

#### 2014

# TRIAL HIGHER SCHOOL CERTIFICATE EXAMINATION

## **Mathematics Extension 1**

#### **General Instructions**

- Reading Time 5 Minutes
- Working time 2 hours
- Write using black or blue pen. Pencil may be used for diagrams.
- Board approved calculators maybe used.
- Marks may **NOT** be awarded for messy or badly arranged work.
- All necessary working should be shown in every question if full marks are to be awarded.
- Answer in simplest exact form unless otherwise instructed.

#### Total Marks - 70 Marks

Section I - 10 Marks

- Attempt Questions 1 10
- Allow about 15 minutes for this section

#### Section II - 60 Marks

- Attempt Questions 11 14
- Allow about 1 hour 45 minutes for this section

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R. Boros

This is an assessment task only and does not necessarily reflect the content or format of the Higher School Certificate

#### **Section I**

#### 10 marks

#### **Attempt Questions 1 – 10**

#### Allow about 15 minutes for this section

Use the multiple-choice answer sheet for Questions 1 - 10

1. If (7, b) divides (3, -4) and (9, -7) internally in the ratio a: 1, find the values of a and b.

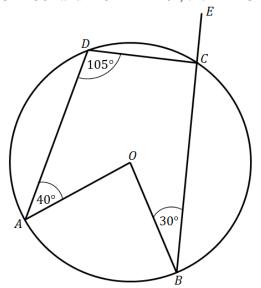
(A) 
$$a = \frac{1}{2}$$
,  $b = -\frac{23}{3}$ 

(B) 
$$a = 2$$
,  $b = -\frac{23}{3}$ 

(C) 
$$a = \frac{1}{2}$$
,  $b = -6$ 

(D) 
$$a = 2$$
,  $b = -6$ 

2. In the diagram below, O is the centre of the circle ABCD. BCE is a straight line. If  $\angle ADC = 105^{\circ}$ ,  $\angle OBC = 30^{\circ}$  and  $\angle OAD = 40^{\circ}$ , then  $\angle DCE =$ 



$$(A)75^{\circ}$$

$$(B)80^{\circ}$$

$$(C)85^{\circ}$$

$$(D)90^{\circ}$$

- **3.**  $\alpha 3\beta$  is a 3-digit number, where  $\alpha$  and  $\beta$  are integers from 1 to 9 inclusive. Find the probability that the 3-digit number is divisible by 5.
  - $(A)\frac{1}{10}$
  - $(B)\frac{9}{50}$
  - $(C)\frac{1}{9}$
  - $(D)^{\frac{1}{5}}$
- **4.** Let b > 1 and c > 1. If  $a = \log_c \sqrt{b}$ , then  $a^{-1} =$ 
  - $(A)\log_b c^2$
  - (B)  $2 \log_c b$
  - (C)  $\log_c \frac{1}{\sqrt{b}}$
  - (D)  $\log_{\frac{1}{c}} \frac{1}{\sqrt{b}}$
- 5.

$$\frac{d}{dx}(x\sin^{-1}x) =$$

- (A)  $\sin^{-1} x \frac{x}{\sqrt{1-x^2}}$
- (B)  $\sin^{-1} x + \frac{x}{\sqrt{1-x^2}}$
- (C)  $\cos^{-1} x + \frac{x}{\sqrt{1-x^2}}$
- (D)  $\cos^{-1} x \frac{x}{\sqrt{1-x^2}}$

- **6.** It is given that  $\alpha$  and  $\beta$  are roots of the equation  $x^2 + 1 = 6x$ , then  $\alpha \beta =$ 
  - $(A)-4\sqrt{2}$
  - (B)  $4\sqrt{2}$
  - (C)  $\pm 4\sqrt{2}$
  - (D)32
- 7. If  ${}^{n}P_{2} = 56$ , then
  - (A)n = -7
  - (B) n = 8
  - $(\mathbf{C})\,n=11$
  - (D) n = 112
- **8.** The minimum value of  $\frac{1}{\sin^2 x 2}$  is
  - $(A)-\frac{1}{2}$
  - (B) 1
  - $(\mathbf{C}) \frac{1}{3}$
  - (D)0

9.

$$\int \frac{1}{\sqrt{25-4x^2}} dx =$$

- $(A)^{\frac{1}{4}}\sin^{-1}\left(\frac{5x}{2}\right) + C$
- $(B)^{\frac{1}{4}}\sin^{-1}\left(\frac{2x}{5}\right) + C$
- $(C)\frac{1}{2}\sin^{-1}\left(\frac{5x}{2}\right) + C$
- $(D)^{\frac{1}{2}}\sin^{-1}\left(\frac{2x}{5}\right) + C$

10. The coefficient of  $x^{2n}$  in the binomial expansion of  $(1+x)^{4n}$  is

- $(\mathsf{A})\frac{4n!}{2n!2n!}$
- (B)  $\frac{(4n)!}{2(n!)^2}$
- $(C)\frac{(4n)!}{(2n)!}$
- (D) None of the above

**End of Section A** 

#### **Section II**

#### 60 marks

#### **Attempt Questions 11 – 14**

#### Allow about 1 hour and 45 minutes for this section

Answer each question in a NEW writing booklet. Extra pages are available

In Questions 11 - 14, your responses should include relevant mathematical reasoning and/or calculations.

#### **Question 11** (15 marks) Start a NEW Writing Booklet

- (a) Determine the acute angle, between the line x 3y + 2 = 0 and the line BC where B is (-1, -1) and C is (1, 3).
- (b) Evaluate  $\lim_{x \to 0} \frac{3x}{2 \sin 4x}$
- (c) Solve for x,  $\frac{(x-2)}{(x-1)(x-3)} \ge 0$
- (d) Write down a general solution to the equation  $\cos 2x = -\frac{1}{2}$ . Leave your answer in terms of  $\pi$ .

(e) (i) Express  $12 \cos x - 5 \sin x$  in the form  $A \cos(x + \alpha)$  where A is positive and  $0^{\circ} \le \alpha \le 180^{\circ}$ , correct  $\alpha$  to the nearest minute.

- (ii) Hence find the maximum value of  $12 \cos x 5 \sin x$  and the smallest positive value of x for which this maximum occurs.
- (f) Calculate the number of different arrangements which can be made using all the letters of the word BANANA.

#### **Question 11 continues on page 7**

- (g)
  - (i) Differentiate  $\cot x$  with respect to x.
- 1

1

(ii) Hence differentiate  $x \cot x$  with respect to x.

(iii) Hence find

1

 $\int x \csc^2 x \cdot dx$ 

**End of Question 11** 

#### **Question 12** (15 Marks) Start a NEW Writing Booklet

(a) Express  $\sin 2\theta$  and  $\cos 2\theta$  in terms of  $t = \tan \theta$  to show that

$$\frac{1 + \sin 2\theta - \cos 2\theta}{1 + \sin 2\theta + \cos 2\theta} = \tan \theta$$

- (b) In the expansion of  $(1 + 2x)^n (1 x)^2$ , the coefficient of  $x^2$  is 9. Find the coefficient of x in the expansion.
- (c) If the roots of  $x^3 6x^2 + 3x + k = 0$  are consecutive terms of an arithmetic series, find k.
- (d) Evaluate  $\int_{0}^{\frac{3}{4}} x \sqrt{1-x} \, dx$

using the substitution u = 1 - x, express your answer in simplest exact form.

(e)
(i) Prove by the Principle of Mathematical Induction that

3

$$1 \times 2^{1} + 2 \times 2^{2} + 3 \times 2^{3} + \dots + n \times 2^{n} = (n-1) \times 2^{n+1} + 2$$

for all positive integers n.

(ii) Using the result of (i), simplify 2

$$\sum_{r=1}^{n} (r+1) \times 2^{r}$$

(f) Brian is to celebrate his 16<sup>th</sup> birthday by having a dinner with 11 other family members. At this dinner, Brian will sit at the head of a non-circular table. In how many ways can everyone be seated?

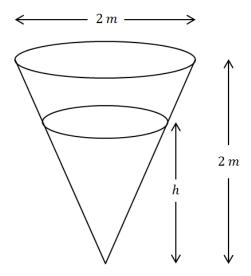
#### **End of Question 12**

#### **Question 13** (15 Marks) Start a NEW Writing Booklet

- (a) A particle moves up and down so that its vertical displacement, x from a point O, is given by  $x = 10 + 8 \sin 2t + 6 \cos 2t$  where x is in metres and t is in seconds.
  - (i) Show that the particle moves in Simple Harmonic motion.
  - (ii) What is the period of the motion?

1

- (iii) What is the amplitude?
- (b) A container in the shape of a right cone with both height and diameter 2 m is being filled with water at a rate of  $\pi$   $m^3/min$ .



(i) Show that 2

$$\frac{dV}{dt} = \frac{\pi h^2}{4} \cdot \frac{dh}{dt}$$

(ii) Find the rate of change of height h of the water when the container is  $\frac{1}{8}th$  full by volume.

#### Question 13 continues on page 10

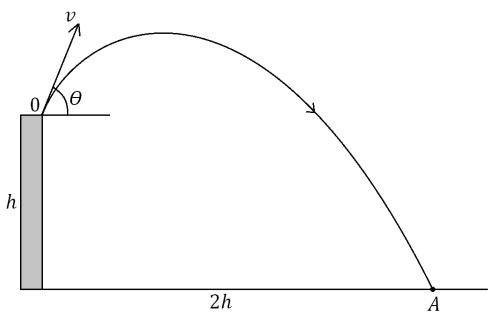
(c) The rate of change in the number of members of the Sydney Boys High School Old Boys Mathematical Society, *M*, is given by

$$\frac{dM}{dt} = k(M - 50)$$

The number of members of this society at the start of 1995 was 70.

- (i) Show that  $M = 20e^{kt} + 50$  satisfies the differential equation above. 1
- (ii) In 2000, the number of members was 150. Find the number of members in 2005.
- (iii) There is a year that this society will eventually become a "ghost society" with no members. Do you agree? Give reasons.

(d)



A projectile is fired with speed  $\sqrt{\frac{4gh}{3}}$  at an angle  $\theta$  to the horizontal from the top of a cliff of height h and the projectile strikes the ground a horizontal distance 2h from the base of the cliff.

You may assume  $y = Vt \sin \theta - \frac{1}{2}gt^2$  and  $x = Vt \cos \theta$ .

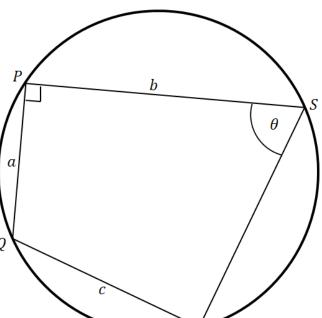
(i) Show that  $y = x \tan \theta - \frac{gx^2}{2V^2} (1 + \tan^2 \theta)$ .

2

(ii) Find the 2 possible values of  $\tan \theta$ .

#### Question 13 continues on page 11

(e) In the diagram below, PQRS is a cyclic quadrilateral,  $\angle QPS = 90^{\circ}$  and  $\angle PSR = \theta$ , PQ = a, PS = b and QR = c.



2

Show that  $(a^2 + b^2) \sin^2 \theta = a^2 + c^2 + 2ac \cos \theta$ .

**End of Question 13** 

#### **Question 14** (15 Marks) Start a NEW Writing Booklet

- (a) At an election, 30% of the voters favoured party A. If 5 voters were selected at random, what is the probability (as a decimal) that
  - (i) exactly 3 favoured party A.

1

(ii) at most 2 favoured party A.

1

(b)

(i) Show that

3

$$\tan 3x = \frac{3\tan x - \tan^3 x}{1 - 3\tan^2 x}$$

(ii) If x satisfies the equation  $\tan 3x = \cot 2x$ , show that x also satisfies the equation  $5 \tan^4 x - 10 \tan^2 x + 1 = 0$ .

2

(iii) Using the result of (ii), deduce that

4

$$\tan\frac{\pi}{5} = \sqrt{5 - 2\sqrt{5}}$$

(c) In the expansion of  $(1+x)^n$ , let  $S_1$  be the terms containing the coefficients  ${}^nC_0$ ,  ${}^nC_2$ ,  ${}^nC_4$ , ... whilst  $S_2$  be the terms containing the coefficients

 ${}^{n}C_{1}$ ,  ${}^{n}C_{3}$ ,  ${}^{n}C_{5}$ , ...

Prove that,

(i)  $4S_1S_2 = (1+x)^{2n} - (1-x)^{2n}$ 

2

(ii) 
$$(S_1)^2 - (S_2)^2 = (1 - x^2)^n$$

2

#### End of paper

#### STANDARD INTEGRALS

$$\int x^{n} dx = \frac{1}{n+1} x^{n+1}, \ n \neq -1; \ x \neq 0, \text{if } n < 0$$

$$\int \frac{1}{x} dx = \ln x, \ x > 0$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax}, \ a \neq 0$$

$$\int \cos ax dx = \frac{1}{a} \sin ax, \ a \neq 0$$

$$\int \sin ax dx = -\frac{1}{a} \cos ax, \ a \neq 0$$

$$\int \sec^{2} ax dx = \frac{1}{a} \tan ax,$$

$$\int \sec ax \tan ax dx = \frac{1}{a} \sec ax, \ a \neq 0$$

$$\int \frac{1}{a^{2} + x^{2}} dx = \frac{1}{a} \tan^{-1} \frac{x}{a}, \ a \neq 0$$

$$\int \frac{1}{\sqrt{a^{2} - x^{2}}} dx = \sin^{-1} \frac{x}{a}, \ a > 0, \ -a < x < a$$

$$\int \frac{1}{\sqrt{x^{2} - a^{2}}} dx = \ln \left( x + \sqrt{x^{2} - a^{2}} \right), \ x > a > 0$$

$$\int \frac{1}{\sqrt{x^{2} + a^{2}}} dx = \ln \left( x + \sqrt{x^{2} + a^{2}} \right)$$

$$\text{NOTE: } \ln x = \log_{e} x, \ x > 0$$

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Student Number:

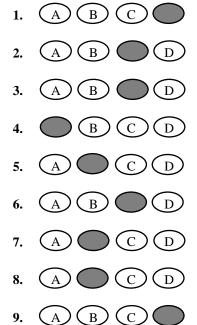
### **SOLUTIONS**

## Mathematics Extension 1 Trial HSC 2014

Sample:	2 + 4 =	(A) 2	(B) 6	(C) 8 C (	(D) 9	
*	•	le a mistake, pu	it a cross throu	gh the incorrec	t answer and fill in the	
new answer.		A leftharpoonup	В	$c \bigcirc$	$D \bigcirc$	
	50 INO		1.7	nd drawing an a	the correct answer, then	1
		A 💓		C $\bigcirc$	D 🔾	

#### **Section I:** Multiple choice answer sheet.

Completely colour the cell representing your answer. Use black pen.



10. (A) (B) (C) (

Guestian 11 B(-1, -1) C(1,3)d.  $\cos 2x = -1/2$ SA  $M_{i} = \frac{3+1}{1+1}$ cose = 12 a= 713  $2x = \frac{2x}{3} + \frac{2kx}{3}, \frac{4x}{3} + 2kx$  $\alpha - 3y + 2 = 0$ 3y = 3C + 2 $y = \frac{1}{3}3C + \frac{2}{3}$  $\Delta = \frac{\pi}{3} + 2k\pi, \quad \frac{2\pi}{3} + k\pi$ ·. M2= 1/3 eilzcosx-ssinx = Acos(x+x) tanx = 2-1/3 1+2. <= 45° =Acosacosa - Asinasina  $12 = A \cos \alpha , 5 = A \sin \alpha$   $\cos \alpha = 12 , \sin \alpha = 5$  A A Ab  $\lim_{\infty} 3x$ 270 asin4x = lim 4, 3a 270 4 2504c  $\frac{1}{2}$   $\frac{1}{3}$   $\frac{42}{3042}$  $+a_{1} \propto = 5/12$   $\propto = 22^{37}$ C x-2 > 0 11 12000x - 5 sin x = 13 Cos(x+  $\alpha \neq 1,3$ Max value = 13 consider occurs when Cos(x+2)37) y = (x-2)(x-1)(x-3) $\cos(x + 22^{2}37') = 1$ x+2237' = 360 x=337'23' 14242, 2473- 1/2 for neg angle (5.89)

 $f. Banana = \frac{6!}{2!3!} = 60 \text{ }$  $\frac{g \cdot 1}{dx} = \frac{1}{tanx} dx \qquad u = 1 \quad u' = 0$   $\frac{1}{dx} = \frac{1}{tanx} dx \qquad v' = sec^2x$  $\frac{d(\alpha \cot a) d\alpha}{d\alpha} = \frac{\alpha \times (-\cos e c^{3} \alpha) + \cot \alpha}{d\alpha}$ = cotx - orcosec3x  $\int a \csc^2 x \, dx = -\int -x \csc^2 x \, dx$  $= -\int (\cot x - 2\cos x - \cot x) dx$  $= -\int (\cot x - \alpha \csc x - \cos x) dx$  $= - \left[ x \cot x - \ln(\sin x) \right] + C$ = In(sinou) - x (otal +c- 1)

12)a) 
$$t = tan 0$$

$$HS = \frac{1 + sin 20 - cos 20}{1 + sin 10 + cos 20}$$

$$= \frac{1 + \frac{2t}{1 + t^2} - \frac{1 - t^2}{1 + t^2}}{1 + t^2} + \frac{1 - t^2}{1 + t^2}$$

$$= \frac{1 + \frac{2t}{1 + t^2} + \frac{1 - t^2}{1 + t^2}}{1 + t^2} \times \frac{1 + t^2}{1 + t^2}$$

$$= \frac{1 + t^2 + 2t - 1 + t^2}{1 + t^2}$$

$$= \frac{2t^2 + 2t}{2t + 2t}$$

$$= \frac{2t^2 + 2t}{2t}$$

$$=$$

$${}^{4}C_{o}(-2) + {}^{4}C_{o}(2) = -2 + 8$$

$$= 6$$

$$(\alpha-\beta)+\alpha+(\alpha+\beta)=-\frac{b}{\alpha}$$

$$3\alpha = -\frac{(-6)}{1}$$

Since x is a root 
$$P(2) = 0$$
  
 $(2)^3 - 6(2)^2 + 3(2) + k = 0$ 

$$\frac{d}{\int_{0}^{3/4} x \sqrt{1-x} dx}$$

$$x=3/4, u=\frac{1}{4}$$

$$= \int_{1}^{4} (1-u) \sqrt{u} - du$$

$$= \int_{1}^{1} \left( u^{\frac{1}{2}} - u^{\frac{3}{2}} \right) du$$

$$= \begin{bmatrix} \frac{2}{3} u^{\frac{3}{2}} - \frac{2}{5} u^{\frac{5}{2}} \end{bmatrix} \pm \begin{bmatrix} \frac{3}{2} u^{\frac{5}{2}} - \frac{$$

$$= \frac{2}{3} \left(1\right)^{\frac{3}{2}} - \frac{2}{5} \left(1\right)^{\frac{5}{2}} - \left(\frac{2}{3} \left(\frac{1}{4}\right)^{\frac{3}{2}} - \frac{2}{5} \left(\frac{1}{4}\right)^{\frac{5}{2}}\right)$$

$$= \frac{47}{246}$$

$$= n \times 2^{n+1} + 1 - 1$$

$$= n \times 2^{n+1}$$

OR
$$= (r+1)2^{r} = \sum_{r=1}^{n} r \times 2^{r} + \sum_{r=1}^{n} e^{n} + \sum$$

#### **Question 13**

- (a)  $x = 10 + 8\sin 2t + 6\cos 2t$ 
  - (i)  $\dot{x} = 16\cos 2t 12\sin 2t$  $\ddot{x} = -32\sin 2t 24\cos 2t$  $\ddot{x} = -4(8\sin 2t + 6\cos 2t)$  $\therefore \ddot{x} = -4(x-10)$ Now let X = x-10

 $\therefore \ddot{X} = -4X$  and thus the motion is SHM.

- (ii) Clearly n = 2.  $\therefore T = \frac{2\pi}{2}$   $= \pi$
- (iii) Amplitude  $a = \sqrt{8^2 + 6^2}$  = 10
- (b) (i)  $\frac{dV}{dt} = \frac{dV}{dh} \frac{dh}{dt}$   $V = \frac{1}{3}\pi \left(\frac{h}{2}\right)^2 h$   $= \frac{1}{12}\pi h^3$   $\frac{dV}{dh} = \frac{1}{4}\pi h^2$   $\therefore \frac{dV}{dt} = \frac{\pi h^2}{4} \frac{dh}{dt}$ 
  - (ii) Maximum Volume

$$V_{\text{max}} = \frac{1}{12}\pi(2)^3$$

One eighth full means

$$V = \frac{8\pi}{12} \div 8$$
$$= \frac{\pi}{12}$$

Thus

$$\frac{\pi}{12} = \frac{1}{12}\pi h^3$$

$$h = 1 \text{m}$$

We seek 
$$\frac{dh}{dt}$$
 when  $h = 1$ .

$$\frac{dh}{dt} = \frac{dh}{dV} \frac{dV}{dt}$$
$$= \frac{4}{\pi h^2} \pi$$
$$= 4 \text{ m/min}$$

(c) 
$$\frac{dM}{dt} = k(M - 50)$$

When t = 0, M = 70.

(i) Consider

$$M = 20e^{kt} + 50$$

$$\frac{dM}{dt} = 20ke^{kt}$$
$$= k(20e^{kt})$$
$$= k(M - 50)$$

: Satisfies D.E.

(ii) When t = 5, M = 150.

$$150 = 20e^{5k} + 50$$

$$100 = 20e^{5k}$$

$$5 = e^{5k}$$

$$k = \frac{\ln 5}{5}$$

$$\approx 0.3219$$

Thus when t = 10

$$M = 20e^{10k} + 50$$
$$= 550$$

(iii) No, as k > 0 membership always increases.

(d) Given 
$$y = Vt \sin \theta - \frac{1}{2}gt^2$$
 and  $x = Vt \cos \theta$ 

(i) 
$$t = \frac{x}{V \cos \theta}$$
, substitute to obtain

$$y = \frac{x \sin \theta}{\cos \theta} - \frac{1}{2} g \left( \frac{x^2}{V^2 \cos^2 \theta} \right)$$
$$y = x \tan \theta - \frac{gx^2}{2V^2} \left( 1 + \tan^2 \theta \right) \text{ as required.}$$

(ii) The point A is (2h,-h). Substitute:

$$-h = 2h \tan \theta - \frac{g(2h)^2}{2V^2} \left( 1 + \tan^2 \theta \right)$$

But 
$$V^2 = \frac{4gh}{3}$$

$$-h = 2h\tan\theta - \frac{3h}{2}\left(1 + \tan^2\theta\right)$$

Thus  $3\tan^2\theta - 4\tan\theta + 1 = 0$ 

So 
$$\tan \theta = 1 \text{ or } \frac{1}{3}$$

(e) Required to prove  $(a^2 + b^2)\sin^2\theta = a^2 + c^2 + 2ac\cos\theta$ 

Join *PR*, *QS*. *QS* is the diameter, so  $\angle QPR = 90^{\circ}$  (angle in a semicircle).

In 
$$\triangle PQS$$
  $QS^2 = a^2 + b^2$  (Pythagoras's Thm)  
 $\sin \angle PQS = \frac{b}{QS}$   
 $\therefore QS = \frac{b}{\sin \angle PQS}$ 

In quad PQRS  $\angle PQR = 180^{\circ} - \theta$  (opposite angles of cyclic quadrilateral)  $\angle PRS = \angle PQS$  (angles in same segment)

In  $\Delta PQR$ 

$$PR^{2} = a^{2} + c^{2} - 2ac\cos(180^{0} - \theta)$$
$$= a^{2} + c^{2} + 2ac\cos\theta$$

In  $\Delta PRS$ 

$$\frac{PR}{\sin \theta} = \frac{b}{\sin \angle PRS}$$

$$= \frac{b}{\sin \angle PQS}$$

$$= QS \qquad \text{from above}$$

$$PR = QS \sin \theta$$

$$PR^2 = QS^2 \sin^2 \theta$$

$$= a^2 + c^2 + 2ac \cos \theta$$
Thus  $(a^2 + b^2) \sin^2 \theta = a^2 + c^2 + 2ac \cos \theta$  QED

## QUESTION 14 (XI)

(a) (1) 
$$P(x=3) = {5 \choose 3} (0.3)^{3} (0.7)^{2}$$

$$= \frac{1}{2} \cdot 0.1323.$$

(11) 
$$P(x=0) + P(x=1) + P(x=2)$$
  
 $= (5) (0.3)^{0} (0.7)^{5} + (5) (0.3)^{1} (0.7)^{4} + (5) (0.3)^{3} (0.7)^{3}$   
 $| = 0.8369 \lambda |$ 

$$\frac{ton 3x = ton (2x+2)}{= ton 2x + ton x}$$

$$\frac{1 - ton 2x \cdot ton x}{1 - t^{2}}$$

$$\frac{2t}{1 - t^{2}} + t$$

$$\frac{1 - 2t}{1 - t^{2}} \cdot t$$

$$= \frac{3t+t(1-t^{2})}{1-t^{2}-2t^{2}}$$

$$= \frac{3t-t^{3}}{1-3t^{2}}$$

$$= 3\tan z - \tan^{3} z$$

OR. ton3x = utax.

("Y(OMTD) A. 
$$\frac{3t-1^3}{1-3t^2} = \frac{1-t^4}{3t}$$

$$2+(3t-t^3) = (i-3t^4)(i-t^4)$$

$$1+t^4-3t+5 = (i-t^4-3t^4+3t^4)$$

$$5t+-10t^4+1 = 0. \quad \text{(III)}$$

$$2=\frac{1}{10} \text{ is also a selection to (A)}$$

$$11 \quad t^2 = \frac{10 \pm \sqrt{100-30}}{10}$$

$$= \frac{10 \pm 4\sqrt{5}}{5}$$

$$12 \quad tan = \pm \sqrt{\frac{5\pm 3\sqrt{5}}{5}}$$

$$13 \quad tan = \pm \sqrt{\frac{5\pm 3\sqrt{5}}{5}}$$

$$14 \quad tan = \pm \sqrt{\frac{5\pm 3\sqrt{5}}{5}}$$

$$15 \quad tan = \sqrt{\frac{5\pm 3\sqrt{5}}{5}}$$

$$16 \quad tan = \sqrt{\frac{5\pm 3\sqrt{5}}{5}}$$

$$17 \quad tan = \sqrt{\frac{5\pm 3\sqrt{5}}{5}}$$

$$18 \quad tan = \sqrt{\frac{5\pm 3\sqrt{5}}{5}}$$

$$19 \quad tan = \sqrt{\frac{5\pm 3\sqrt{5}}{5}}$$

$$19 \quad tan = \sqrt{\frac{5\pm 3\sqrt{5}}{5}}$$

1- 5 ± 255

(") CONTD.

$$= \frac{2\sqrt{5t^2\sqrt{5}}}{5}$$

$$= \frac{1}{4}\sqrt{5t^2\sqrt{5}}$$

$$= \frac{1}{4}\sqrt{5t^2\sqrt{5}}$$

$$= \sqrt{5t^2\sqrt{5}}$$

$$= \sqrt{5t^2\sqrt{5}}$$

$$= \sqrt{5t^2\sqrt{5}}$$

$$= \sqrt{5t^2\sqrt{5}}$$
(clearly  $tan II > 0$ )
$$= \sqrt{5t^2\sqrt{5}}$$

$$= \sqrt{5t^2\sqrt{5}}$$
Also
$$= \sqrt{5t^2\sqrt{5}}$$

$$tan II < tan II <$$

which is >1.

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