $45^{\circ}$ . From a point Q, on the ground due south of the tower, the angle of elevation of the top of the tower is  $30^{\circ}$ . If the distance PQ is 40 metres, find the exact height of the tower.

- (b) A particle P is moving along the x-axis with acceleration A = -16x, where x is the displacement of the particle from the origin. Initially, the particle is at the origin, moving with a velocity of 24 units per second.
  - (i) By using integration, show that the displacement is given by  $x = 6 \sin 4t$ , where t is time in seconds.
  - (ii) State the maximum distance from the origin that the particle reaches.
  - (iii) What is the period of the motion?
  - (iv) Sketch the graph of displacement, x, against time, t, for the first  $\pi$  seconds.
  - (v) Calculate the average speed of the particle during the first  $\pi$  seconds.

Question 4 (12 marks) Use a SEPARATE writing booklet.

Marks

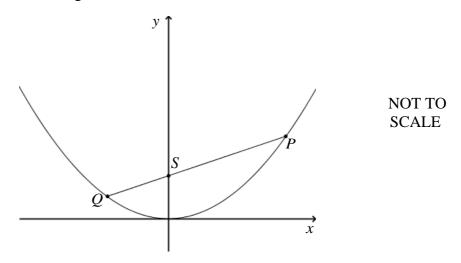
2

2

(a) (i) Given that  $x^2 + 4x + 5 \equiv (x + a)^2 + b^2$ , show that a = 2 and  $b = \pm 1$ .

(ii) Hence, find 
$$\int \frac{1}{x^2 + 4x + 5} dx$$
.

- (b) At Phillips High School in NSW there are 3 Science teachers. The probability that in a NSW a Science teacher is female is 0.6. The probability that in NSW a Science teacher (male or female) is 50 years or older is 0.2.
  - (i) What is the probability that at Phillips High School there is at least one female Science teacher?
  - (ii) What is the probability that at Phillips High School all 3 Science teachers are female and younger than 50 years.
- (c) Two points  $P(2ap, ap^2)$  and  $Q(2aq, aq^2)$  lie on the parabola  $x^2 = 4ay$ , where a > 0. The chord PO passes through the focus, S.



(i) Show that 
$$pq = -1$$
.

(ii) Show that the length of chord PQ is  $a\left(p + \frac{1}{p}\right)^2$ .

## Question 5 (12 marks) Use a SEPERATE writing booklet.

Marks

- (a) A pig farm has 100 pigs. The number of pigs, N, infected with a disease at time t days is given by  $N = \frac{100}{1 + ce^{-t}}$ , where c is a constant.
  - (i) Show that eventually all the pigs will be infected.

1

(ii) Initially, one pig is infected. After how many days will 70 pigs be infected?

3

(b) Prove by mathematical induction that  $\sum_{k=1}^{n} k \times 2^{k-1} = 1 + (n-1)2^{n}$ 

3

(c) Find the roots of the equation  $x^3 - 12x^2 + 30x + 8 = 0$ , given that they are consecutive terms in an arithmetic series.

3

(d) The population P of a country has an annual growth rate,  $\frac{dP}{dt} = 0.06P$ . How long will it take the population of this country to double? 2

## Question 6 (12 marks) Use a SEPARATE writing booklet.

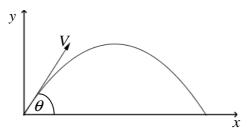
**Marks** 

2

2

(a) A particle, P, is fired from the ground at t = 0. The particle is projected from the origin at an angle of  $\theta$  to the horizontal, with a velocity of V. The horizontal equation of motion for the particle is

 $x_p = Vt\cos\theta$ . **DO NOT PROVE THIS**.

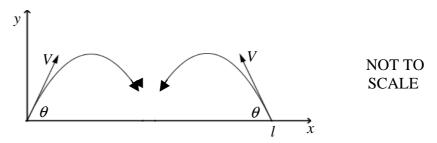


NOT TO SCALE

- (i) Prove that the vertical equation of motion for the particle is  $y_P = Vt \sin \theta \frac{1}{2} gt^2$ .
- (ii) Show that the horizontal range of the projectile,  $R_p$ , is given by

$$R_P = \frac{V^2 \sin 2\theta}{g}.$$

A second particle, Q, is fired back towards the origin from the ground at a distance of l metres to the **right** of the origin at time t = 0, with an angle of  $(180 - \theta)^{\circ}$  to the positive direction of the x-axis, with velocity V.



The equations of motion of this particle are:

$$x_Q = -Vt\cos\theta + l$$
 and  $y_Q = Vt\sin\theta - \frac{1}{2}gt^2$ . **DO NOT PROVE THESE**.

- (iii) Show that if the particles collide, it will occur when  $t = \frac{l}{2V \cos \theta}$ .
- (iv) For the particles to collide, it must occur while the particles are still in flight (ie above the ground).

Prove that, for the particles to collide in the air,  $0 < l < \frac{4v^2 \cos \theta \sin \theta}{g}$ .

Question 6 continues on page 9

### Question 6 (continued)

- (b) Consider  $f(x) = x^3 3x^2 9x$  in the domain  $x \le -1$ .
  - (i) Find the point(s) of intersection of y = x and y = f(x) in this domain 2
  - (ii) Hence, find the gradient of the inverse  $f^{-1}(x)$  at this point.

## **End of Question 6**

## Question 7 (12 marks) Use a SEPARATE writing booklet.

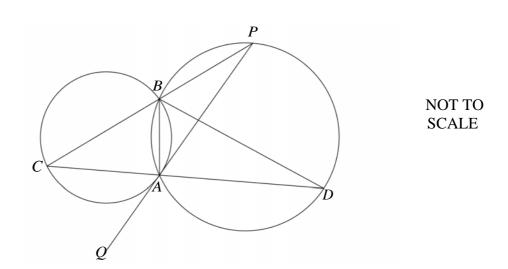
Marks

(a) It is known that  $\sin^{-1} x$ ,  $\cos^{-1} x$  and  $\sin^{-1} (1-x)$  are acute angles.

(i) Show that 
$$\sin(\sin^{-1} x - \cos^{-1} x) = 2x^2 - 1$$
.

(ii) Hence or otherwise, solve the equation  $\sin^{-1} x - \cos^{-1} x = \sin^{-1}(1-x)$ .

(b)



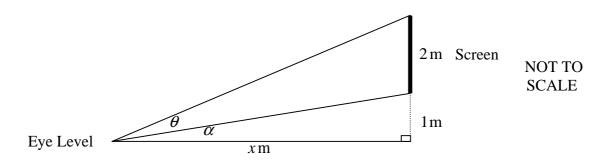
Two circles of unequal radii intersect at A and B. The tangent to the smaller circle at A cuts the larger circle at P, with PB produced cutting the smaller circle at C. The line CA produced cuts the larger circle at D.

If 
$$\angle CAQ = \alpha$$
 and  $\angle BAP = \beta$ , show giving reasons, that  $\angle ADB = \alpha - \beta$ .

#### **Question 7 continues on page 11**

#### Question 7 (continued)

(c) A projector screen on the front wall of a classroom is 2 metres high and its lower edge is 1 metre above the eye level of a seated student as indicated in the diagram. The horizontal distance of the student from the screen is x metres, the angle of elevation to the bottom of the screen is  $\alpha$  and the viewing angle is  $\theta$ . The "best" viewing angle is when  $\theta$  is a maximum.



(i) Show that 
$$\alpha = \tan^{-1} \left( \frac{1}{x} \right)$$
.

(ii) Show that when  $\theta$  is expressed as a function of x,

$$\theta = \tan^{-1} \left( \frac{2x}{3 + x^2} \right).$$

(iii) Hence or otherwise determine how far from the front of the room the student should sit in order to have the "best" view of the projector screen.

## **End of paper**

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Year 12 Ext 1 HGHS Solvs.	
Question 1	09
a) lini 826.	(a) $F = \int_{1}^{9} dx$ $x = u^2$
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= limi 8 .5x x=0 5 sin5x	
x->0 5 sin5x	dx= 2u.du.,
- <u>8</u>	When xel, nel
	x=9, u=3.
D) A(-3,2) B(2,4)	I= ( 3 Ru.dy .
C(1), -5) $7:2$ .	$\int_{0}^{2} \frac{1}{u^{2}+u} du$
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99= 7x-6	= 2[h(u+1)]}
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B(15,-7)	<u> </u>
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	= tax + 2 ln (cosx) + C.
$(2x+)(x+3)-3(x-3)^2<0$	
(x-3)[2x+1-3x+9] = 0	
(x-3)(10-x) < 6	
/3 10 X	
·· z>10, z=3.	

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Question 2  (a) $\int_{0}^{1/4} \cos^{2}x  dx$	(c) (i) $^{22}C_A = 7315$ - warm
Jo	(i) $i^2C_4 = 7315$ - ways. (ii) $i^2C_3 \times i^9C_2 = 9900$ ways
$=\frac{1}{2}\int_{0}^{4}(1+\omega 2x)dx$	
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$= \frac{1}{2} \left[ x + \frac{1}{2} \sin 2x \right]^{\frac{1}{2}}$	LRTP = LOT Q (compos and)
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= } ( 17+2 )	(ii) PT = RT (corresponding)  QT PT SIONS OF ARETHIS  PT = QT. RT.
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b) $f(x) = 2\cos^{-1}\left(\frac{x}{3}\right)$	ρ/ = Q/, Q/,
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(i) $f(0) = 2\omega^{-1}D$ = $2(\pi z)^{-3}$	
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Question 4	*
(a) (i) $x^2 + 4x + 4 + 1 = (2x + 2)^2 + 1$	(ii) Ope = J(200-20p)2 + (0g2-0p2)2
a=2, b'=1	
$a=\lambda, b'=1$ $b=\pm 1.$	$= \int 4\alpha^2 (q - p)^2 + \alpha^2 (q - p)^2 (q + p)^2$ $= \int 4(q - p)^2 + (q - p)^2 (q + p)^2$
$\int dx = \int dx$	$= \alpha \sqrt{4(q-p)^2 + (q-p)^2 (q+p)^2}$
$\int x^2 + 4x + 5 \int (x+2)^2 + 1$	
	= a / (9-p), [ 4 + 6 + 4 + 5 + 6 + 6 ]
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= 1-(0.4)3	= a. \(p+1)^2 \(p^2 + 2 \x p^2 + \left(1)^2\)
- 0.936	1
	$= a \sqrt{p+1/p}$
ii) P(3 (male, =50) = (0.6)3 x (0.8)3	
$\stackrel{=}{=} 0.11 (2d\rho)$	$= a(p+1)^2$
	C P
:	
e) (i) Chad PQ:	
y-ap = ag, 2-ap2	
-x-2ap 2ag-2ap	
S(0,G) satisfies equation	
$\frac{\Delta - ap^2 = \alpha(q, p)(q, p)}{-2\alpha p} = \frac{\alpha(q, p)(q, p)}{2\alpha(q/-p)}$	
1-p2 = 9+p -Zp 2	
1-p2=-pq-p2	
195	,
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QUESTION 5	
a) i) lim e-t = 0	c) let roots be a-d, a a+d
	sum 100ts = a-d+a+a+d = 12
! Lim 100 = 100 top 1+ce-t = 1+0	a=4
F 100	prod voots = (4-d)(4+d) +4 = -8
ii) when t=0 N=1	16-d= = -2
: 1 = 100 1+4	$d^{2} = 18$
C=99	$d = 3J\Sigma$
when N=70	: 100ts are 4, 42352
70 = 100 1+99e-t	
	d) $dP = 0.06P$
$e^{-t} = \frac{1}{231}$	
t = In (231)	:. A=Re0.06E
= 5.44	when 2P = P e o . abt
	2 = e 0.06t
6) /x2°+ 2x2'+3x72+ +Ax	2A-1-1+G-112 +=12
b) 1x2°+ 2x2'+ 3x2++ 1x.	$2^{A-1} = 1 + (A-1) \cdot 2^{-1}$ $E = 1 \cdot 1 \cdot 2^{-1}$ $0.06$
. Place let 401 HEL	$2^{n-1} = 1 + (n-1) \cdot 2^n$ $E = 1 \cdot 2$ $0.06$
L.H.S. = (x 2° = 1	$2^{A-1} = 1 + (A-1) \cdot 2^{A-1} = 1 + (A-1) \cdot 2^{A-1} = 0.06$
L.H.S. = 1 x 2° = 1 R.H.S. = 1 + 0 = 1	$2^{n-1} = 1 + (n-1) \cdot 2^{n-1}$ $= 1 + (n-1) \cdot 2^{n-1}$ $= 0.06$
L.H.S. = 1 x 2° = 1  R.HS = 1+0 = 1  True for M=1	$2^{n-1} = 1 + (n-1) \cdot 2^{n-1}$ $= 1 \cdot 2^{n-1}$ $= 0.06$
L.H.S. = 1 × 2° = 1  R.HS = 1+0 = 1  True for M=1  . Assume true for A= R+1	$2^{n-1} = 1 + (n-1) \cdot 2^n$ $= 1 \cdot 2^n$ $= 1 \cdot 2^n$ $= 0.06$
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L.H.S. = 1 × 2° = 1  R.H.S = 1+0 = 1  True for M=1  Assume true for A= k+1  1è. 1×2° + 2×2'×3×2° + × 1×2  Prove true for 1= k+1  i.e. 1×2°+2×2'+ + k×2 <sup>k-1</sup> i.e. 1×2°+2×2'+ + k×2 <sup>k-1</sup>	$2^{k-1} = (+(q-1), 2^{k}) = 1 + (k-1)$ $4^{k-1} = 1 + (k-1)$ $(k+1) = 2^{k} = 1 + k \cdot 2^{k+1}$
L.H.S. = 1 × 2° = 1  R.HS = 1 + 0 = 1  True for M = 1  . Assume true for A = R + 1  1è. 1× 2° + 2× 2′ × 3× 2° + × 1× 2°  . Prove True for 1 = R + 1  i.e. 1× 2° + 2× 2′ + + k× 2 <sup>k-1</sup> L.H.S. = 1 + (k-1). 2 <sup>k</sup> + (k+1)	$2^{h-l} = (+(q-l), 2^{h}) = \lim_{k \to \infty} \frac{1}{0.06}$ $A^{-l} = (+(k-l), 2^{h})$ $(k+l) = 2^{h} = (1+k, 2^{h+1})$ $(k+l) = 2^{h}$
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L.H.S. = 1 × 2° = 1  R.HS = 1 + 0 = 1  True for M = 1  . Assume true for A = k + 1  1è. 1×2° + 2×2' × 3×2° + × 1×2'  . Prove frue for 1 = k + 1  i.e. 1×2° + 2×2' + + k×2 <sup>k-1</sup> i.e. 1×2° + 2×2' + + k×2 <sup>k-1</sup> L.H.S. = 1 + (k-1). 2 <sup>k</sup> + (k+1)  = 1 + R.2 <sup>k</sup> - 2 <sup>k</sup> + k.2 <sup>k</sup> +  = 1 + 2k.2 <sup>k</sup>	$2^{h-l} = (+(q-l), 2^{h}) = \lim_{k \to \infty} \frac{1}{0.06}$ $A^{-l} = (+(k-l), 2^{h})$ $(k+l) = 2^{h} = (1+k, 2^{h+1})$ $(k+l) = 2^{h}$
L.H.S. = 1 × 2° = 1  R.HS = 1+0 = 1  True for M=1  Assume true for A= k+1  1è. 1×2° + 2×2'×3×2° +×1×2  Prove true for 1=k+1  i.e. 1×2°+2×2'++k×2 <sup>k-1</sup> +  i.e. 1×2°+2×2'++k×2 <sup>k-1</sup> +  1.H.S. = 1+(k-1).2 <sup>k</sup> +(k+1)  = 1+k.2 <sup>k</sup> -2 <sup>k</sup> +k.2 <sup>k</sup> +  = 1+2k.2 <sup>k</sup> = 1+k.2 <sup>k</sup> +1	$2^{h-l} = (+(q-l), 2^{h}) = \lim_{k \to \infty} \frac{1}{0.06}$ $A^{-l} = (+(k-l), 2^{h})$ $(k+l) = 2^{h} = (1+k, 2^{h+1})$ $(k+l) = 2^{h}$
L.H.S. = 1 × 2° = 1  R.HS = 1+0 = 1  True for M=1  Assume true for A= k+1  1è. 1×2° + 2×2'×3×2° + + 0×2  Prove True for 1= k+1  i.e. 1×2°+2×2'++ k×2 <sup>k-1</sup> i.e. 1×2°+2×2'++ k×2 <sup>k-1</sup> 1.H.S. = 1+(k-1). 2 <sup>k</sup> + (k+1)  = 1+k.2 <sup>k</sup> -2 <sup>k</sup> +k.2 <sup>k</sup> +  = 1+2k.2 <sup>k</sup> = 1+k.2 <sup>k</sup> = R.H.S	$2^{h-l} = (+(q-l), 2^{h}) = \lim_{k \to \infty} \frac{1}{0.06}$ $A^{-l} = (+(k-l), 2^{h})$ $(k+l) = 2^{h} = (1+k, 2^{h+1})$ $(k+l) = 2^{h}$
L.H.S. = 1 × 2° = 1  R.H.S = 1+0 = 1  True for M=1  . Assume true for A=k+1  1è. 1×2°+ 2×2'×3×2°+	$2^{h-l} = (+(q-l), 2^{h}) = \lim_{k \to \infty} \frac{1}{0.06}$ $A^{-l} = (+(k-l), 2^{h})$ $(k+l) = 2^{h} = (1+k, 2^{h+1})$ $(k+l) = 2^{h}$
L.H.S. = 1 × 2° = 1  R.H.S = 1+0 = 1  True for M=1  Assume true for A= R+1  1è. 1×2° + 2×2' × 3×2° + × 1×2  Prove True for 1= R+1  i.e. 1×2°+2×2' + + k×2 <sup>k-1</sup> L.H.S. = 1+(k-1).2 <sup>k</sup> + (k+1)  = 1+ k.2 <sup>k</sup> - 2 <sup>k</sup> + k.2 <sup>k</sup> +  = 1+ k.2 <sup>k</sup> = 1+ k.2 <sup>k</sup> = R.H.S	$2^{h-l} = (+(q-l), 2^{h}) = \lim_{k \to \infty} \frac{1}{0.06}$ $A^{-l} = 1 + (k-l)$ $(k+l) = 2^{h} = 1 + k \cdot 2^{k+l}$ $2^{k}$

Question 6	
a) (i) ÿp=-9	(iv) [ There are a few netbods
	time of flight is 231
when to VI	3
when to VI	Need colloui the to be les
VSIO D=C	this.
yp = -9t+1/sin0	$\frac{o < \ell}{2\sqrt{\cos\theta}} < \frac{2\sqrt{\sin\theta}}{9}$
yp = -gt + v+sin0 +d	21/10/0. 19
<u> </u>	Z <sub>1</sub> V <sub>W</sub> OO
uhen t=0, y=0	n = 0 < 41/2018.
d= 0	$0 < \ell < 4V^2 sin \theta c$
-: yp = -gt + Vtsino	<u> </u>
- Annual Control of the Control of t	[ lo, since listor
is het yp=0	of origin ]
$0 = -gt^2 + V + yhO$	
0= -t(gt-Vsin0)	(b) $f(x) = x^3 - 3x^2 - 9x$
gt=Vsin@ (t=70)	het a= x2-3x2-9x
02 ,	$0 = x^3 - 3x^2 - 10x$
t= 2Vsino	0= x(x2-3xc-10)
<i>g</i> ·	0= x(x-5)(x+2)
Sub into oc	: x=0, x=-2, x=
$z = V/2V \sin \theta$ ) coole	But 315-1
( 9 /	:. Pt of intersection is
= 2V2 villeanle	
= 2V251100000	(i) $f'(x) = 35x^2 - 65x - 9$
= V28102Q	$f'(-2) = 3(-2)^2 - 6(-2)$
	= /5
	: f'(x) how gractiont
ii) Pord Q house some y-values	at this point.
at time to Need 20 = xp	
cet some time-	
l-Vtcora = Vtcora	
l = 2V+c00	
t = l 24000 -	

07a) let sù'x=x 1/8x	$\frac{\partial 111}{\partial x} = \frac{1}{1 + \left(\frac{2x}{3+x^2}\right)^{-2}} \frac{2(3+x^2) - 2x \cdot 2x}{(3+x^2)^{\frac{1}{2}}}$
05-1x-B & D	$+\left(\frac{3+\lambda_{2}}{2\kappa}\right)$ $\left(3+\lambda_{z}\right)$
J 1-x2	$= 0$ when $6 + 2x^2 - 4x^2 = 0$
i) sin(x-β) = sin x cosβ - cosα s ι β	ie $6-2x^2=0$
$= \chi \cdot \chi - \sqrt{1-\chi^2} \cdot \sqrt{1-\chi^2}$	x = ±√3
$=\chi^2-(1-\chi^2)$	x = 53 , x > 0
$= 2x^2 - 1$	
ii) sú (sù x - cos x) = sú (sù (1-x))	
$2x^2 -   -   - x$	
$\frac{1}{2}x^{2}+x-2=0$	<u> </u>
$\alpha = -1 \pm \sqrt{1-4(2)(-2)}$	
$\therefore x = -\frac{1 \pm \sqrt{17}}{4}  (x = -\frac{1 \pm \sqrt{17}}{4}, x > 0)$	
L) < CAQ = X	
= <abc (angle="" alternate="" in="" segment)<="" td=""><td></td></abc>	
< BAP = B	
= <bca (angle="" alternate="" in="" segment)<="" td=""><td>· · · · · · · · · · · · · · · · · · ·</td></bca>	· · · · · · · · · · · · · · · · · · ·
< APB = < ADB (Angles on same arc AB)	
< ABC = < BAP + < APB (exterior < of MARP)  = < BAP + < ADB	
· · · · · · · · · · · · · · · · · · ·	
c) i) tan « = ==	
· x = + x = 1 ( \frac{1}{2} )	
ii) tan (0+x) = = = .	· · · · · · · · · · · · · · · · · · ·
1- tan 0 + tan x = 3	
tan x = x : x (+a 0 + \( \frac{1}{2} \) = 3 - \( \frac{3}{2} \) +a 0	
72 ta 0 + 3 ta 0 = 2x	
120 + 3 + 2 = 2x	
72+3 1è D = 1 -1 ( 2x )	i
ie D. L1 ( 2x )	