$\square$

## General 2 <br> Mathematics

## 2015 <br> YEAR 12 TRIAL HSC EXAMINATION

AM FRIDAY $31{ }^{\text {st }} \mathbf{J U L Y}$

## Section I - Multiple Choice

Select the alternative A, B, C or D that best answers the question. Fill in the response oval completely.
Sample
$2+4=$
(A) $2 \quad$ (B) 6
(C) 8
(D) 9
(A) $\bigcirc$
(B)
(C) $\bigcirc$
(D) $\bigcirc$

If you think you have made a mistake, put a cross through the incorrect answer and fill in the new answer.
(A)
(B)
(C) $\bigcirc$
(D) $\bigcirc$

If you change your mind and have crossed out what you consider to be the correct answer, then indicate this by writing the word correct and drawing an arrow as follows.
(A) خ
(B)
$\zeta$
(C) $\bigcirc$
(D) $\bigcirc$


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Student Number

## Mathematics General 2

2015<br>YEAR 12<br>TRIAL HSC EXAMINATION

Staff Involved:
AM FRIDAY 31 ${ }^{\text {st }}$ JULY

- PJR* •DZP*
- AXD • TE
- LAK • VAB
- JWH • AJD

Number of copies: 165

## General Instructions

- Reading time - 5 minutes
- Working time $-2 \frac{1}{2}$ hours
- Write using black or blue pen Black pen is preferred
- Board-approved calculators may be used
- A formulae and data sheet is provided at the back of this paper
- In Questions $26-30$, show relevant mathematical reasoning and/or calculations

Total marks - 100

## Section I

Page 2-10
25 marks

- Attempt Questions 1 - 25
- Allow about 35 minutes for this section

Section II
Pages 11 - 32
75 marks

- Attempt Questions 26 - 30
- Allow about 1 hours 55 minutes for this section


## Section I

## 25 marks

Attempt Questions 1 - 25

## Allow about 35 minutes for this section

Use the multiple-choice answer sheet for Questions 1-25.
Choose the best response and fill in the corresponding response oval completely.

1 What is the correlation between the variables in this scatterplot?

(A) Weak positive
(B) Weak negative
(C) Strong positive
(D) Strong negative

2 There are 24 competitors in a cycling race.
How many different selections are possible for first and second place?
Assume there are no dead heats.
(A) 47
(B) 276
(C) 552
(D) 576

3 Expand and simplify $6 x^{2}\left(x^{2}-1\right)+2 x^{2}$
(A) $6 x^{4}+2 x^{2}-1$
(B) $6 x^{4}-4 x^{2}$
(C) $6 x^{4}+8 x^{2}$
(D) $6 x^{4}+4 x^{2}$

4 The cost of a mobile phone including GST is $\$ 280$. What is the GST payable on this mobile phone?
(A) $\$ 25.45$
(B) $\$ 28$
(C) $\$ 252$
(D) $\$ 254.54$

5 The table shows the monthly repayments per $\$ 1000$ on a personal loan.

| Term of loan | $\mathbf{6 . 0 0 \%}$ | $\mathbf{6 . 2 5 \%}$ | $\mathbf{6 . 5 0 \%}$ | $\mathbf{6 . 7 5 \%}$ |
| :---: | :---: | :---: | :---: | :---: |
| 5 | $\$ 19.33$ | $\$ 19.45$ | $\$ 19.57$ | $\$ 19.68$ |
| 10 | $\$ 11.10$ | $\$ 11.23$ | $\$ 11.35$ | $\$ 11.48$ |
| 15 | $\$ 8.44$ | $\$ 8.57$ | $\$ 8.71$ | $\$ 8.85$ |
| 20 | $\$ 7.16$ | $\$ 7.31$ | $\$ 7.46$ | $\$ 7.60$ |

What is the monthly repayment for a loan of $\$ 240000$ at $6.5 \%$ p.a. interest over 20 years?
(A) $\$ 7.46$
(B) $\$ 149.20$
(C) $\$ 1790.40$
(D) $\$ 35808.00$

6 A set of 13 scores has a median of 11.
The scores $6,7,12$ and 18 are added to the data set.
Which of the following summary statistics is unaffected?
(A) interquartile range
(B) median
(C) mean
(D) standard deviation

7 What is the correct equation of the line shown below?

(A) $y=-3 x+1$
(B) $y=\frac{1}{3} x+1$
(C) $y=3 x+1$
(D) $y=-\frac{1}{3} x+1$

8 The cost $\$ C$ of a birthday party is given by $C=50 n+135$ where $n$ is the number attending the party.

If five people decide not to attend, by how much does the cost decrease?
(A) $\$ 135$
(B) $\$ 185$
(C) $\$ 250$
(D) $\$ 385$

9 A group of six students completed a test.
The mean for the group on this test was 15 .
However, one of the scores had been incorrectly recorded as a 10 instead of 20.
What is the correct mean?
(A) 13.3
(B) 14.2
(C) 16.7
(D) 18.3

10 Amelia spent the following amounts on the given food in one week.

| Groceries | $\$ 98$ |
| :--- | :---: |
| Meat and fish | $\$ 67$ |
| Milk and dairy | $\$ 53$ |
| Fruit and vegetables | $\$ 27$ |
| Other | $\$ 25$ |

Amelia would like to display the information in a sector graph.
What size angle is needed to represent fruit and vegetables?
(A) $9^{\circ}$
(B) $13^{\circ}$
(C) $27^{\circ}$
(D) $36^{\circ}$

11 A cone has a diameter of 5 cm and a height of 13 cm . What is its volume?
(A) $85 \mathrm{~cm}^{3}$
(B) $255 \mathrm{~cm}^{3}$
(C) $340 \mathrm{~cm}^{3}$
(D) $1021 \mathrm{~cm}^{3}$

12 Which of the following represents 0.5 terabytes using standard notation?
(A) $5.5 \times 10^{8} \mathrm{~B}$
(B) $5.0 \times 10^{8} \mathrm{~B}$
(C) $0.55 \times 10^{12} \mathrm{~B}$
(D) $5.5 \times 10^{11} \mathrm{~B}$

13 Which graph best represents $y=2^{x}$ ?
(A)

(B)

(C)

(D)


14 If $p=2 q^{3}-1$, what is the value of $q$ when $p$ is 13 ?
(A) $\sqrt[3]{6}$
(B) $\sqrt[3]{7}$
(C) $\frac{\sqrt[3]{14}}{2}$
(D) 4393

15 Two unbiased coins are tossed together 30 times.
Which calculation shows the expected number of times you would get two heads?
(A) $\frac{1}{2} \times 60$
(B) $\frac{1}{4} \times 60$
(C) $\frac{1}{2} \times 30$
(D) $\frac{1}{4} \times 30$

16 What is the bearing of A from C ?

(A) $075^{\circ} \mathrm{T}$
(B) $105^{\circ} \mathrm{T}$
(C) $255^{\circ} \mathrm{T}$
(D) $285^{\circ} \mathrm{T}$

17 What is the amount of interest paid on a $\$ 194000$ investment over 25 years if the interest rate charged is $6.7 \%$ p.a. compounding annually? Answer to the nearest dollar.
(A) $\$ 324950$
(B) $\$ 518950$
(C) $\$ 787550$
(D) $\$ 981550$

18 Ava and Zoe are competing in two different cycling races.
The probability that Ava wins her race is 0.8 and the probability that Zoe wins her race is 0.7 . The probability tree diagram below shows this information.


What is the probability that only one of Ava and Zoe will be successful?
(A) 0.14
(B) 0.24
(C) 0.38
(D) 0.62

19 What is the length of $A B$ ?


Not to scale
(A) 7.1 cm
(B) 7.6 cm
(C) 9.5 cm
(D) 9.8 cm

20 Millie's car uses 7.25 litres of petrol per 100 km .
How many litres of petrol will her car use on a trip of 310 km from Bulahdelah to Wollongong?
(A) 2.339 L
(B) 22.475 L
(C) 42.759 L
(D) 427.586 L

21 Riley bought a new car for $\$ 40500$. In the first year, the value of the car depreciated by $15 \%$. In the second year, the car depreciated by $10 \%$. In the third year, the value depreciated by $8 \%$. At the end of the third year, what was the percentage value of the car based on its original sale price?
(A) $33 \%$
(B) $67 \%$
(C) $70 \%$
(D) $95 \%$

22 What is the value of $x$ in the diagram below?


Not to scale
(A) $\frac{6 \sin 44^{\circ}}{\tan 34^{\circ}}$
(B) $6 \sin 44^{\circ} \sin 34^{\circ}$
(C) $\frac{6 \tan 34^{\circ}}{\sin 44^{\circ}}$
(D) $\frac{6}{\sin 34^{\circ} \sin 44^{\circ}}$

23 Which equation correctly shows $r$ as the subject of $S=500(1-r)$ ?
(A) $\quad r=\frac{S}{500}+500$
(B) $r=\frac{S-500}{500}$
(C) $\quad r=500-\frac{S}{500}$
(D) $\quad r=1-\frac{S}{500}$

24 What is the point of intersection of the lines $y=x+4$ and $y=-x-4$ ?
(A) $(-4,0)$
(B) $(-4,-8)$
(C) $(0,-4)$
(D) $(4,8)$

25 Forty Year 12 students were surveyed to find out how many hours of sport they play per week, (to the nearest hour). The results are shown in the frequency table below.

| Hours per week | Frequency |
| :---: | :---: |
| $0-2$ | 10 |
| $3-5$ | 20 |
| $6-8$ | 6 |
| $9-11$ | 4 |

What is the relative frequency of students who played more than five hours of sport?
(A) $\frac{1}{4}$
(B) $\frac{1}{2}$
(C) $\frac{3}{20}$
(D) 10

## End of Section I

$\square$
Student Number

# 2015 <br> YEAR 12 <br> TRIAL HSC <br> EXAMINATION 

## Mathematics General 2

## Section II

## 75 marks

Attempt Questions 26-30
Allow about 1 hour and 55 minutes for this section.

Answer the questions in the spaces provided.
Your responses should include relevant mathematical reasoning and / or calculations.

Extra writing space is provided on page 33. If you use this space, clearly indicate which question you are answering.

Write your Barker College assessment number at the top of each page.

## Question 26 (15 marks)

(a) What is the value of $\sqrt{\frac{m+3 n}{4 n}}$ if $m=5.9$ and $n=2.4$ ?

Answer correct to two significant figures.
$\qquad$
$\qquad$
(b) Medicine is given as a concentration of 350 mg per 100 mL .

What is the dosage rate for this medicine in $\mathrm{g} / \mathrm{mL}$ ?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(c) Find the height of the tree in the diagram below. All measurements are in metres.

$\qquad$
$\qquad$
$\qquad$
$\qquad$
(d) The magazine holder below has four sides and a base. It is open at the top.

(i) Show that the area of the shaded side is $409.5 \mathrm{~cm}^{2}$
$\qquad$
$\qquad$
$\qquad$
(ii) Calculate the surface area of the magazine holder.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(iii) The magazine holder is to be made from heavy duty cardboard. The cost of this type of cardboard is $\$ 4.29$ per square metre. What is the cost of making fifty of these magazine holders (to nearest cent)?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Question 26 (continued)
(e) The table below shows the present value of a $\$ 1$ annuity.

| Present value of \$1 annuity |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Period | $1 \%$ | $2 \%$ | $4 \%$ | $6 \%$ | $8 \%$ |  |
| 1 | 0.9901 | 0.9804 | 0.9615 | 0.9434 | 0.9259 |  |
| 2 | 1.9704 | 1.9416 | 1.8861 | 1.8334 | 1.7833 |  |
| 3 | 2.9410 | 2.8839 | 2.7751 | 2.6730 | 2.5771 |  |
| 4 | 3.9020 | 3.8077 | 3.6299 | 3.4651 | 3.3121 |  |
| 5 | 4.8534 | 4.7135 | 4.4518 | 4.2124 | 3.9927 |  |

(i) What would be the present value of a $\$ 9000$ per year annuity at $6 \%$ per annum for 5 years, with interest compounding annually?
$\qquad$
$\qquad$
$\qquad$
(ii) An annuity of $\$ 6000$ every three months is invested at $4 \%$ per annum, compounded quarterly for 1 year. What is the present value of this annuity?
$\qquad$
$\qquad$
$\qquad$
(iii) What is the regular payment that would provide a present value of \$43 230 over 3 years at $8 \%$ per annum compound interest? Answer to the nearest dollar.
$\qquad$
$\qquad$
$\qquad$


Student Number
Question 26 (continued)
(f) Tim weighs 75 kg and has bought a six-pack of an alcoholic beverage to drink at a party. 3 If each drink in this six-pack is one standard drink, what is the minimum length of time over which he must consume all six drinks in order to have a blood alcohol content (BAC) reading of less than 0.05 at the end of the party? (Answer to the nearest 10 minutes)
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## End of Question 26

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(a) James recorded the times for 160 music downloads, grouped them into classes and then displayed this information using the cumulative frequency histogram shown below.

Time taken for download

(i) Using the graph above, estimate the median
(ii) Use the graph to estimate the interquartile range
$\qquad$
$\qquad$
$\qquad$
(iii) James said "There were about 10 downloads that took exactly 30 seconds" Is he correct? Give a reason for your answer.
$\qquad$
$\qquad$
$\qquad$

Question 27 (continued)
(b) A table of home loan repayments for a $\$ 390000$ loan is shown below.

| Amount borrowed |  |  | $\$ 390000$ | Monthly repayment $(R)=\$ 2100$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Annual interest rate $(r)$ | $6.15 \%$ p.a. |  |  |  |  |
| Month $(n)$ | Principal $P$ | Interest $I$ | $P+I$ | $P+I-R$ |  |
| 1 | $\$ 390000.00$ | $\$ 1998.75$ |  |  |  |
| 2 |  |  |  |  |  |

(i) What is the amount owing at the beginning of the second month?
$\qquad$
$\qquad$
(ii) How much of the initial loan had been paid off during the first two months?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(c) Solve the equation $\frac{1}{2} a+4=\frac{5 a-6}{3}$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

|  |  |  |  |
| :--- | :--- | :--- | :--- |

Student Number
Question 27 (continued)
(d) The diagram shows the common cross-section of a carved block of wood 0.5 metres long.


Use Simpson's rule twice to determine an approximation for the area of the cross-section (giving your answer to one decimal place)
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Question 27 (continued)
(e) The diagram shows a map of the Namoi catchment area in NSW. The shaded area has been designated for forestry conservation.


Melinda flies a plane directly from Tamworth to the northwest corner of this forestry conservation area.
Using the scale given, determine the length of her journey.
Give your answer to the nearest kilometre.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## End of Question 27

|  |  |  |  |
| :--- | :--- | :--- | :--- |

Student Number

Question 28 (15 marks)
(a) The arrow on this regular pentagon is spun twice.

The result is recorded as either blue, green, orange, yellow or red.
Behind two of the colours, there is a prize of $\$ 500$.

(i) What is the probability of winning $\$ 500$ on the very first spin?
$\qquad$
$\qquad$
(ii) What is the probability of winning $\$ 500$ on the second spin only?
$\qquad$
$\qquad$
$\qquad$
(iii) What is the probability of winning at least $\$ 500$ after the two spins?
$\qquad$
$\qquad$
$\qquad$

Question 28 (continued)
(b) Toby travels 27 km from point $C$ to point $A$ on a bearing of $049^{\circ} \mathrm{T}$.

He then changes direction and travels due south for 12 km to point $B$.


Not to scale
(i) What is the size of $\angle C A B$ ?
$\qquad$
$\qquad$
(ii) Calculate the length of $B C$ (correct to the nearest metre).
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(iii) What is the area $\triangle C A B$ ?

Give your answer correct to two decimal places.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

|  |  |  |  |
| :--- | :--- | :--- | :--- |

Student Number
Question 28 (continued)
(c) The weight (in kilograms) of twelve bags of wood are listed below.

| 9 | 10 | 11 | 11 | 16 | 17 | 21 | 26 | 30 | 36 | 39 | 41 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(i) Determine the five number summary for this data.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(ii) Construct a box-and-whisker plot for this data on the grid below, displaying an appropriate scale.
(iii) Describe the skewness of this distribution
$\qquad$
$\qquad$
$\qquad$

Question 28 (continued)
(d) The time taken ( $t$ in hours) to complete a journey is inversely proportional to the average speed ( $s \mathrm{~km} / \mathrm{h}$ ).
A car takes four hours to complete a journey at an average speed of $65 \mathrm{~km} / \mathrm{h}$. Find the time taken to complete a journey if the car travels at an average speed of $80 \mathrm{~km} / \mathrm{h}$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(e) Solve these equations simultaneously, showing all working.

$$
\begin{aligned}
& 5 x-4 y=20 \\
& 3 x-4 y=12
\end{aligned}
$$

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

|  |  |  |  |
| :--- | :--- | :--- | :--- |

Question 29 (15 marks)
Student Number
(a) The table below shows Lola's average water usage per day.

| Water usage | L/day |
| :---: | :---: |
| Shower | 95 |
| Washing machine | 120 |
| Toilet | 86 |
| Other | 49 |

(i) How many kilolitres of water does Lola use in a year?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(ii) Lola is charged $\$ 2.115$ per kL for water usage.

What is the cost of her water usage for the toilet in a year?
$\qquad$
$\qquad$
$\qquad$
(b) A truck is bought by a local council for $\$ 120000$. It depreciates at $16 \%$ p.a.

Using the declining balance formula, find the total loss in value of the truck over the first three years of use.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Question 29 (continued)
(c) A raffle ticket can be bought for $\$ 10$ each. There are 100 tickets in the raffle.

There is one first prize of $\$ 500$
There are five second prizes of $\$ 50$ each.
There is one mystery prize.
How much is the mystery prize if the raffle is to have a financial expectation of zero?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(d) Alice was driving her car at $40 \mathrm{~km} / \mathrm{h}$ through a school zone.

A school student suddenly ran onto the road 15 metres in front of her.
If her reaction time is 0.50 seconds and her braking distance was 7.9 metres, was Alice able to stop her car without hitting the child? Show calculations to support your answer.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

|  |  |  |  |
| :--- | :--- | :--- | :--- |

(e) Data was collected from 16 students on the number of text messages they sent on Monday. This data is displayed in the following stem-and-leaf plot.

| Stem | Leaf |  |  |  |  |  |  |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 7 | 8 |  |  |  |  |  |
| 1 | 1 | 1 | 2 | 3 | 5 | 5 | 6 |
| 2 | 0 | 3 | 5 | 9 |  |  |  |
| 3 | 0 | 2 |  |  |  |  |  |
| 4 | 9 |  |  |  |  |  |  |

(i) What is the interquartile range of the data?
$\qquad$
$\qquad$
$\qquad$
(ii) Is 49 an outlier for this set of data? Justify your answer with suitable calculations.
$\qquad$
$\qquad$
$\qquad$
(iii) The number of text messages sent by the same 16 students on the following day (Tuesday) were collected and organised.
The following five number summary was generated from this second set of data:
$\begin{array}{lllll}8 & 12 & 14 & 28 & 51\end{array}$
Compare and contrast the two data sets by referring to measures of location and spread.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Question 29 (continued)
(f) Sarah is 20 years old and has received this quote for comprehensive car insurance.

| Premium details | Excesses | Cost |
| :--- | :---: | :---: |
| 12 month policy <br> Basic premium $\$ 678$ <br> plus | Standard | $\$ 500$ |
| pla | Male under 21 | $\$ 1200$ |
| $30 \%$ No claim bonus | Female under 21 | $\$ 900$ |

(i) Calculate the cost of her quote.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(ii) Sarah's car is valued at $\$ 16980$ by the insurance company.

To register her car for a year, she must also pay the following:

Safety check
$\$ 35$
Compulsory third-party insurance
\$498
Registration
GST $10 \%$ of the total of safety check, compulsory third party and registration

Find the total amount that Sarah must pay in order to have her car registered and comprehensively insured using the above quote.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(a) Darren's bucket is initially filled with 4 litres of water.

Sadly, the bucket has a hole in its base and is leaking at a rate of 20 millilitres per minute.
(i) Write a linear equation in the form $V=m t+b$ to describe this situation
(ii) What volume of water remains after 150 seconds?
$\qquad$
$\qquad$
$\qquad$
(iii) How long would it take for all the water to leak out?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(b) Jack has a mobile phone contract that charges a monthly access fee of $\$ 79$ with included calls worth $\$ 250$, a call connection fee of $\$ 0.35$ and call rate of $\$ 0.45$ per 30 second or part thereof.
What is the monthly charge if Jack made 300 calls, each with duration less than 30 seconds?
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Question 30 (continued)
(c) Matthew investigated a comparison between the forearm length and hand length of 10 male friends.

His results were recorded in the table below. All lengths are in centimetres.

| Forearm length $(\boldsymbol{x})$ | 25.1 | 25.4 | 25.9 | 26.4 | 26.7 | 27.3 | 27.7 | 28.2 | 28.8 | 29.3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Hand length $\boldsymbol{y}$ ) | 17.3 | 17.5 | 18.2 | 18.4 | 19.3 | 19.6 | 19.8 | 20.0 | 20.2 | 20.3 |

He used the data to produce the scatterplot below.

(i) Find the correlation coefficient (correct to two decimal places) and explain what this indicates about the relationship between forearm length and hand length.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

|  |  |  |  |
| :--- | :--- | :--- | :--- |

(ii) Complete the table below by calculating the mean, $\bar{y}$, and standard deviation $\sigma_{y}$ for the hand length data (correct to two decimal places).

|  | Mean | Standard Deviation |
| :--- | :--- | :--- |
| Forearm length | $\bar{x}=27.08$ | $\sigma_{x} \approx 1.35$ |
| Hand length | $\bar{y}=$ | $\sigma_{y} \approx$ |

(iii) Using the figures in this table, prove the equation of the least squares line of best fit is:

$$
y=0.75 x-1.25
$$

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(iv) Use the equation to predict the hand length when the forearm length is 24 cm .
$\qquad$
$\qquad$
(v) Sketch the least squares line of best fit onto the scatter plot presented on page 30.
(vi) Can Matthew use this line of best fit to predict the hand length of his sister who has forearm length of 15 cm ? Explain your answer.
$\qquad$
$\qquad$
$\qquad$

Question 30 (continued)
(d) The diagram below shows a garden bed in the shape of an annulus with a sector removed.


Find the perimeter of this unusual garden bed.
Give your answer in metres correct to two decimal places.
$\qquad$
$\qquad$
$\qquad$
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$\qquad$


Student Number

## Section II Extra writing space

If you use this space, clearly indicate which question you are answering.
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## Section II Extra writing space

If you use this space, clearly indicate which question you are answering.
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# MATHEMATICS GENERAL 2 <br> FORMULAE AND DATA SHEET 

## Financial Mathematics

## Simple Interest

$$
I=\operatorname{Prn}
$$

$P$ is initial amount
$r \quad$ is interest rate per period, expressed as a decimal
$n$ is number of periods

## Compound Interest

$$
A=P(1+r)^{n}
$$

$A$ is final amount
$P$ is initial amount
$r$ is interest rate per period, expressed as a decimal
$n$ is number of compounding periods

## Present value and future value

$$
P V=\frac{F V}{(1+r)^{n}}, \quad F V=P V(1+r)^{n}
$$

$r$ is interest rate per period, expressed as a decimal
$n$ is number of compounding periods

## Straight-line method of depreciation

$$
S=V_{0}-D n
$$

$S$ is salvage value of asset after $n$ periods $V_{0}$ is initial value of asset
$D$ is amount of depreciation per period
$n$ is number of periods

## Declining-balance method of depreciation

$$
S=V_{0}(1-r)^{n}
$$

$S \quad$ is salvage value of asset after $n$ periods
$V_{0}$ is initial value of asset
$r$ is depreciation rate per period, expressed as a decimal
$n$ is number of periods

## Data Analysis

## Mean of a sample

$$
\bar{x}=\frac{\text { sum of scores }}{\text { number of scores }}
$$

## $z$-score

For any score $x$,

$$
z=\frac{x-\bar{x}}{s}
$$

$\bar{x}$ is mean
$s$ is standard deviation

## Outlier(s)

score(s) less than $Q_{L}-1.5 \times I Q R$
or
scores(s) more than $Q_{U}+1.5 \times I Q R$
$Q_{L} \quad$ is lower quartile
$Q_{U} \quad$ is upper quartile
$I Q R$ is interquartile range

## Least-squares line of best fit

$y=$ gradient $\times x+y$-intercept
gradient $=r \times \frac{\text { standard deviation of } y \text { scores }}{\text { standard deviation of } x \text { scores }}$
$y$-intercept $=\bar{y}-($ gradient $\times \bar{x})$
$r$ is correlation coefficient
$\bar{x} \quad$ is mean of $x$ scores
$\bar{y}$ is mean of $y$ scores

## Normal distribution

- approximately $68 \%$ of scores have $z$-scores between -1 and 1
- approximately $95 \%$ of scores have $z$-scores between - 2 and 2
- approximately $99.7 \%$ of scores have $z$-scores between - 3 and 3


## Spherical Geometry

## Circumference of a circle

$$
C=2 \pi r \text { or } C=\pi D
$$

$r$ is radius
$D$ is diameter

## Arc length of a circle

$$
l=\frac{\theta}{360} 2 \pi r
$$

$r$ is radius
$\theta$ is number of degrees in central angle

## Radius of Earth

(taken as) 6400 km

## Time differences

For calculation of time differences using longitude: $15^{\circ}=1$ hour time difference

## Area

## Circle

$$
A=\pi r^{2}
$$

$r$ is radius

## Sector

$$
A=\frac{\theta}{360} \pi r^{2}
$$

$r$ is radius
$\theta$ is number of degrees in central angle

## Annulus

$$
A=\pi\left(R^{2}-r^{2}\right)
$$

$R \quad$ is radius of outer circle
$r$ is radius of inner circle

## Trapezium

$$
A=\frac{h}{2}(a+b)
$$

$h$ is perpendicular height $a$ and $b$ are the lengths of the parallel sides

## Area of land and catchment areas

unit conversion: $1 \mathrm{ha}=10000 \mathrm{~m}^{2}$

## Surface Area

## Sphere

$$
A=4 \pi r^{2}
$$

$r$ is radius

## Closed cylinder

$$
A=2 \pi r^{2}+2 \pi r h
$$

$r$ is radius
$h$ is perpendicular height

## Volume

## Prism or cylinder

$$
V=A h
$$

$A$ is area of base
$h$ is perpendicular height

## Pyramid or cone

$$
V=\frac{1}{3} A h
$$

$A$ is area of base
$h$ is perpendicular height

## Volume and capacity

unit conversion: $1 \mathrm{~m}^{3}=1000 \mathrm{~L}$

## Approximation Using Simpson's Rule

## Area

$$
A \approx \frac{h}{3}\left(d_{f}+4 d_{m}+d_{l}\right)
$$

$h$ is distance between successive measurements
$d_{f}$ is first measurement
$d_{m}$ is middle measurement
$d_{l}$ is last measurement

## Volume

$$
V \approx \frac{h}{3}\left\{A_{L}+4 A_{M}+A_{R}\right\}
$$

$h$ is distance between successive measurements
$A_{L}$ is area of left end
$A_{M}$ is area of middle
$A_{R}$ is area of right end

Trigonometric Ratios
opposite side

$\sin \theta=\frac{\text { oppositeside }}{\text { hypotenuse }}$
$\cos \theta=\frac{\text { adjacentside }}{\text { hypotenuse }}$
$\tan \theta=\frac{\text { oppositeside }}{\text { adjacentside }}$

## Sine rule

In $\triangle A B C$,

$$
\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}
$$

## Area of a triangle

In $\triangle A B C$,

$$
A=\frac{1}{2} a b \sin C
$$

## Cosine Rule

In $\triangle A B C$,

$$
\begin{aligned}
& c^{2}=a^{2}+b^{2}-2 a b \cos C \\
& \text { or } \\
& \cos C=\frac{a^{2}+b^{2}-c^{2}}{2 a b}
\end{aligned}
$$

## Units of Memory and File Size

$$
\begin{aligned}
1 \text { byte } & =8 \text { bits } \\
1 \text { kilobyte } & =2^{10} \text { bytes }=1024 \text { bytes } \\
1 \text { megabyte } & =2^{20} \text { bytes }=1024 \text { kilobytes } \\
1 \text { gigabyte } & =2^{30} \text { bytes }=1024 \text { megabytes } \\
1 \text { terabyte } & =2^{40} \text { bytes }=1024 \text { gigabytes }
\end{aligned}
$$

## Blood Alcohol Content Estimates

$B A C_{\text {male }}=\frac{10 N-7.5 H}{6.8 M}$
or
$B A C_{\text {female }}=\frac{10 \mathrm{~N}-7.5 H}{5.5 M}$
$N$ is number of standard drinks consumed
$H$ is number of hours of drinking
$M$ is person's mass in kilograms

## Distance, Speed and Time

$$
D=S T, \quad S=\frac{D}{T}, \quad T=\frac{D}{S}
$$

average speed $=\frac{\text { total distance travelled }}{\text { total time taken }}$
stopping distance $=\left\{\begin{array}{c}\text { reaction-time } \\ \text { distance }\end{array}\right\}+\left\{\begin{array}{c}\text { braking } \\ \text { distance }\end{array}\right\}$

## Probability of an Event

The probability of an event where outcomes are equally likely is given by:

$$
P(\text { event })=\frac{\text { number of favourable outcomes }}{\text { total number of outcomes }}
$$

## Straight Lines

## Gradient

$$
m=\frac{\text { vertical change in position }}{\text { horizontal change in position }}
$$

## Gradient-intercept form

$$
y=m x+b
$$

$m$ is gradient
$b$ is y-intercept

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General2 Triac Somptious $2015 \quad$ 22. A let $y=$ vertical line

Multiple Chore.

1. D
2.C $24 \times 23=552$
2. $B \quad 6 x^{4}-6 x^{2}+2 x^{2}=6 x^{4}-4 x^{2}$
3. A $280 \div 110=2.54 \quad 2.54 \times 10=25.45124 . A$
S.C $240 \times 7.46=1790.40$
4. $B$
5. $A \quad y$ int $=1 \quad m=-\frac{3}{1}$

$$
y=-3 x+1
$$

8. $C \quad 50+5=250$
9. $C \quad 6 \times 15-10+20=100 \quad 100 \div 6=6.726$.
10. $D \quad \frac{27}{270} \times 360=36$
11. A $V=\frac{1}{3} \times \pi \times\left(\frac{5}{2}\right)^{2} \times 13=85.08$
12. D $0.5 \times 1024 \times 1024 \times 1024 \times 1024$
13. $B$
14. $B$

$$
\begin{aligned}
& 13=2 q^{3}-1 \\
& 14=2 q^{3} \\
& 7=q^{3} \\
& q=\sqrt[3]{7}
\end{aligned}
$$

$15 D$
16. $D \quad \angle B C S=75$ (alt $\angle$ 's 11$)$

$$
180+75+30=285
$$

17. $C \quad 194000(1+0.067)^{25}=981550$
$981550-194000=787550$
18. $C \quad(0.8 \times 0.3)+(0.2 \times 0.7)=0.38$
19. $B \quad B D^{2}=5^{2}-4^{2} \quad A B^{2}=7^{2}+3^{2}$

$$
B D=3 \quad A B=7.6
$$

20. $B \quad 7.25 \times \frac{310}{100}=22.475$
21.C $40500 \times 0.85 \times 0.9 \times 0.92$

$$
=28503.90
$$

$$
\frac{28503.90}{40.500}=0.70
$$

$$
\begin{aligned}
& y=6 \sin 44 \\
& \tan 34=\frac{6 \sin 44}{x} \\
& x=\frac{6 \sin 44}{\tan 34}
\end{aligned}
$$

23. D $\quad \frac{\mathrm{s}}{500}=1-r \quad r=1-\frac{\mathrm{S}}{500}$

$$
\begin{array}{rlrl}
x+4 & =-x-4 & y & =-4+4 \\
2 x & =-8 & & =0 \\
x & =-4 & \therefore(-4,0)
\end{array}
$$

$25 A \quad \frac{10}{40}=\frac{1}{4}$

Section 2

$$
\text { 2) } \sqrt{\frac{5.9+3 \times 2.4}{4 \times 2.4}}=1.16815=1.2
$$

b) $350 \mathrm{mg} / 100 \mathrm{~mL}$

$$
0.35 \mathrm{~g} / 100 \mathrm{~mL}
$$

$0.0035 \mathrm{~g} / \mathrm{mL}$
c) $\frac{h}{2.7}=\frac{5}{2} \quad h=6.75$
d) $A=\frac{21}{2}(24+15)=409.5$
ii. $409.5 \times 2=819$

$$
15 \times 6=90
$$

$$
21 * 6=126
$$

$$
\frac{24 \times 6}{\text { Total }}=\frac{144}{1179}
$$

iii) $1179 \div 10000=0.1179 m^{2}$

$$
0.1179 \times 50 \times 4.29=\$ 25.29
$$

e) i, $9000 \times 4.2124=\$ 37911.60$
ii, $6000 \times 3.9020=\$ 23412$
iii) $x \times 2.5771=43230$

$$
x=\$ 16775
$$

f)

$$
\begin{aligned}
& 0.05= 10 \times 6-7.5 \mathrm{H} \\
& 25.8 \times 7.5 \\
& 7.5 H=60-7.5 \mathrm{H} \\
& H=4.6 \mathrm{hr} \rightarrow 4 \mathrm{hr} 36 \mathrm{~min}
\end{aligned}
$$

$$
\therefore 4 \mathrm{hr} 40 \mathrm{~min}
$$

Time taken for download
(27. a) $i$

(Class centres)
; 38 (accept 36-39)
ii) $45-22=23$ (accept 21-24)
iii y No as it is a grouped freq table
we do not know what each
download was exactly.
b) i, 389898.75
ii) $390000-389796.98=\$ 203.02$
c)

$$
\begin{aligned}
\frac{3}{2} a+12 & =5 a-6 \\
3 a+24 & =10 a-12 \\
36 & =7 a \\
a & =\frac{36}{7}
\end{aligned}
$$

d)

$$
\begin{aligned}
A_{1}=\frac{2.7}{3}(0+4 \times 1.3+2.3) & =6.75 \\
A_{2}=\frac{2.7}{3}(2.3+4 \times 3.5+0) & =14.67 \\
\text { Total } & =21.4 \mathrm{~cm}^{2}
\end{aligned}
$$

e) meas $=6.6 \mathrm{~cm}$ scale $2.2 \mathrm{~cm}=80 \mathrm{~cm}$

$$
6.6 \div 2.2=3 \quad 3 \times 80=240 \mathrm{~km}
$$

28
a) $i, \frac{2}{5}$
ii, $\frac{3}{5} \times \frac{2}{5}=\frac{6}{25}$
iii) $1-\left(\frac{3}{5} \times \frac{3}{5}\right)=\frac{16}{25}$
b) ; 49 (alt $\angle$ with $\angle C A B$ )

$$
\text { ii) } B C^{2}=27^{2}+12^{2}-2 \times 27 \times 12 \times \cos 49
$$

$$
B C=21.16
$$

iii. $A=\frac{1}{2} \times 27 \times 12 \times \sin 49$

$$
=122.26 n^{2}
$$

c) $i, 9,11,19,33,41$

iii positively skewed
d)

$$
\begin{aligned}
t & =\frac{k}{s} \\
4 & =\frac{k}{65} \\
k & =260
\end{aligned} \quad \therefore t=\frac{260}{80}, ~=3.25 \mathrm{hrs}
$$

e)

$$
\begin{align*}
5 x-4 y & =20  \tag{1}\\
3 x-4 y & =12  \tag{2}\\
(1)-2 & \\
2 x & =8 \\
x & =4
\end{align*}
$$

sub $x=4$ into (1)

$$
\begin{aligned}
5 \times 4-4 y & =20 \\
-4 y & =0 \\
y & =0
\end{aligned} \quad \begin{aligned}
& =4 \\
& =0
\end{aligned}
$$

29. 

$$
\text { a) i, } 350 \times 365=127750 \mathrm{~L}
$$

$$
=127.75 \mathrm{~kL}
$$

ii) $0.086 \times 365=31.39 \mathrm{~kL}$
$31.39 \times 2.115=\$ 66.39$

$$
\text { b) } \begin{aligned}
A & =120000(1-0.16)^{3}=71124.48 \\
120000-71124.48 & =\$ 48875.52
\end{aligned}
$$

c) $\frac{1}{100} \times 500+\frac{5}{100} \times 50+\frac{1}{100} \times x-10=0$

$$
\begin{aligned}
7.5+\frac{x}{100} & =10 \\
\frac{x}{100} & =2.5 \\
x & =250
\end{aligned}
$$

d) $40 \mathrm{~km} / \mathrm{h} \rightarrow 40000 \mathrm{~m} / \mathrm{h} \rightarrow 11 \mathrm{~m} / \mathrm{sec}$

$$
\begin{aligned}
& \therefore 5.5 \mathrm{~m} / \frac{1}{2} \mathrm{~s} \\
& 5.5+7.9=13.4 \mathrm{~m}
\end{aligned}
$$

yes she will stop before the child iv
e); $27-11.5=15.5$

$$
\therefore 27+1.5 \times 15.5=50.25
$$

No as 49 is less than 50.25
iii, They are very similar as the medians an ty differ by 1.5 and the ranges only differ by 1
f) i, $678 \times 0.70=\$ 474.60$
ii) $\operatorname{Rego}(35+498+0.02 \times 16980) \times 1.10$ $=959.86$

$$
\begin{aligned}
\text { Total }- & 959.86+474.60 \\
= & 1434.46
\end{aligned}
$$

30
a) $i v=4000-20 t \quad 0$

$$
v=4-0.02 t
$$

$$
\begin{aligned}
i v & =4000-20 \times 2.5 \\
& =3950 \mathrm{~mL}
\end{aligned}
$$

iii

$$
\begin{aligned}
0 & =4000-20 t \\
20 t & =4000 \\
t & =200 \mathrm{~min}
\end{aligned}
$$

b) $300 \times(0.35+0.45)=\$ 240$
$\therefore$ only pays $\$ 79$
c) $i r=0.96$
strong positive correlation
ii $\bar{y}=19.06 \quad \sigma_{y}=1.06$
iii gradient $=0.96 \times \frac{1.06}{1.35}$

$$
\begin{aligned}
& =0.75 \\
y \text {-int } & =19.06-(0.75 \times 27.08) \\
& =-1.25
\end{aligned}
$$



$$
=16.75 \mathrm{~cm}
$$

vi, No-as this graph is for men
oe - it is beyond the bounds of the data points on this graph
d) Inside -

$$
\begin{aligned}
P & =2 \times \pi \times 1.5 \times \frac{290}{360} \\
& =7.592
\end{aligned}
$$

Outside $P=2 \times \pi \times(1.5+1.2) \times \frac{290}{360}$

$$
=13.666
$$

Ends

$$
\begin{aligned}
P & =2 \times 1.2 \\
& =2.4
\end{aligned}
$$

Total

$$
\begin{aligned}
P & =7.592+13.666+2.4 \\
& =23.66 \mathrm{~m}
\end{aligned}
$$

