Name:



2014

Mathematics Extension 2 Trial HSC Exam

General Instructions

- Reading time 5 minutes
- Working time 3 hours
- Write using black or blue pen. Black pen is preferred
- Board-approved calculators may be used
- A table of standard integrals is provided at the back of this paper
- In Questions 11-16, show relevant mathematical reasoning and/or calculations

Total marks – 100

Section I pages 2 – 5

10 marks

- Attempt Questions 1-10
- Allow about 15 minutes for this section

Section II pages 6 – 16

90 marks

- Attempt Questions 11 16
- Allow about 2 hours and 45 minutes for this section

Section I

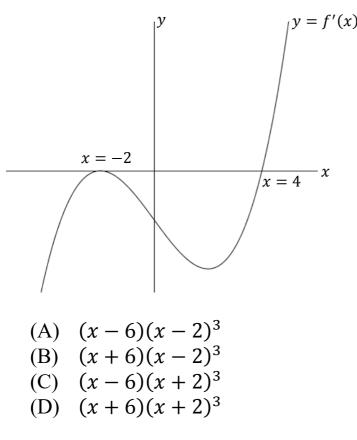
10 marks Attempt Questions 1-10 Allow about 15 minutes for this section

Use the multiple-choice answer sheet for Questions 1-10.

1 Which of the following is equivalent to

 $\int x \sec^2(x^2) \, dx$

- (A) $2\tan(x^2) + C$ (B) $\frac{1}{2}\tan(x^2) + C$ (C) $\frac{1}{3}\tan(x^2) + C$ (D) $3\tan(x^2) + C$
- 2 From the graph of y = f'(x) drawn, which could be the equation of y = f(x)



3 The $\sqrt{-3+4i}$ is

 $\begin{array}{ll} (A) & 2+i \\ (B) & 1+2i \\ (C) & 2-i \\ (D) & 1-2i \end{array}$

4 A conic section has foci S = (3,0) and S' = (-3,0) and vertices (2,0) and (-2,0). The equation of the conic is

(A)
$$\frac{x^2}{5} + \frac{y}{4} = 1$$

(B) $\frac{x^2}{4} + \frac{y^2}{5} = 1$
(C) $\frac{x^2}{4} - \frac{y^2}{5} = 1$
(D) $\frac{x^2}{5} - \frac{y^2}{4} = 1$

5 For the function $g(x) = \tan^{-1}(e^x)$ the range is

(A)
$$0 \le y \le \frac{\pi}{2}$$

(B) $0 \le y < \frac{\pi}{2}$
(C) $0 < y \le \frac{\pi}{2}$
(D) $0 < y < \frac{\pi}{2}$

⁶ If $e^x + e^y = 1$, which of the following is an expression for $\frac{dy}{dx}$?

(A)
$$-e^{x-y}$$

(B) e^{x-y}
(C) e^{y-x}
(D) $-e^{y-x}$

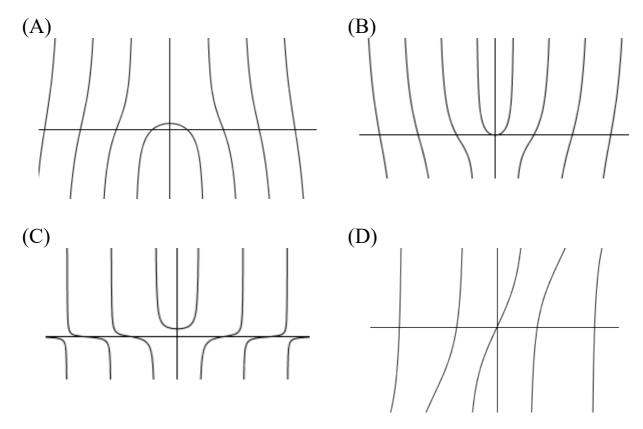
7 The polynomial $P(x) = x^4 + ax^2 + bx + 28$ has a double root at x = 2.

What are the values of *a* and *b*?

- (A) a = -11 and b = -12
- (B) a = -5 and b = -12
- (C) a = -11 and b = 12
- (D) a = -5 and b = 12
- 8 If ω is a non-real sixth root of -1 and ϕ is a non-real fifth root of 1 consider the following two statements:
 - (I) $1 \omega + \omega^2 \omega^3 + \omega^4 \omega^5 = 0$

(II)
$$1 + \phi + \phi^2 + \phi^3 + \phi^4 = 0$$

- (A) Both (I) and (II) are correct
- (B) Only (I) is correct
- (C) Only (II) is correct
- (D) Neither is correct
- 9 Which of the following best represents the graph of $g(x) = x \tan x$



10 Without evaluating the integrals, which one of the following integrals is greater than zero?

(A)
$$\int_{-1}^{1} -e^{x} dx$$

(B) $\int_{-1}^{1} \frac{\sin^{-1} x}{x^{2}+1} dx$
(C) $\int_{-1}^{1} \frac{\tan^{-1} x}{\cos x} dx$
(D) $\int_{-1}^{1} e^{-x^{2}} dx$

Section II

90 marks Attempt Questions 11-16 Allow about 2 hours and 45 minutes for this section

Answer each question in a SEPARATE writing booklet. Extra writing booklets are available.

In Questions 11-16, your responses should include relevant mathematical reasoning and/or calculations.

Question 11 (15 marks) Use a SEPARATE writing booklet

- (a) For the complex numbers z = 1 + i and w = 2 3i find:
 - (i) $\bar{z} w$ 1
 - (ii) *zw* 1

2

3

(iii) Write z in modulus-argument form

(b) Show that
$$z = \sqrt{2} \ cis\left(\frac{\pi}{3}\right)$$
 is a solution of the equation $z^8 - 8z^2 = 0$

(c) Find all real roots of the polynomial $P(x) = x^4 - x^3 - 4x^2 - 2x - 12,$ given that one root is $\sqrt{2} i$.

Question 11 continues on page 7

- (d) Sketch the locus of z where the following conditions hold simultaneously $0 \le \arg(z - i) \le \frac{2\pi}{3}$ and $|z - i| \le 2$
- (e) In an Argand diagram the points *P*, *Q* and *R* represent complex numbers z_1 , z_2 and $z_2 + i(z_2 z_1)$ respectively.
 - (i) Show that PQR is a right-angled isosceles triangle 2

3

(ii) Find in terms of z_1 and z_2 the complex number represented 1 by the point S such that PQRS is a square.

Question 12 (15 marks) Use a SEPARATE writing booklet.

By completing the square find (a)

$$\int \frac{1}{\sqrt{2 - (x^2 + 4x)}} dx$$

(b) Find

$$\int \frac{\sin^3 x}{\cos^2 x} dx$$

(c) Use the substitution
$$t = \tan\left(\frac{x}{2}\right)$$
 to evaluate
$$\int_{0}^{\frac{\pi}{2}} \frac{dx}{\cos x + \sin x + 1}$$

(d) (i) Find the values of *A*, *B*, *C* and *D* such that

$$\frac{5x^3 - 3x^2 + 2x - 1}{x^4 + x^2} = \frac{A}{x} + \frac{B}{x^2} + \frac{Cx + D}{x^2 + 1}$$

(ii) Hence find
$$\int \frac{5x^3 - 3x^2 + 2x - 1}{x^4 + x^2} dx$$
 2

(e) Evaluate

$$\int_{1}^{e} \frac{\ln x}{\sqrt{x}} dx$$

2

2

4

2

Question 13 (15 marks) Use a SEPARATE writing booklet.

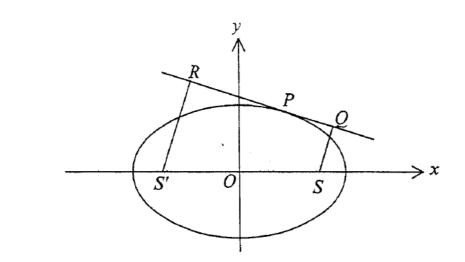
(a) (i) Use the substitution x = t - y where t is a constant to show

$$\int_0^t f(x)dx = \int_0^t f(t-x)dx$$

(ii) Hence, evaluate

(b)

$$\int_0^1 x(1-x)^{2014} dx$$



(i) Prove that the equation of the tangent to the ellipse

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$
at the point $P(a\cos\theta, b\sin\theta)$ is
 $(b\cos\theta)x + (a\sin\theta)y - ab = 0$
(ii)

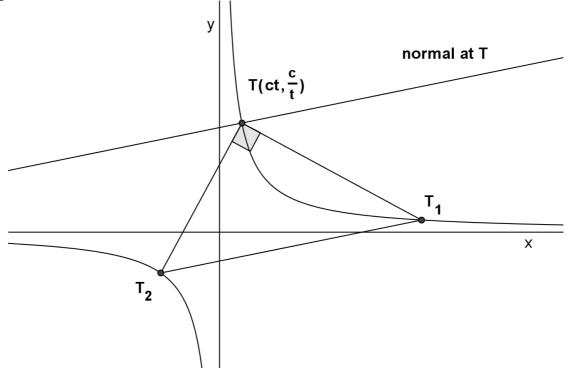
(ii) Q and R are the feet of the perpendiculars to the tangent **3** from the foci S and S' respectively Prove that $SQ \times S'R = b^2$

Question 13 continues on page 10

2

1

(c) As shown in the diagram below T_1 and T_2 are two points on the rectangular hyperbola $xy = c^2$ with parameters t_1 and t_2 respectively and T is a third point on it with parameter t such that $\angle T_1TT_2$ is a right angle



(i) Show that gradient of T_1T is $-\frac{1}{t_1t}$ and deduce that since 3 $\angle T_1TT_2$ is a right angle then $t^2 = -\frac{1}{t_1t_2}$

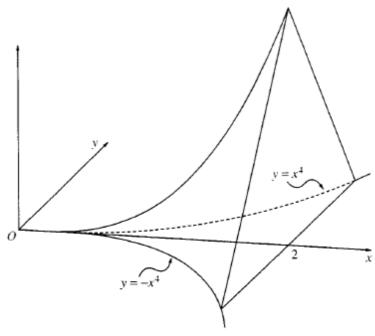
(ii)	Write down the gradient of T_1T_2	1

2

(iii) Hence, prove that T_1T_2 is parallel to the normal at T

Question 14 (15 marks) Use a SEPARATE writing booklet.

- (a) α, β and γ are the roots of the equation $x^3 - 6x^2 + 12x - 35 = 0$ Form a cubic equation whose roots are $\alpha - 2$, $\beta - 2$ and $\gamma - 2$
- (b) By taking slices perpendicular to the axis of rotation find the volume of 3 the solid generated by rotating the region bounded by the curve $y = (x - 2)^2$ and the line y = x about the x-axis
- (c) The base of a solid is the region in the xy plane enclosed by the curves $y = x^4$, $y = -x^4$ and the line x = 2. Each cross-section perpendicular to the x-axis is an equilateral triangle



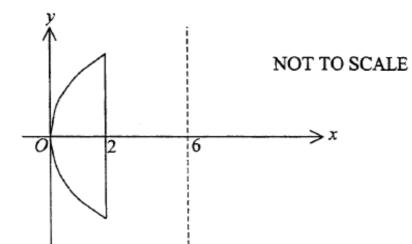
- (i) Show that the area of the triangular cross-section at x = h 2 is $\sqrt{3} h^8$
- (ii) Hence, find the volume of the solid

3

2

Question 14 continues on page 12

-11-

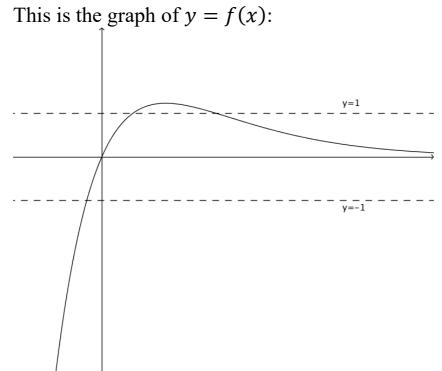


The region bounded by the parabola $y^2 = 4x$ and the line x = 2 is rotated about the line x = 6.

Using the method of cylindrical shells, find the volume of the solid formed.

Question 15 (15 marks) Use a SEPARATE writing booklet.

(a)



On the separate graph answer sheet, sketch:

(i)
$$y = (f(x))^2$$
 1

(ii)
$$y = \sqrt{f(x)}$$
 1

(iii)
$$y = \frac{1}{f(x)}$$
 1

Question 15 continues on page 14

- (b) A particle of mass m is projected vertically upwards under gravity, the air resistance to the motion being $\frac{mgv^2}{k^2}$, where the speed is v, and k is a constant
 - (i) Show that during the upward motion of the ball a

$$\ddot{x} = -\frac{g}{k^2}(k^2 + v^2)$$

2

3

where x is the upward displacement.

(ii) Hence, show that the greatest height reached is $\frac{k^2}{2g} \ln\left(1 + \frac{u^2}{k^2}\right)$

where u is the speed of projection

(c) An object is to undergo vertical motion on a bungee cord in a vacuum so that air resistance can be neglected. The only forces it experiences are gravity, mg and an elastic force, -kmx, where x is the particle's displacement from the origin. Initially, the object is at its lowest point given by x = -a. All constants are positive.

(i) Using a force diagram show that
$$\ddot{x} = -g - kx$$

(ii) By integration show that

$$v^{2} = k \left(\left(a - \frac{g}{k} \right)^{2} - \left(x + \frac{g}{k} \right)^{2} \right)$$
(iii) Show that the motion is described by 3

(iii) Show that the motion is described by

$$x = \left(\frac{g}{k} - a\right)\cos(\sqrt{k}t) - \frac{g}{k}$$

Question 16 (15 marks) Use a SEPARATE writing booklet.

(a) Let

$$I_n = \int_0^1 x^n e^{-x} dx$$

Prove that for $n \ge 1$

$$I_n = nI_{n-1} - \frac{1}{e}$$

(b) Use the binomial theorem to find the term independent of x in the expansion 3

$$\left((x+1)+x^{-1}\right)^4$$

(c) Find the cartesian equation of the locus of w where $w = \frac{z}{z+2}$ is purely 2 imaginary.

Question 16 continues on page 16

(d) (i) Use de Moivre's theorem to show that

$$\cos 3\theta = 4\cos^3 \theta - 3\cos \theta$$

(ii) Deduce that
$$8x^3 - 6x - 1 = 0$$
 has solutions $x = \cos \theta$, 2
where $\cos 3\theta = \frac{1}{2}$

(iii) Find the roots of
$$8x^3 - 6x - 1 = 0$$
 in the form $\cos \theta$ 2

(iv) Hence, evaluate
$$\cos\frac{\pi}{9}\cos\frac{2\pi}{9}\cos\frac{4\pi}{9}$$
 2

End of paper

2014 Ext 2 Trial 1) $\int 2 \sec^2(z^2) dz = \frac{1}{2} \int 2z \sec^2(z^2) dz = \frac{1}{2} \int -\frac{1}{2} \tan z^2 + C$ Ð B. €, -C, С, 2) f(x) has a double root @ ==-2 \$ so f has a triple root Since f. is increasing to right of start pt @ sc=4 f must be C **C**;~ €-C 6, 6 $\int -3 + 4i = \int 1 + 4i - 4$ 3 6-5 $= \sqrt{1 + 4i + 4i^{2}}$ = $\sqrt{(1 + 2i)^{2}}$ 6 6 C. = 1 + 2ie **E**. Must be est hyperbola. $S = (ae, c) \qquad \therefore e = \frac{3}{2}$ $b^{2} = 2^{2} \left(\left(\frac{3}{2} \right)^{2} - 1 \right)$ 4 Ð e C **C**) $\frac{2}{4} - \frac{2}{2} = 1$ **C**. G €⊇ 5 0<4<72 e e $e^{x} + e^{x} + e^{x} + e^{y} = 0$ $\frac{dy}{dy} = -\frac{e^{y}}{e^{y}}$ $= -e^{y}$ e $\left(\right)$ e e e <u>_</u> <u>_</u> P(2) = 0 = 16+49+26+28 7) 2 P(x)=4x2+2ax+b 2 ۲ P121 = 32 +4a + b = 0 6 =-12 K a = -5

ت لرم 9 \circ F . . 1- w+ w- w+w-1 doesn't work (w + even power ័ 0 Ф ٦ $(4 + \phi^3 + \phi^2 + \phi^1 + 1) = 0$ • ¢ ۳ ф 5 0 9(2 Hrow posse origin 9 5 (0) and f(3<) ہ رے د ز even always tue -20 D 3 3 , ÷ 2

Grestion II $\overline{z} - \omega = 1 - \hat{c} - (2 - 3\hat{c})$ = 1 - $\hat{c} - 2 + 3\hat{c}$ = -1 + 2 $\hat{\tau}$ a ĺ = -1 + 2i $= 2 - 3i + 2i - 3i^{2}$ = 5 - i |z| = 52 z = 5 - i z = 5 - i z = 5 - i<u>ii</u> LHS = (JZ cis(等))⁶-8(JZ cis(哥)) = 16 cis 等 - 16 cis 等 = 16 cis 等 - 16 cis 等 (= O = RHS Since one root is JZ: another is -JZ: let other two roots be d, B d+B+JZ: A-JZ: = 1 $\alpha + \beta = 1$ $\alpha + \beta = -12$ $\alpha + \beta = -6$ $\beta = -2 \quad \text{are the other root}$ _ root 3 and -3 60 Ω d (2,1)旁∽

)i) PQ = Z_2-Z_1 QR = Z_2 + i(Z_2-Z_1) - Z_2 = i(Z_2-Z_1) Since multiplication by i rotates through 90° & doesn't change modulus PQ is perpendicular to QR & equal in length - PQR is right b isosceles $Q = Z_2 - Z_1$ The parts $\frac{\overline{OS} = \overline{OP} + \overline{QR}}{= \overline{Z}_{1} + \overline{Z}_{2} - \overline{Z}_{2} + i(\overline{Z}_{2} - \overline{Z}_{1})}$ = Z_{1} + i(\overline{Z}_{2} - \overline{Z}_{1}) i.

e e ٢ C C do 6a doc 5 5 $(x^{2}+4x+4)$ 6 (x+2) 5 2C+2 6 **C**.**e**,_ C. 512 JL 1-605-いうべ dr G 6 (0) x 6sina sinx 6-6 6 6 **C**tegrals + cosx **e** _ **e**) 2dF<u>ス</u> 2 e 21-1++2+1 $|++^{2}$ e ee -+2-1 $2++1_{+}$ C, 2: 2+24 C シーデ Чe += e 2+21 *t= 0* スニロ = e e 4 - 1n2] C 2 e -6 C 5x - 3x + 2x - 1 = A x(x + 1)+ x=0 -1 = B x+D x Bzz (sć e C C, * - 22-1 Ax + e = (A+C 22 + C A=2 requating coeffs D-1 =-3* => D = -2(=3

3x-2 70 ~ 2 × $+\frac{3x}{x^2+}$ 2 D 5 $\frac{3}{2}\ln(2)$ Ĵ All C $\frac{U=}{\frac{1}{2}}$ nx Jx っメ = 2 x 2 = 2Je 2Je 2 Je =) 2 2 -4Je +4 2Je ; Э 3 4-= 3 2 5 5 Э 2 2

13 ai f(t-y)dy when z = 0f(x) dre = =0 my variable is_ Sina -x) x dx -><)2014 ĩ (1 2014 2015 DC______dx $\frac{1}{2015}$ $\frac{2016}{7}$ $\frac{1}{2015}$ $\frac{2016}{7}$ 2015 2016 4 062 240 y=b<in0 a sind = dy x do b cost -asint $y = b \sin \theta = \frac{b \cos \theta}{-\cos \sin \theta} \left(x - a \cos \theta \right)$ $y \sin \theta + a b \sin^2 \theta = b \cos \theta - a b \cos^2 \theta$ $0 = (b \cos \theta) x + (a \sin \theta) y - a b (s \sin^2 \theta + \cos^2 \theta)$ $0 = (b \cos \theta) x + (a \sin \theta) y - a b$

S=(ae,0) S = (-ae,0 abe cost - ab -abecos 0 - ab RS' =**6**\$= $\frac{ab(eusQ-1)|x|-ab(}{b^2us^2Q+a^2sin^2Q}$ $-a^2b^2(e^2us^2Q-1)|$ SQ×SR= x -ab (ecos O +1 $b^2 \cos^2\theta + a^2 \sin^2\theta$ for an ellipse $b^2 = a^2(1-b^2)$ -ab (e2 cos 0-1) $\frac{a^{2}(1-e^{2})\cos \theta + a^{2}\sin^{2}\theta}{-a^{2}b^{2}(e^{2}\cos \theta - 1)}$ $\frac{-inu}{a^2(\cos\theta + \sin\theta) - ae\cos\theta}$ $\frac{a^2(\cos\theta + \sin\theta) - ae\cos\theta}{a^2b^2(1 - e\cos\theta)}$ $\frac{a^2(1 - e^2)}{a^2(1 - e^2)}$ ct, -= 9 m T,T ct, -ct +-+' +,+Slope for TT2 = Since perpendicu = +2+ 42+ ł,

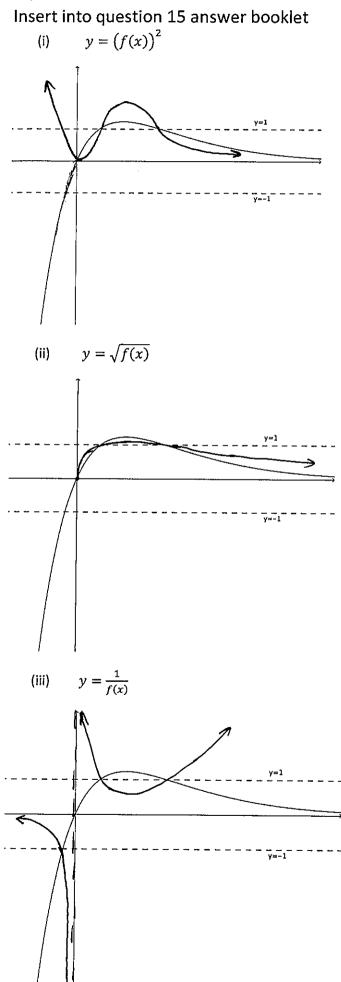
 $M_{T_1T_2} = -\frac{1}{++2}$ $y = \frac{c^2}{x}$ $\frac{dy}{dx} = -\frac{c^2}{x^2}$ $\frac{dy}{dx} = \frac{c^2}{x^2}$ $\frac{dy}{dx} = \frac{c^2}{x^2}$ $\frac{dy}{dx} = \frac{c^2}{x^2}$ ĩų $\textcircled{\label{eq:linear}{\label{e$ Normal@Thas slope += ------- ` ` ~ Fron i) +2 = - ++2 -' normal perallel to tit.

()4 0 5 α <u>56</u>+2 3 · 6 (24+2 5 12/2+2 0 2 6x + 12x+8 6x-3 -24+12x+24-35=0 \mathcal{S} 7 = 02 5 9 (x-2) <u><u>ب</u></u> 5 >< 0 2 2 x-=0 ŧ 4 4 00 X ine D = (qc <u> 41= ×</u> 9 12 Sz = TT bx 5 14 9 ふえ = 2 ÷ (2 -32 3 5 Ξ ۲ 2 7 2 · · · ·

e. E Ê; Ċ. ì (a 4 **e**; 7 ð es ena Si C) **G**) 214 6 25 6 * 142 4. 7 7 3 C, C, 13 C J314 Ĵ G 6 LB 6 53 6 6 11 8 6 6 C <u>×</u> 9 e 50 . e ۰. -53 6 2 51 **e** Q . G A 6 e ame is so C e SV = 2 Marx 2 TT (6-x) x 8x e 87 Jx -8× ~>(2 211 8 C > C 1.2 ST C **>**0 15 G C C _

 $\frac{1}{2} - \frac{3}{2} dx$ 1 2 $\sqrt{-}$ 8-6= Ø 42 طاله 5/2 8 TT) - 8 11 5 852 852 -(6) 256 JZ TT 5 5 9 5 د 9 Ŋ 7 -. -D . . 5 • \$ -. Э D . 2 **-**, 5 · . _ 5 • ŗ . -4 Э

Question 15 a Answer Sheet



Q1 \$15 6 - maj F=-ma $\frac{\sqrt{k^2}}{m^2 z = -mq\left(\frac{k^2 + v^2}{k^2}\right)}$ - MgV -may $\frac{mq}{h^{2}}\left(\frac{b^{2}}{t^{2}}\right)$ $V_{d5c}^{a} = -\frac{m_{1}}{p_{1}} \left(\frac{h^{2} + v^{2}}{h^{2} + v^{2}} \right)$ 11 $\frac{1}{2} \frac{2v}{k^2 \tau v^2} dv =$ - mg dac $\frac{1}{2} \ln \left(k^2 + v^2 \right)$ = $\frac{19}{12^2} \times +$ $\frac{V=0}{2}\left(n\left(b^{2}+u^{2}\right)=C\right)$ x=O V=U \sim max height when U=0 $\frac{1}{2} \ln \left(\frac{k^2}{k} \right) = \frac{-q}{k^2} x + \frac{1}{k^2}$ $\frac{1}{2}\ln(b^2+u^2)$ $\left(-\ln\left(k^{2}+u^{2}\right)-\ln\left(k^{2}\right)\right)$ $\frac{q}{\sqrt{2}} \times \frac{1}{2}$ $x = \frac{k}{2q} \left(\frac{k^2 + u^2}{k^2} \right)$ $= \frac{k^2}{2q} \left(\frac{k^2 + u^2}{k^2} \right)$

-ma nz -km>c kx) ii) v dv = -q - kx $\frac{1}{2}v^2 = -qxc - \frac{k}{2}x^2 + C$ $Q x = -a \quad v = 0$ (init ially skiftinovy $P = aq - \frac{a^2k}{2} + C$ $C = \frac{a^2k}{2} - aq$ k-2 + 2 -gx シン= -99 $\frac{2qx}{x} - x$ 20x $\left(\begin{array}{c}a \\ p\end{array}\right)^{2} - \left(\begin{array}{c}a^{2} \\ b^{2}\end{array}\right)^{2} + \frac{2gx}{12} + \frac{2gx}{12}$ 7 $\frac{1}{2}\left(\left(\alpha-\frac{1}{2}\right)^{2}-\left(\chi+\frac{1}{2}\right)^{2}\right)$ -リュナ、 $-\left(x+\frac{2}{R}\right)^{2}$ $\left(\alpha \right)$ $\left(\alpha - \frac{2}{12}\right)^2 - \left(x + \frac{2}{12}\right)^2$ $\cos\left(\frac{x+\frac{1}{p}}{\alpha-\frac{3}{p}}\right) = +Jk$ 4 @+=0 $\frac{\left(-a+\frac{a}{R}\right)}{\left(a-\frac{a}{R}\right)} = \frac{-1}{4}\int \frac{b}{k}xO + C$ cos-1) = C) = T cos (-1 $= \cos(\pi - Jk +$ スャ

Since $\cos(\pi + d) = \cos(\pi - d)$ we can take either without any concern. choosing the -vel $\frac{k}{2} = \cos(\pi - \sqrt{k})$ $(\pi - Jk' t)$ a Since cos(TT-d) = - cos x for all x = - cas JR7 g--a) cosi X + a) costr 3

= $x = e^{-1} - \int nx x - e^{-x} dx$ $= 1 \times -e^{-1} = (0 \times -e^{-1}) + (1 \times -e^{-1}$ $= \Lambda \int_{-1}^{1} \frac{1}{2e^{-x}} dx = \frac{1}{e}$ $= \Lambda \int_{-1}^{1} \frac{1}{e^{-x}} dx = \frac{1}{e^{-x}}$ b) $((x+1) + x^{-1})^4 = \sum_{r=0}^{4} 4(r(x+1))^r$ Using binomial theorem on (X+1)^{4-r} = k=0 k=0 $(x+1) + x^{-1})^{4} = \sum_{r=0}^{4} \frac{-r}{r} \times \sum_{k=0}^{4-r} \frac{4-r}{C_{k}} \times \sum_{k=0}^{k} \frac{1}{r} \sum_{k=0}^{$ for term independent of x x x x = x -r+k = 0 o const term is $\frac{4}{2} + \frac{4}{12} +$ let w= xny to be purely imaginary real part = 0 x=0 but 0 is not an imaginary number so locus is x = 0 except (0,0)

consider di (1)30= (ciso) $= (\cos \theta + i \sin \theta)^{3}$ = $(\cos^{3} \theta + 3i \cos^{3} \theta \sin \theta + 3i \cos^{3} \theta + i \sin^{3} \theta$ $= \cos^3 \Theta + 3 i \cos^2 \Theta \sin^2 \Theta - 3 \cos \Theta \sin^2 \Theta - i \sin^3 \Theta$ equating real parts cos30 = co30 - 3cos0 sin 0 = cos 0 - 3cos 0 (1-cos 0-= cos 0 - 3 cos 0 + 3 cos 0 = 40030 - 30050 00530=2 when $\frac{4\cos^{3}Q-3\cos Q=2}{8\cos^{3}Q-6\cos Q=1}$ 8\cos^{3}Q-6\cos Q-1=0 8x3-6x-(=0 x=c000 given by x=cos0 Alk solutions are eroots of soc-60c-1=0 are given by the colutions of 20003 iii) theroo cos30=2 30=2mn = == O = Hat taking $\wedge = O$ 07 黄 for tue ∧ ~ Q = 130 2 reed 3 roots since degree 3 polynomial 01 005 TT, 005 TT ws (0) a U racting 275 - COx T the 5 -05 - T

iv) roots are cost, cost and cost consider cos F. $\cos \frac{2\pi}{9} = \cos (\pi - \frac{2\pi}{9})$ = $\cos \frac{2\pi}{9}$ $consider cos \frac{13\pi}{9} = cos \left(-\frac{5\pi}{9}\right)$ $= cos \left(-\pi + \frac{4\pi}{9}\right)$ $= -cos \frac{4\pi}{9}$ Z are costy - costy and - costy ·. roc ć $\frac{1}{1000} \frac{1}{1000} \frac{1}{1000$ producto froots is to ~ . LOS F CO1 2 LOX 4 = 5